# A MORPHOMETRIC STUDY OF YELLOWFIN TUNA THUNNUS ALBACARES (BONNATERRE) 

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#### Abstract

Morphometric measurements were compared for 4,180 yellowfin tuna from 28 locations in the Pacific Ocean; from off Angola, Africa, in the Atlantic Ocean; and from off Somaliland, Africa, in the Indian Ocean. The measurements used were head length; pectoral fin length; heights of second dorsal and anal fins; distances from snout to insertion of first dorsal fin, to second dorsal fin, anal fin, and ventral fin; distance from insertion of ventral to anterior edge of vent; and greatest body depth. Each measurement was related to fork length by regression analysis, and each relationship was considered a character. Curvilinear regression due to allometric growth was controlled by transforming some data to logarithms and by separating all samples into small, medium, and large size groups (less than 80, $\mathbf{8 0 - 1 2 0}$, and greater than $\mathbf{1 2 0} \mathrm{cm}$. fork lengths). Mean character sizes were determined for each sample at lengths of 65,100 , and 140 cm .

A comparison of mean character sizes revealed a cline in most characters from samples taken along the Pacific Equator between the vicinity of Costa Rica and the Caroline Islands. Yellowfin from the eastern Pacific have larger heads and greater distances from snout to insertion of first dorsal, second dorsal, ventral, and anal fins; a greater distance from insertion of ventral fins to insertion of anal fin; and a greater body depth. On the other hand, they have shorter pectoral fins and much shorter anal and second dorsal fins. The samples from the more temperate parts of the Pacific and from off the coasts of Africa differed little from some part of this cline.

A multiple character comparison of overlap among samples from near the Pacific Equator showed less than $\mathbf{5 0}$-percent overlap between samples separated by 1,500 miles, less than $\mathbf{2 5}$-percent overlap between samples separated by 3,000 miles, and less than 6 -percent overlap between samples separated by 6,000 miles. The possibility of long intermigrations among the equatorial stocks seems remote.

The full variation in length of the pectoral fin and heights of second dorsal and anal fins, which most authors have used to separate the species of yellowfin, occurs within the cline along the Pacific Equator. This occurrence, plus the continuous circumtropical high seas distribution of the yellowfin, indicates a single worldwide species. The appropriate name is Thunnus albacares (Bonnaterre) 1788.


A problem of immediate concern to us in investigation of the tuna fisheries of the Pacific is to determine the degree of intermingling of the tuna populations. Intermingling matters because tunas are being sought in different parts of the ocean by fishermen who are asking whether the catch by one nation in one area is affecting the population of tunas and catch by another nation in another area. In other words, do these tunas migrate thousands of miles, as do some of our migratory birds, or are they relatively localized, hatching, maturing, and
dying within an area of a few hundred miles? A closely related matter of secondary concern is to distinguish the species and subspecies of each kind of tuna in the oceans of the world.

Among the tuna fisheries of the Pacific, those for the yellowfin (Thunnus albacares) ${ }^{1}$ are the most

[^0]important. The yellowfin is a major fishery resource from California to Chile and from Japan to Indonesia, especially near the Caroline Islands. Smaller fisheries also exist off Hawaii, Australia, and many of the islands of the central Pacific. In addition, exploration by the Bureau of Commercial Fisheries Pacific Oceanic Fishery Investigations (POFI) ${ }^{2}$ in the central Pacific revealed major concentrations of yellowfin along the Equator from longitude $110^{\circ} \mathrm{W}$. to $180^{\circ}$. These stocks were fished repeatedly by research vessels and subsidized commercial vessels between 1950 and 1955. The methods and results have been summarized by Sette (1954) and detailed by Murphy and Shomura (1953a, 1953b, and 1955) and Shomura and Murphy (1955). Since 1955 these populations have been fished with increasing intensity by Japanese commercial concerns.

One appronch to the general problem of relations among Pacific tuna stocks has been through morphometric studies. Workers have included Schaefer (1948), who described the morphometric characteristics and relative growth of yellowfin off central America; Godsil (1948), who made a preliminary population study of yellowfin and albacore, Germo alalunga (Bonnaterre); Schaefer and Walford (1950), who compared yellowfin from off Angola, Africa, and the Pacific coast of Central America; Schaefer (1952), who compared yellowfin from the Hawaiian Islands with those from the Pacific coast of Central America; Royce (1953), who compared numerous groups of Pacific yellowfin; Tsuruta (1954), who compared yellowfin from the Gilbert Islands with those from Hawaii; and Schaefer (1955), who further compared yellowfin tuna from Central America and Hawaii with those of southeastern Polynesia.

A different technique, which may provide direct evidence of intermingling, has been applied by the California Department of Fish and Game, Marine Fisheries Branch, and used subsequently by other groups. Yellowfin, albacore, and skipjack, Katsuwonus pelamis (Linnaeus), have been tagged with plastic tags, as reported by Wilson (1953), and have already shown some remarkable migrations. One albacore released 18 miles south of Los Angeles, California, was recovered nearly 1 year later about 5,000 miles distant at latitude $31^{\circ} 30^{\prime} \mathrm{N}$., longitude $149^{\circ} 40^{\prime} \mathrm{E}$., off the coast of

[^1]Japan (Ganssle and Clemens, 1953) and two other albacore, tagged near Guadalupe Island, were recovered about 6 months later in the vicinity of Midway Island (Blunt, 1954). Yellowfin also were tagged off the Line Islands from March 1955 to February 1956 (Iversen and Yoshida, 1957). Of the 1,056 that were released, 2 were recaptured locally and 1 was recovered 800 miles east of the point of release after being at liberty 13 months. But these tag returns are as yet too few to provide good evidence of the extent of intermingling or of any different migratory behavior of the several species.

Much interest in these problems of intermingling of tuna populations has been expressed at various meetings of the Indo-Pacific Fisheries Council, and the collection of data has been a matter of major concern to its Tuna Subcommittee. Through this organization the aid of numerous people in the Indo-Pacific area has been enlisted in the collection of data, which have been used in this report. This interest has also been expressed by some independent studies along the same lines in other countries, particularly in Japan by Tsuruta (1954) and in Australia where morphometric studies are underway.

## STATISTICAL COMPARISON OF MORPHOLOGICAL DATA

The following section is a summary of a general review of the problem involved in statistical comparisons of morphological data previously made by Royce (1957).

In all morphometric studies of yellowfin tuna the authors have used essentially the same methods. All have used measurements of body parts, especially lengths and heights of the fins and distances from the snout to insertion of the fins, as principal characters. All have used regression analysis to relate part size to fork length and then have compared samples by covariance analysis. All have found much larger differences between samples than would be expected from chance variations, and from such differences there has been a tendency to conclude that the populations were distinct.

But this method of analysis is not wholly satisfactory. It provides a test of whether a difference is significant, but this conclusion may be trivial, because significant differences can be found commonly between even the most closely related
natural populations (Mayr, Linsley, and Usinger, 1953: 151). It does not show how great the differences are in terms that can readily be compared. It does not provide evidence of clines or character gradients, which are to be expected in tuna populations because of their continuous distribution and which are useful indicators of relations of the populations. Neither do the methods in current use provide information on the key problem of the amount of intermingling.

Use of regression analysis to relate size of body parts to fork length does provide basic data needed for finding clines according to the method described by Hubbs and Hubbs (1953). The regression statistics provide the mean character size estimated for a fixed length of fish; the measure of dispersion about the mean, which is the standard deviation from regression; and the measure of reliability, which is the standard error of the estimated mean. I showed that clines exist among yellowfin tuna populations (Royce, 1953), but I did not use the method of Hubbs and Hubbs nor employ sufficiently precise methods of regression analysis. In this paper I will use more refined methods of regression analysis and try to show fully the nature of the clines.

The problem of intermingling will be approached through an exterision of the concept of overlap, which has been applied to comparison of natural populations by many taxonomists. The methods in current use have been summarized by Mayr, Linsley, and Usinger (1953: 142). They have indicated overlap between populations by a coefficient of difference (CD), which is computed according to the formula-

$$
\mathrm{CD}=\frac{\bar{x}_{1}-\bar{x}_{2}}{s_{1}+s_{2}}
$$

The overlap is the difference between means $\bar{x}_{i}$ divided by the sum of standard deviations $s_{i}$ of the two populations. I prefer to change this formula slightly to-.

$$
D=\frac{\bar{x}_{1}-\bar{x}_{2}}{s}
$$

in which $s$ is the within-sample standard deviation computed from the pooled variance, and $D$ is the distance between the means in the standard measure of statistics, i.e., in units of the standard deviation. It is obvious that $\mathrm{CD} \simeq \frac{D}{2}$.

The concept of overlap of two frequency distributions is shown graphically ( 1 A and 2 A ) in figure 1. The mutual area (1B and 2B) of


Figure 1.-Overlap of normal distributions. 1A and 2A indicate normal populations which overlap in the shaded areas 1B and 2B; $s$ indicates one standard deviation, $\bar{x}_{1}$ and $\bar{x}_{2}$ indicate means; $D$ is the distance between means in units of the standard deviation.
the two curves is shaded; one-half of the shaded area, or tail of one distribution, which I designate as $p$, may be determined readily from a table of the probability integral, such as table 2 in Pearson (1948). The table is entered with the value of $\frac{D}{2}$. The value of $p$ represents the probability
of misclassifying the individuals on the basis of the character used. When the two means are identical and the chances of making a proper choice are equal, $p$ will range from 0.5 to essentially zero when the two curves are widely separated, and for all practical purposes there is no overlap. However, the value $p$, while indicative of overlap, is not fully satisfactory because it approaches a maximum of 0.5 and because it must be considered properly as a probability of misclassification rather than a measure of the mutual area of the frequency curves.

A more satisfactory measure of overlap may be obtained if one considers the area of one frequency curve and within it the proportion ( $2 p$ ) that might belong to another specified frequency curve. I have designated this by $\Omega=200 p$, expressed as a percentage. It is a measure of overlap which will be 100 percent when the curves have the same mean and will approach zero as the means become widely separated.

The particular usefulness of $\Omega$ is in the concept that it is an estimate of the proportion of one sample with the characteristics of another. If the samples are representative of populations in
a specific time and place, it follows that $\Omega$ is that proportion which might have come from another population, and thus the value of the overlap indicates a maximum for the amount of intermingling. The overlap $\Omega$ does not show that intermingling has occurred, and when large it merely shows that a large amount of intermingling may have occurred. Whether intermingling did occur must be determined by other means. When $\Omega$ is small, however, and we can establish that the characters used do not change during migration, we may then be able to establish that no significant intermingling occurs.

The most satisfactory measure of overlap is obtained from several characters simultaneously, which requires a substantial extension of the computations. The measure in current use by most taxonomists has been applied merely to comparisons of single counted characters. I have shown (Royce, 1957) that it may be applied readily to single measured characters through substitution of the regression statistics. The much greater extension to multiple characters is based on $D$ as already defined. The use of $D$ as a distance between populations has been generalized for multiple characters by Mahalanobis (1936). In his generalization, each additional character adds to $D$ only to the extent that it is not correlated with previously considered characters. Thus, all arbitrary combinations of characters as ratios or indices are avoided. Rao (1947, 1952) pointed out that $D$ satisfies two fundamental postulates of distance: (1) the distance between two groups is not less than zero; (2) the sum of distances from one group to two other groups is not less than the distance between the two other groups (triangle law of distance). The further empirical requirement that the distance must not decrease when additional characters are considered is also satisfied.

## AVAILABLE DATA

There were available for this study 28 samples of yellowfin from the Pacific Ocean, 1 from the Atlantic Ocean off Angola, Africa, 1 from the Indian Ocean off Somaliland in northeast Africa, and 1 of only 3 specimens from off Ceylon. ${ }^{3}$ The data include the measurements of yellowfin

[^2]from off the American coast published by Godsil (1948), whose 13 samples have been combined into 6; those from off Costa Rica by Schaefer (194S); from Angola by Schaefer and Walford (1950); from Fiji, Palmyra, and Hawaii by Godsil and Greenhood (1951); from Hawaii by Schaefer (1952); and those from the Gilbert Islands by Tsuruta (1954). The original measurements of most of the remaining samples were published by Dung and Royce (1953). The remainder, a sample from the Pacific Equator near longitude $110^{\circ} \mathrm{W}$. and another from northeast Africa, are listed in appendix tables 1 and 2.

The geographic distribution of Pacific samples is shown in figure 2. There is an excellent series from about S, 000 miles along the Pacific Equator between the American coast and the central Caroline Islands. In addition, there are samples from the South Pacific off the Fiji and Society Islands, and from the North Pacific off the Philippines, Japan, Bikini Island, Hawaii, Mexico, and Guatemala. All major areas of the Pacific where yellowfin are known to occur are included except the South American coast and the southwest Pacific from Australia to the coast of Asia.

It was necessary to omit four samples from the Pacific. Those from the western Marshall, western Caroline, and Fiji Islands have not been further considered, because they contain less than 20 fish, the number I arbitrarily established as the minimum. In another sample from near the Gilbert Islands, reported by Tsuruta (1954), measurements of one specimen are questionable (No. 2 in his table 1), and I have been unable to verify the computations shown in his table 2 . Fairly large discrepancies occur in the regression statistics, apparently because enough digits were not carried during the computations. This sample was obtained on only 3 days from a limited area. For these reasons I have not further considered it.

Certain basic statistics about the samples will be needed repeatedly in the ensuing discussion and are presented here. The length distribution of all samples is shown in table 1. Pertinent data on how the samples finally used were collected are shown in table 2 . The sums, sums of squares, and sums of products for all characters of all samples which have not been published are given in appendix table 3. Included, also, are the means, regression constants, and estimated character sizes at certain lengths for all samples.


Figure 2.-Geographic distribution of Pacific samples of yellowfin tuna. ( X indicates approximate center of distribution of fish comprising each sample from Hawaii and the equatorial area. (G) indicates Godsil, 1948; ( $\mathrm{G} \& \mathrm{G}$ ) Godsil and Greenhood, 1951; ( $\mathbf{S}$ ) Schaefer, 1952; (T) Tsuruta, 1954.)

MORPHOLOGICAL CHARACTERS USED
The morphological characters I have used in this study were selected through precedent and experience. The precedent was established by several workers who attempted thorough morphometric studies. None of the recent workers (Schaefer, 1948; Godsil, 1948; or Schaefer and Walford, 1950) explained how they selected their characters, but undoubtedly they were guided by previous research reported in the literature in which yellowfin tuna had been differentiated largely on the basis of fin length. Godsil (1948) defined 16 measurements but presented data on only 6: fork length; head length; and distances from the snout to insertion of first dorsal, second dorsal, anal, and ventral fins. He states that he investigated counts but discarded them because they were unsatisfactory. Schaefer (1948) used five of these measurements (he did not measure snout to insertion of ventral fin). He added the greatest body depth; length or height of the pectoral, second dorsal, and anal fins; longest dorsal
finlet and dorsal ray; distance from pectoral fin insertion to insertion of first dorsal fin; length of the base of first dorsal fin; diameter of iris; and length of maxillary. In addition, he obtained four counts: number of dorsal fin rays (including spines if any), dorsal finlets, anal finlets, and gill rakers.

Schaefer and Walford (1950), for part of the specimens measured off Angola, Africa, used the same measurements as Schaefer (1948), but added spread of caudal fin, length of first dorsal spine, least depth of caudal peduncle, greatest width of caudal peduncle at keels, and snout to insertion of ventral fins. They also obtained the same four counts and recorded the sex of some of the fish. Subsequently, this list of measurements was markedly reduced by Schaefer (while he was directing the morphometric program at POFI) to fork length; head length; snout to insertion of first dorsal, second dorsal, anal, and ventral fins; length or height of pectoral, second dorsal, and anal fins; greatest body depth; and diameter of the

Table 1.-Number of tuna measured, by size interval and place of collection.

| Arca | Number of fish in fork length (em.) interval of- |  |  |  |  |  |  |  |  |  |  |  |  |  |  | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $30-$ 39.9 | $\begin{aligned} & 40- \\ & 49.9 \end{aligned}$ | $\begin{array}{r} 50- \\ 59.9 \end{array}$ | $\begin{gathered} 60- \\ 69.9 \end{gathered}$ | $\begin{gathered} 70- \\ 79.9 \end{gathered}$ | $\begin{array}{r} 80- \\ 89.9 \end{array}$ | $\begin{gathered} 90-1 \\ 99.9 \end{gathered}$ | $\begin{aligned} & 100- \\ & 109.9 \end{aligned}$ | $\begin{aligned} & 110- \\ & 110.0 \end{aligned}$ | $\begin{aligned} & 120- \\ & 120.9 \end{aligned}$ | $\begin{array}{r} 130- \\ 139.9 \end{array}$ | $\begin{aligned} & 140- \\ & 149.9 \end{aligned}$ | $\begin{aligned} & 150- \\ & 159.9 \end{aligned}$ | $160-$ | $\begin{aligned} & 170- \\ & 179.9 \end{aligned}$ |  |
| Mexico ${ }^{1}$ |  |  | 52 | 143 | 155 | 8 | 3 |  |  |  |  |  |  |  |  | 361 |
| Guatenala ${ }^{\text {d }}$ |  |  | 49 | 54 | 16 | 1 |  |  |  |  |  |  |  |  |  | 120 |
| Panama and Costa Rica |  | 1 | 129 | 283 | 282 | 36 | 42 | 43 | 48 | 20 | 3 |  |  |  |  | 887 |
| Costa Rica ${ }^{2}-1$ |  |  | 2 | 7 | 3 | 6 | 11 | 6 | 6 | 2 |  | 2 | 1 |  |  | 46 311 |
| Cocos Island 1 |  | 6 | 8 | 36 | 128 | 80 | 28 | 2 |  | 4 | 10 | 5 | 4 |  |  | 311 |
| Galapagos Island ${ }^{1}$ |  |  | 97 | 14 | 9 | 65 | 9 |  |  |  |  |  |  |  |  | 194 |
| Clipperton Island 1 |  |  | 1 | 21 | 7 | 4 | 2 | 1 | 2 |  |  |  |  |  |  | 38 |
| $109^{\circ}-119^{\circ} \mathrm{W}$---- |  |  |  |  | 1 | 2 |  | 1 | 2 | 3 |  | 7 | 5 | 6 |  | 27 |
| $119^{\circ}-129^{\circ} \mathrm{W}$ - |  |  |  |  |  |  |  |  |  | 3 | 10 | 15 | 14 | 4 |  | 47 |
| $129^{\circ}-139^{\circ} \mathrm{W}$. |  |  |  | 1 | 1 |  | 1 |  |  | 5 | 5 | 12 | 10 | 11 |  | 46 |
| $139^{\circ}-149^{\circ} \mathrm{W}$-- |  |  |  |  |  |  |  |  |  | 4 | 25 | 29 | 33 | 20 | 2 | 113 |
| East Line Islands |  |  |  | 1 | 4 | 4 | 8 | 16 | 5 | 12 | 35 | 48 | 52 | 10 |  | 195 |
| West Line Islands |  | 1 | 5 | 16 | 22 | 28 | 22 | 19 | 17 | 11 | 21 | 18 | 7 | 1 |  | 188 |
| Palmyra Island ${ }^{3}$ |  |  | 1 | 10 | 24 | 18 | 27 | 10 | $\frac{2}{15}$ | 15 |  | 1 |  |  |  | 94 |
| Phoenix Islands |  |  | 4 | 19 | 14 | 16 | 19 | 9 | 15 | 15 | 21 | 7 | 2 | 1 |  | 142 |
| East Marsiall Islands. |  |  |  |  |  |  |  |  | 2 | 6 | 16 | 16 |  |  |  | 40 |
| Gilbert Islands ${ }^{\text {- }}$ |  |  |  |  |  |  |  |  | 2 | 3 | 13 | 14 | 1 |  |  | 33 |
| West Marshall Islands | 2 | 2 | 7 | 1 |  |  |  |  |  |  |  |  | 4 | 2 |  | 18 |
| Bikini Island |  |  | 21 | 6 | 4 | 5 | 4 |  | 1 |  |  |  |  |  |  | 44 |
| East Caroline Islands |  | 1 | 18 | 23 | 18 | 19 | 16 | 6 | 14 | 12 | 21 | 9 | 13 | 1 |  | 171 |
| Central Caroline Island |  | 1 | 6 | 11 | 19 | 21 | 21 | 33 | 27 | 33 | 24 | 13 | 2 |  |  | 211 |
| West Caroline Islands. |  |  |  | 2 | 1 | 1 | 3 |  | 2 | 7 | 1 |  |  |  |  | 17 |
| Philippines (SW. Panay) |  | 1 | 58 | 121 | 62 | 47 | 19 |  | 6 | 15 | 11 | 5 | 2 |  |  | 356 |
| Japan | 1 | 11 | 6 | 6 | 7 | 8 | 6 | 1 |  |  |  |  |  |  |  | 46 |
| Hawaii 2 |  | 16 | 15 | 3 | 2 | 4 | 9 | 15 | 6 | 17 | 29 | 22 | 15 | 32 | 18 | 203 |
| Hawaii ${ }^{\text {8 }}$ - |  |  | 42 | 5 |  | 11 |  |  | 1 |  | 7 | 11 | 1 | 1 |  | 79 |
| Society Islands |  | 2 | 15 | 3 | 2 | 7 3 | 1 |  |  |  |  | 2 | ----- | ----- |  | 13 |
| Northeast Africa |  |  |  | 5 | 12 | 30 |  | 1 |  |  |  |  |  |  |  | 48 |
| Angola, Africa ${ }^{\text {-.- }}$ |  | 1 |  |  | 11 | 11 | 1 |  | 9 | 8 | 9 | 6 | 2 | 2 |  | 60 |
| Total. | 3 | 43 | 537 | 793 | 804 | 435 | 253 | 151 | 167 | 181 | 261 | 243 | 168 | 91 | 20 | 4,180 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

iris. But another measurement was added-the distance from insertion of the ventral fins to the anterior edge of the vent.

This reduction was undertaken without conclusive evidence that the omitted characters were less satisfactory than those retained; but some reduction was clearly necessary in order to have a manageable number of characters, and we think that the selection was good. The characters retained are, in general, external measurements that differentiate several species of tuna closely related to the yellowfin. Of special importance are length of the pectoral fin, length of the anal and second dorsal fins, and the general body proportions, which are reflected by length of the head and distance to the insertions of several fins. It is reasonable to assume that if these characters have differentiated during evolution of these other tuna species, they may well be differentiating in the evolution of the yellowfin group.

Some characters were excluded because they were troublesome to measure or count. For example, the counting of dorsal and anal finlets is complicated occasionally by the apparent absence of a finlet in the midst of the series. Sometimes it is obvious that a finlet has been torn off, at other times it is uncertain whether there had been
a finlet in the space. The diameter of the iris has been omitted because of confusion among our workers between measuring the diameter of the iris and that of the eye. When plotted, these measurements seemed to fall into two groups and we found that measurements had been taken in different ways. We also have not used the gill raker counts, even though we obtained considerable numbers of them, because of uncertainty that our numerous field people were counting gill rakers in the same way. The difficulty is that gill rakers become progressively smaller on one side of the gill arch until covered by skin and, in any gross examination such as must be made in the field, it is always necessary to decide whether certain gill rakers are big enough to be counted. In addition, the number of gill rakers is not entirely independent of length of the fish. In one long series of counts made with grent care in the laboratory on yellowfin from a single area, we found a statistically significant association between number of gill rakers and length of the fish.

Thus, the selection of characters has obviously been haphazard and I cannot claim to have selected the best ones. I can say only that they are the principal external characters which have served to differentiate the species of tunas and they
[Size groups: $\mathrm{S} .<\mathbf{8 0} \mathrm{cm} ., \mathrm{M}, 80-120 \mathrm{~cm}$., and L. $>120 \mathrm{~cm}$.]

${ }^{1}$ A few specimens lacked record of gear used. ${ }^{2}$ Statistics based on curvilinear regressions, Godsil (1948). Additional information from correspondence. ${ }^{2}$ Schaefer (1952). 4 More than half of samples measured by one person. Godsil and Greenhood (1951). © Schaefer and Walford (1950).
appear to be the most variable ones within the yellowfin group that can be measured with presision and consistency by different pcople.

## METHODS OF MEASUREMENT

Our methods of measuring tuna follow the specifications given by Marr and Schaefer (1949). I think we have measured the fish exactly as they intended, but we slightly modified their definitions to overcome some confusion existing among our measurers. The most recent instructions given POFI workers have been as follows:

The measurements described are all made in millimeters with calipers or dividers, depending on the size of the fish and the distance to be measured. All distances are straight lines. The tip of the fixed arm of the calipers (or one point of the dividers) is applied to the first point mentioned and the tip of the sliding arm of the calipers (or the other point of the dividers) is applied to the second point mentioned. Where a choice of sides is involved, all measurements and counts are made on the left side of the fish. Fin insertions are to
be determined while holding the fin approximately perpendicular to the contour of the fish.

Fork length.-(Total length of Marr, Schaefer, and Godsil.) The distance from the tip of the snout (most anterior point on upper jaw), with jaws closed, to the cartilaginous median part of the caudal fork (seating the sliding arm of the caliper firmly and thus depressing the small fleshy flap extending posteriorly).

Head length.-Distance from the tip of the snout to the most posterior point on the margin of the subopercle (depressing the fleshy flap extending posteriorly).

Snout to insertion of first dorsal fin.-The distance from the tip of the snout to the insertion of the first dorsal. The insertion of the first dorsal is the intersection of the anterior margin of the first dorsal spine, when the fin is held erect, with the contour of the back. This point is identical with the most anterior point of the first dorsal fin slot.

Shout to insertion of second dorsal fin.-The distance from the tip of the snout to insertion of the second dorsal. The insertion of the second dorsal is not so clearly defined as the insertion of the first dorsal, particularly on larger fish; but it is the intersection of the anterior margin of the second dorsal with the contour of the back when the fin is held erect. When the second dorsal is raised, the determined point should be marked with thumbnail or scalpel.

Snout to insertion of anal fin.-The distance from the tip of the snout to the insertion of the anal fin. The insertion of the anal fin is determined in the same manner as the insertion of the second dorsal.

Snout to insertion of ventral fin.-The distance from the tip of the snout to the insertion of the ventral. The insertion of the ventral is the intersection of the anterior margin of the ventral, when the fin is extended, with the contour of the body.

Insertion of ventral fins to anterior edge of vent.The midline distance from the insertion of the ventrals to the anterior edge of the vent.

Greatest body depth. - The greatest distance between the dorsal and ventral contours perpendicular to the axis of the fish. The measurement is taken from the dorsal body contour to the ventral body contour, with the first dorsal fin depressed in its slot. It is oriented by reference
to the dorsal spine, the insertion of which is at or nearest to the upper end of the vertical. Dorsal spines are counted posteriorly, the most anterior spine being the first.

Length of pectoral fin.-The distance from the anterior end of the fin slot to the most posterior point, taken with the pectoral fin extended posteriorly and opposed to the side.

Height (length) of second dorsal fin.-The distance from the insertion of the second dorsal fin to its distal end, with the fin in a normal position. Note that this fin is often extended in a long filament, especially in large Neothunnus, and care should be taken to notice if this extension is frayed.

Height (length) of anal fin.-The distance from the insertion of the anal fin to its distal end, with the fin in a normal position. Remarks under height of second dorsal fin apply here.

Diameter of iris.-The greatest diameter measured to the margin of the yellow iris and the adjoining black tissue. This is generally not a line parallel to the median line of the body.

Number of gill rakers.-The number of anterior rakers on the most anterior gill arch on the left side of the fish (some species also have postiterior rakers on this same arch). The counts of the rakers on the two arms of the arch are kept separate. For example, $10+20=30$ gill rakers with 10 on the upper arm and 20 on the lower. The counts include all rakers that project above the surrounding epithelium. We have encountered no difficulty in assigning rakers near the angle of the arch to one arm or the other.

Sex.-Determined by inspection. Very immature males and females may be difficult to distinguish. Ovaries, which are tubular, may often roll between the fingers, while testes, which are solid, will turn over. The testes of ripening or ripe males are enlarged, solid, white bodies, not round in cross section. The ovaries of ripening or ripe females are enlarged, turgid, pink or yelloworange bodies, round in cross section. Ova may often be distinguishable with the naked eye. The testes of spawned-out males are less turgid, tougher, and pinker than those not spawned, and are difficult or impossible to distinguish from maturing testes in early stages. The ovaries of spawned-out females are hollow, more or less flabby, saclike tubes.

Weight.-Should be determined in pounds on steelyards of proper range. Do not weigh on
steelyard having capacity greater than about three times the weight. Be sure to subtract the weight of any hooks used to hold the fish. Record weight to smallest unit on steelyard. Note if fish is weighed in pieces.

## IMPORTANT

Check steelyards before each cruise. Errors must not exceed 1 percent.

Check calipers each time they are used. Errors must not exceed 1 mm .

In addition to these instructions, diagrams were provided on the back of each field sheet (fig. 3).

All measurements of distances exceeding about 55 mm . have been obtained with sliding calipers. This lower limit occurs because some of our calipers will not measure closer than that and hence the shorter distances have been measured with dividers and millimeter rule. All measurements are the actual distance between two points and not the distance parallel to the midline of the body and between perpendiculars as specified by LeGall (1951) for body measurements of European tunas.

Our calipers have usually been of two sizes, 1 m . and 2 m . They evolved through brass and aluminum to standard wooden meter sticks.
dIAGRAMS SHOWING CERTAIN MCRPHOMETRIC MEASUREMENTS OF TUNA

make all measurements with calipers or dividers while fish is lying on its right side
Figure 3.-Diagrams on the back of the field data sheet showing certain morphometric measurements of tuna.

The 1-m. caliper consisted simply of a fixed jaw and a slider on a standard meter stick. If the meter sticks are selected with care to get straight ones, we find it easy to maintain the accuracy within 1 mm . by checking the caliper prior to each use. (We found this checking equally essential with the metal calipers because of the ease with which they can be bent.) For the $2-\mathrm{m}$. calipers we put two meter sticks end to end in a sheet aluminum channel. The channel was made slightly longer than the two meter sticks to permit a third meter stick with a movable jaw to be inserted when we were measuring large sharks or marlins more than 2 m . long.

Almost all of our measurements were obtained in the field and usually on shipboard. In equatorinl areas on POFI vessels it was customary to measure up to about 10 tuna of all species during the course of a day's fishing. During longline fishing operations, which were usually carried out along a line of stations, this ensured that the sample included tunas from a wide-spread area. On the Japanese mothership expeditions in the Caroline Islands area, POFI observers measured fish on the deck of the mothership a few days after capture by catcher vessels.

The original measurements not obtained on POFI vessels came from a variety of sources. In the Honolulu area most measurements were from specimens received at the fresh fish market. The Japanese specimens were measured by members of the POFI reconnaissance team that visited Japanese markets in 1949. Specimens from the Society Islands were measured from the catch of the vessel Havaiian Tuna when they were landed at the Honolulu market and after they had thawed.

## METHODS OF COMPUTATION

As indicated in the general discussion on the comparison of morphometric data, I have not considered ratios or indexes but have used regression analysis entirely in order to control the effect of size of fish in our comparisons. I have used the regressions for yellowfin tuna proposed by Schaefer (1948), who stated that the original measurements provided a satisfactory straight-line relation with fork length in the case of head length, snout to insertion of first dorsal fin, snout to insertion of second dorsal fin, snout to insertion of anal fin,
and greatest body depth. ${ }^{4}$ For the length of the pectoral fin he used the actual length of the fin with the logarithm of fork length, and for heights of the second dorsal and anal fins he used the logarithm of length of fin with the logarithm of fork length. For the other character, the distance from the insertion of the ventral fins to the anterior edge of the vent, which Schaefer (1948) did not use, no transformation is needed to obtain a reasonably straight line.

After accumulating several thousand sets of measurements for several species of tunas, we found that the labor of analysis was beyond our facilities and we turned to the International Business Machines Corporation for assistance. On most of our material, in which the original field data sheets had one fish per sheet, codes were added for species, locality, $10-\mathrm{cm}$.-length group, month, year, sex, and the examiner. Certain measurements were transformed to logarithms and the code and measurements were punched on cards. It was then possible to square, cross multiply, and tabulate automatically. A complete tabulation of sums, sums of squares, and sums of the products for regression analysis was obtained, arranged according to species, locality, and $10-\mathrm{cm}$.-length group. Subsequently, special tabulations of the material were made as needed.

After the data had been completely tabulated and totaled, scatter diagrams were made for each character on all specimens from each area to permit an immediate judgment of aberrant observations. If any data were obviously aberrant, ${ }^{5}$ they were checked with the original field data, and, if plotted as recorded, they were assumed to be in error and were discarded. The regression line was then computed and plotted along with parallel lines plus and minus three standard deviations from regression. At this time, any remaining points more than three standard deviations from regression were assumed to be in error and were dropped. Then, final regression and the standard deviation from regression were computed. I have not tabulated the number of discarded observations, but I estimate it to be less than 2 percent of the total.

[^3]Discarding any data is questionable because correct but unusual observations may be discarded. By my method, however, most of those dropped were far removed from the line. The rejected values frequently were so located that one suspected that digits had been transposed or errors made in the decimeter digit. I believe that few if any correct observations were discarded. Furthermore, some culling is desirable for all data of this kind which have been collected under difficult field conditions where it is not practical to check original measurements.

Checks were made at all stages of computations. All IBM card punching was verified. All desk calculator operations that could not be independently checked were repeated. Finally, the plots of the regression line and standard deviations from regression provided a visual check which detected any but trivial errors.

## SELEGTION OF REGRESSION EQUATIONS

In the analysis of yellowfin tuna morphometrics, two fundamental statistics, mean and variance, are required. Both must be unbiased estimates of corresponding population parameters. These statistics are estimated from the best regression formulae. If I apply straight line regressions to data that are curvilinear, then my estimates of the means may diverge an unknown amount from the population parameter and the estimates of variance will tend to be excessive. On the other hand, curvilinear regression techniques tremendously increase already laborious calculations and for practical reasons should be avoided unless fully justified.

The two authors who have dealt with relative growth of the yellowfin tuna are in fundamental disagreement on whether curvilinear regression is needed for several characters. Schaefer (1948: 117) stated, "Over the range of sizes considered, all the characters measured, with the exception of the lengths of the pectoral, second dorsal and anal fins, bear a linear relationship to the length of the fish." For the length of the pectoral fin he used the logarithm of fork length and for the other two fin dimensions he used the logarithm of both fin length and fork length and simply states, without offering proof, that these transformations are appropriate. Schaefer later (1952) cautioned that the relationships were only approximations that did not completely describe the relation between
fork length and size of the body part. On the other hand, Godsil (1948: 7) stated-

Plotting to a large scale the actual measurements of a given character against body length in each case, revealed that the sample regressions were nearly but not quite linear. Of the various functions tried, the expression $Y=a+b x+c \frac{1}{3}$ (where $x=$ body length in each case and $Y=$ the dependent variable) resulted in the best fit.
The other functions tried included $y=a+b x$, $y=a+b x+c x^{2}, \quad y=a+b x+c x^{2}+d x^{3}, \quad y=a x^{b}, \quad$ and $y=a e .^{b x}$ He also stated that the reduction in the sum of the squared deviations from the above expression when compared with the sum from the linear regression was in most cases highly significant. He offered no statistical data supporting this assertion; but his graphs, with the plotted points and curved lines, show clearly that the data for head length and snout to the insertions of first dorsal, ventral, second dorsal, and anal fins are slightly curvilinear and the computed lines fit well. The curvilinearity in Godsil's data is further puzzling because Schaefer and Walford (1950) presented data for characters used by Godsil that show no curvilinearity.

Therefore, it is desirable to examine in greater detail the source of curvilinearity in Godsil's data. This may be done by comparing the meansquare deviations from linear regression with those from curvilinear regression (table 3). When such comparisons are summed for the 13 samples for each character, I find that curved lines significantly reduced the mean square of pooled data as well as the mean square of within-sample data for each character. I notice, however, that for
all characters reduction in the mean square from linear to curvilinear regression is much greater for pooled data than it is for within-sample data. Such differences between pooled and withinsample data suggest than a major part of the curvilinearity is between samples rather than within samples.

More conclusive evidence of the source of curvilinearity is to be found by examining the significance of the reduction in the mean square, character by character and sample by sample (table 3). Here significant or highly significant curvilinearity for most characters occurs in samples $1,3,4,5,6$, and 7 . In the remaining seven samples, 2 and 8 through 13, only four instances of a significant but not highly significant reduction in mean square occur in 35 comparisons. Since two significant reductions would be expected to occur by chance in this number of comparisons, little importance can be attached to the four. Clearly, curvilinearity is associated with certain samples and not with certain characters for all samples, as would be expected from a truly curvilinear regression of body part on fork length.

One characteristic of the samples that might be associated with curvilinearity is size, since it is obvious that very large samples ( $D F=385,348$ ) show curvilinearity whereas small samples ( $D F=$ $25,36,67$ ) do not. Among the eight samples of intermediate size, however, four, with degrees of freedom equaling $192,121,98$, and 96 , show no more than one character with significant curvilin-

Table 3.-Mean-square deviations from linear and curvilinear regressions of yellowfin morphometric measurements
[Measurements from Godsil, 1948]

| Sample number | $\left.\begin{gathered} \text { Degrees } \\ \text { of } \\ \text { freedom } 1 \end{gathered} \right\rvert\,$ | Length of head |  | Snout to insertion of- |  |  |  |  |  |  |  | Date of collection ${ }^{\text {2 }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | First dorsal fin |  | Second dorsal din |  | Anal fin |  | Ventral fin |  |  |
|  |  | Linear | Curvilinear | Linear | Curvilinear | Linear | Curvilinear | Linear | Curvilinear | Linear | Curvilinear |  |
| 1 | 92 | 7.84 | ${ }^{*}$ * 0.69 | 14.53 | ++13. 49 | 20.15 | *19.212 | 20.26 | ${ }^{* *} 17.88$ | 13.07 | *'11. 41 | Mar. 13, 1939. |
| 2 | 96 | 5.71 | 5.68 | 10.06 | 10.21 | 12.83 | 12.45 | 19.59 | ${ }^{+18.47}$ | 11.89 | 11.79 | Mar. 8, 1939. |
| 3 | 106 | 10.80 | *11. 58 | 12. 40 | 12. 10 | 21.17 | **19.29 | 26. 43 | *26. 44 | 16.87 | 17.10 | Aprr. 25, 27, 1040. |
| 4 | 385 | 11.06 | ${ }^{*}+10.34$ | 20.98 | **19.70 | 32. 46 | + +29.91 | 99. 40 | 30.63 | $\stackrel{25.07}{ }$ | ${ }^{* * * 24.70}$ | Nov. 5 to Dec. 7, 1936. |
| 5 | 348 118 | 11.08 | +*8.91 | 18.97 10.66 | +*15. 72 | 20.95 | + ${ }_{+15 .} 13918$ | 29.63 | **19.70 | 20.06 12.86 | **19. 07 | Jan. 14 to Feb. 13, 1937. Mar. $26,1939$. |
| 7. | 141 | 18. 40 | ${ }^{* * 14.19}$ | $\underline{25.57}$ | **2922 | 38.00 | * 32.30 | 134. 09 | **30. 69 | 31. 75 | +48.29 | Jan. 16 to $19,1937$. |
| 8 | 192 | 7.73 | 8.37 | 12. 01 | 12.49 | 11. 62 | 12.55 | 16. 56 | 16.85 | 14. 07 | 15. 71 | apr. 1 to 19, 1940. |
| 9 | 6i7 | 6.37 | 6. 29 | 4.84 | 14.55 | 12.81 | 13. 06 | 16. 07 | 16.15 | 8.42 | 8.58 | May 12, 1940. |
| 10 | 121 | 5.45 | *5. 20 | 9.91 | 10.30 | 11.19 | 11. 03 | 15. 74 | 16. 43 | 13. 79 | 14.16 | Jan. 21 to Feb. 10, 1937. |
| 11 | 36 | 7.81 | 7.83 | 9.94 | '8. 83 | 22.92 | 21.03 | 13.97 | 14. 17 | 18. 63 | 19.32 | Mar. 22 to 24, 1940. |
| 12 | 25 | 6.92 | 7.21 | 7.84 | 8.17 | 15.16 | 15. 75 | 23. 60 | 24. 54 | $\stackrel{1}{21.12}$ | 21.96 | Apr. 29, 1940. |
| 13 | 98 | 8.28 | 8.32 | 14. 99 | 15.11 | 13.04 | *12.64 | 16. 72 | 16.84 | 14.27 | 14.25 | Mar. 30, 31, 1940. |
| Pooled-sample variance_ | 1909 | 12.07 | ${ }^{* *} 9.53$ | 19. 07 | ${ }^{* * 15.78}$ | 24. 83 | **20. 40 | 27.25 | ${ }^{* * 25.85}$ | 19.91 | * ${ }^{19} 19.31$ |  |
| Withiu-sample variance. | 1585 | 9.71 | **8. 80 | 16.14 | ${ }^{* *} 14.94$ | $\underline{21.69}$ | ${ }^{* 19.24}$ | 22.65 | **21.99 | 18. 73 | *+18. 34 |  |
| 1 Varies slightly with different eharacters. $\quad{ }^{2}$ Supplied by Godsil in personal communication. $\quad$ Statistically significant reduction in mean square ( $0.05>p>0.01$ ). **Iighly signifcant reduction in mean square ( $p<0.01$ ). |  |  |  |  |  |  |  |  |  |  |  |  |

earity. The other four samples of intermediate size show highly significant curvilinearity in at least one character and significant curvilinearity in more than half of the characters. It is likely that something other than sample size alone has caused curvilinearity.

Another source of curvilinearity may be accidents of sampling. Such accidents appear to be rather likely because most of Godsil's samples (table 2) were obtained on a single day or over a period of a few days. It is well-known that yellowfin school by size, and when one of the larger samples includes a considerable range in sizes it is probable that it was obtained from only a few schools of different average size. If the sample included schools of slightly different morphological characteristics and also of different mean size, there would be two sources of regression-one within schools fished and the other between schools fished. The combined regressions might appear to be curvilinear.

Therefore, when I examined our data for curvilinear regression I turned first to the sample that I considered had the best coverage of the area sampled and that contained a good size distribution of fish. It was the sample from the western Line Islands area, obtained during 13 different months with the majority of the fish caught by longlining and trolling and measured by 12 different measurers. During both longlining and trolling operations, it was customary to measure only a few fish a day (rarely more than 10), and thus these fish came from several dozen different schools and as many different locations within the area. There are 188 sets of measurements available in this sample, with good numbers in most $10-\mathrm{cm}$. length groups from 50 to 160 cm .

Evidence of curvilinearity was sought in the plots of complete data that were made to check each sample. Some evidence of curvilinearity appeared in the plots for certain characters, but the scatter of points around the line made interpretation difficult. Hence, I sought a way to magnify any curvilinearity and plotted the deviations of the $10-\mathrm{cm}$. group means from the rectilinear regression equations for each character in the sample (fig. 4). These equations were based on the transformations, proposed by Schaefer (1952), which are log fork length and log height of second dorsal fin, log fork length and log height of anal fin, and $\log$ fork length and length of pectoral fin.


Figure 4.-Sample of yellowfin tuna from western Line Islands area. Deviations of $10-\mathrm{cm}$. group means from regressions were used. (X, average of less than 10 fish; 0 , average of 10 or more fish.)

The data for all other characters were not transformed.

The graph suggests that some curvilinearity occurs in several characters. If a random distribution of $10-\mathrm{cm}$.-group means about the regression line is assumed, a line connecting the group means would be expected to cross the regression line an average of five times (with 11 points). To the contrary, for four characters-
length of pectoral, height of second dorsal fin, height of anal fin, and snout to insertion of first dorsal fin-the lines crossed only twice. In the case of only one character-the snout to insertion of second dorsal fin-did the lines cross more than the most probable number of times.

The question then arose whether the curvilinearity prevailed in other samples, and I made a similar analysis of our other two large samples


Figure 5.-Sample of yellowfin tuma from central Caroline Islands area. Deviations of $10-\mathrm{cm}$.-group means from regression. ( $X$, average of less than 10 fish; 0 , average of ' 10 or more fish.)


Figure 6.-Sample of yellowfin tuna from eastern Caroline Islands area. Deviations of $10-\mathrm{cm}$.-group means from regression. ( X , average of less than 10 fish; 0 , average of 10 or more fish.)
that also are well distributed over a wide range of lengths. They were the samples from the eastern Caroline Islands and the central Caroline Islands, which contained 171 and 211 sets of measurements, respectively. Similar plots of deviations of $10-\mathrm{cm}$.-group means from the rectilinear regression lines (figs. 5 and 6) indicated
again that the lines cross less than the expected number of times for most characters.

When compared, the deviations from regressions of all three areas indicate that they tend to form a curve concave upwards for height of second dorsal fin, height of anal fin, and greatest body depth. Other characters, especially head Iength, snout to insertion of first dorsal fin, and snout to insertion of ventral fin, appear sinuous with some tendency for the line connecting means to start below the regression, then go above, then below, and then upward again. The line appears to be curved for length of the pectoral fin, but in a different way in each sample.

I conclude that for most characters in these large samples some curvilinearity remains that is not associated with sampling, but is rather an expression of the allometric growth of the fish. Furthermore, it is an irregular allometry which is not readily expressed by any linear or simple curvilinear formulation.

Such curvilinearity would not be troublesome if all samples had similarly distributed lengths, in which case it would probably be satisfactory to use the regression techniques proposed by Schaefer (1948). The rather small amount of curvilinearity would result in some bias in mean, variance, and regression constants, but if such bias were similar among samples it would not matter. However, it has not been possible to obtain samples covering a uniform range of lengths. In numerous areas, particularly along the Pacific Equator, where we have fished only with longline gear, we have obtained only very large fish, and in other areas, where fishing has been done only by trolling, we took mostly small fish.

The compromise solution has been to split the samples into three size groups and compare them at three different standard lengths, each very close to the grand mean of its size group. The following groups have been used:

Small (S)—fish less than 80 cm ., most of which are more than 50 cm . and which have been compared at a length of 65 cm . (about 12 lb .); medium (M)-fish from 80 to 120 cm ., compared at a length of 100 cm . (about 43 lb .); large (L)-fish more than 120 cm ., most of which are less than 170 cm . and which have been compared at a length of 140 cm . (about 118 lb .).

Further restrictions were adopted: first, to avoid uncertainties due to the small samples it was
required that there be more than 20 specimens in each size group, and second, to minimize the effect of any curvilinearity remaining within a size group, it was required that more than 10 percent of the sample be above and more than 10 percent below the comparison size. For example, in Godsil's sample from Panama and Costa Rica there were 23 fish between 120 and 140 cm . and none above 140 cm . This part of his sample was not considered in the large group, whereas his sample from Cocos Island including 23 fish ranging from 120 to 160 cm ., with 9 above 140 cm ., was considered. One sample remains that is not well distributed in fork length-the one from northeast Africa. It has been used, but the comparisons are made with reservations.


Figure 7A.-Regressions of head length, distances from snout to insertions of first dorsal and ventral fins, and greatest body depth in yellowfin tuna from central Caroline Islands area.

The fit of the lines to the three size groups may be judged from the plots of the data from the central Carolines area (figs. $7 \mathrm{~A}, 7 \mathrm{~B}$, and 7 C ). Each of the three separate lines appears to be a


Figure 7B.-Regressions of distances from snout to insertion of second dorsal and anal fins and distance from insertion of ventral fin to anterior edge of vent, in yellowfin tuna from central Caroline Islands area.
good fit in its limited range, but when projected beyond the range it may rapidly diverge from the plotted points. The tendency that has been noted toward a sinuous line in certain characters is again evidenced in the plots and in the changing regression constants. I judge, however, that any remaining curvilinearity within each size group is much less than the dispersion of points about the line and that samples within each size group may be compared with little fear of erratic results due to curvilinear regression.

## RELIABILITY OF SAMPLE STATISTICS

In addition to determining methods of regression analysis that will give reliable estimates of mean and variance the reliability of the raw data must be assessed. Two matters may be


Figure 7C.-Regressions of .log heights of second dorsal and anal fins and length of pectoral fin, in yellowfin tuna from central Caroline Islands area.
examined: first, the adequacy of the sampling, and second, the accuracy of the measurements.

An ideal sample of yellowfin tuna for a morphometric study would be representative of all sizes of tuna in the specified area during the period of study. Such a sample would contain a distribution of sizes proportionate to the numbers of each size in the ocean and would be randomized over the time and area covered. This ideal is far out of reach because it is not possible to catch all of the sizes, as each fishing gear selects certain size groups, and it has not been possible to fish any area at randomly selected locations or times.

Consideration of the habits of the yellowfin suggests, however, that satisfactory samples may be obtained from a relatively limited coverage.

The yellowfin is a schooling species (Murphy and Elliott, 1954), and I have suggested that schools in a limited area may vary slightly in their morphometric characteristics (p. 406). The yellowfin are fast swimmers, however, and it seems probable that they could cover hundreds of miles in a few days. Furthermore, the larger yellowfin at least are entirely independent of coastal regions. The ocean in which they are found is relatively uniform, with no absolute barriers to migration, although the yellowfin do prefer certain areas, presumably where they find the most food. So it is possible that a sample made up of subsamples from numerous, different schools may be adequately representative of an area even though the area is not randomly covered. The schools may be assumed to have been randomly swimming in the area. A similar assumption with regard to time is less safe because many species migrate annually, and even if yellowfin are present in an area throughout the year, they might be different spawning groups.

Even though the ideal sample cannot be obtained, samples with widely varying coverage in area and time (table 2) may be compared. As the samples were extended in space and time, however, they were taken by an increasing number of people, who may have varied in their techniques of measurement. Therefore, the problems of sampling and precision in measuring the fish must be considered simultaneously, and here I digress briefly to consider the problem of obtaining consistent measurements of yellowfin.

Fortunately, all tunas are easy to measure consistently. The body is stiff, and even when not in rigor mortis has almost no tendency to bend when the fish is laid on a flat deck on its side. The parts to be measured were accurately defined by Marr and Schaefer (1949). The numerous measurers from POFI have compared their methods-almost no one measured tuna without first working with someone who had measured them before-and most differing interpretations of the definitions have been quickly settled. Nevertheless, I consider that minor differences of technique must have occurred both among POFI and other measurers, and the problem is to assess how great the differences have been.

One approach to this problem might be to have different people repeat measurements on the same fish and then analyze the differences. We
have made repeat measurements to standardize our methods but have not analyzed the differences, because our concern is with what people have done independently and routinely and not what they could do under experimental conditions.

It will not be possible to separate the differences in technique from differences of time and area, but the combined problem can be approached by examining the variance in relation to coverage of the sample and number of measurers. Also mean values and overlap of closely related samples obtained by different measurers can be compared. The latter comparison must be left until I have introduced the method of comparing means and overlap.

The variance itself is not suitable for our comparison. Better is the standard deviation from regression $S_{y . x}$, which is directly indicative of the spread of points about the line, but it obviously is related to the size of the character, even when the characters have been transformed to logarithms. So I have used a kind of coefficient of variation,

$$
C=\frac{100 S_{y . x}}{\bar{x}}
$$

to eliminate the effect of size of character $\bar{x}$ and so obtain a better mean value for all characters in a sample.

These coefficients of variation have been computed for each character in each sample and are shown in table 4 (except the samples of Godsil (1948) from Panama and Costa Rica and from Cocos Island, in which his curvilinear regressions were used and in which the range spreads extensively over two or more of our size groups).

Several samples contained measurements for only five characters, and hence the sample means and the grand means were computed from these five characters only.

This table shows close agreement among grand means of the cocfficients of size groups for the five characters, which indicates that the standard deviation from regression is almost exactly related to size of the fish. Further, there is some difference among characters: length of pectoral fin and greatest body depth have a high coefficient; log heights of second dorsal and anal fins show coefficients that increase with size of fish; distances from snout to insertion of second dorsal and aual fins have the lowest values.

Table 4.-Coefficients of variation of yellowfin morphometrics

| Area and size 1 | Length of head | $\begin{aligned} & \text { Length } \\ & \text { of } \\ & \text { pectoral } \\ & \text { fin } \end{aligned}$ | Weight of second dorsal fin | Weight of anal fin | Snout to insertion of- |  |  |  | Greatest body depth <br> (9) | Insertion ventral to anterior edge vent <br> (10) | Means ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | First dorsal fin | Sccond dorsal fin | $\begin{aligned} & \text { Anal } \\ & \text { fin } \end{aligned}$ | $\underset{\text { Ventral }}{\text { Vin }}$ |  |  |  |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) |  |  |  |
| Mexico: ${ }^{3} \mathrm{~S}$.- | 1.38 |  |  |  | 1. 70 | 1.05 | 1.04 | 1.60 |  |  | 1.35 |
| Guatemala: ${ }^{\text {S }}$ S | 1.32 |  |  |  | 1.64 | 1.06 | . 96 | 1.76 |  |  | 1.35 |
| Costa Rica: 4 M | 1.75 | 3.13 | 1.67 | 1.85 | 1. 76 | 1.38 | . 95 | 171 | 3.14 | ---- | 1.46 |
| Galapagos Island: ${ }^{8} \mathrm{~S}$ | 1. 42 |  |  |  | 1.61 | . 92 | . 99 | 1.71 |  |  | 1. 33 |
| Clipperton Island: ${ }^{3} \mathrm{~S}$ | 1.33 |  |  |  | 1.36 | 1. 18 | . 85 | 1.83 |  |  | 1. 31 |
| ${ }_{109} 109^{\circ}-119^{\circ}$ W.: ${ }^{\circ} \mathrm{L}$ | 1. 24 | 3. 58 4.68 | 1.32 2.58 | 2. 55 | 3. 03 2. 01 | 1.44 1.18 1.38 | 1.10 <br> 1.38 <br> 1 | 2.35 2.90 | 2. 198 | 2. 288 | 1.97 1.93 |
| $129^{\circ}-139^{\circ} \mathrm{W} .:$ L | 1. 16 | 4.17 | 2. 66 | 2.58 | 2.07 | 1.33 | 1.24 | 2.04 | 4. 09 | 2. 61 | 1. 73 |
| $139^{\circ}-149^{\circ} \mathrm{W} .:$ L | 1.81 | 3.50 | 2. 47 | 2.60 | 2.23 | 1. 28 | 1.33 | 2. 14 | 2.96 | 2. 72 | 1. 76 |
| Fast Line Islands: M | 1. 57 | 3.03 | 2.50 | 2.34 | 2.02 | 1.34 | 1.63 | 1. 84 | 3. 24 | 2. 27 | 1. 68 |
| L | 1.82 | 4.05 | 2. 57 | 2.71 | 2.44 | 1. 62 | 1.33 | 2. 55 | 2. 51 | 2.54 | 1. 95 |
| West Line Islands: |  |  |  |  |  |  |  |  |  |  |  |
| S | 2.28 | 3.77 | 1.56 | 1. 55 | 2.63 | 1.34 | 1.63 | 2. 53 | 3.43 4 4 | 2. 65 | 2. 08 |
| M | 2. 16 1.96 | 4.40 2.88 | 1.8 2.15 2.44 | 2. 2.24 | 2. 27 1.76 | 1.48 1.29 | 1. 1.11 | 3.70 1.94 | 4. 19 3.19 | 2. 23 | 2. 1.61 |
| Palmyra Island: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |  |  |  |
| S.---------- | 2.02 |  |  |  | 2. 64 | 1.38 | 1.24 | 1. 58 |  |  | 1. 77 |
| M--7sionds: | 1.57 |  |  |  | 1.86 | 1. 36 | 1.59 | 1. 72 |  |  | 1. 62 |
| Phoenix Islands: | 2.33 | 4.09 | 1.63 | 1.80 | 1.85 | 2.20 | 1.50 | 2.53 | 2. 59 | 2.15 | 2. 08 |
| M | 2.30 | 4. 45 | 2.02 | 2. 59 | 2. 00 | 2.49 | 1. 70 | 2.57 | 4. 10 | 1. 98 | 2. 21 |
| L. | 1.93 | 3.22 | 2. 22 | 1.97 | 2.09 | 1. 37 | 1.32 | 2.80 | 3.73 | 2. 53 | 1. 90 |
| East Marshall Islands: L | 1. 45 | 3.78 | 2.08 | 1.97 | 1. 41 | 1.03 | 1. 04 | I. 58 | 2. 54 | 2.57 | 1. 30 |
| Bikini Island: S | 1.51 | 3.30 | 1.28 | 1.58 | 1.78 | . 84 | 1. 10 | 2. 41 | 2.18 |  | 1. 53 |
| East Caroline Islands: |  |  |  |  |  |  |  |  |  |  |  |
| $\stackrel{\mathrm{S}}{\mathbf{M}}$ | 1. 34 | 4.04 3.79 | 1.25 1.34 | 1.49 1.49 | 2. 04 1.65 2.68 | 1.21 .93 | 1.19 .87 | 1.75 1.78 | 2. 83 <br> 2. 68 <br> 8 | 2. 50 | 1. 51 |
| L | 1. 60 | 3.27 | 1.98 | 1.66 | 2.22 | 1. 10 | 1.11 | 1.90 | 3.23 | 2.04 | 1.59 |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |  |  |  |
| M | 1.64 1.31 | 3.01 3.91 | .90 1.52 | 1.50 1.56 | 1.61 | 1.37 1.41 | 1.74 1.52 | 3. 2. 48 | 3.32 <br> 2.93 | $\begin{array}{r}2.93 \\ 2.51 \\ \hline\end{array}$ | 1.90 1.75 |
| L. | 1. 97 | 3.63 | 2. 46 | 2.07 | 2.23 | 1. 48 | 1. 52 | 3. 13 | 3.72 | 3. 13 | 2.07 |
| Phillppines: |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{S}_{\mathbf{M}}$ | 2.14 2.37 | ------ |  |  | 2.82 2.31 | 2.49 1.62 | 2.02 1.55 | 2. 50 |  |  | 2.39 2.03 |
| L. | 2.74 |  |  |  | 3.11 | 1.87 | 2.25 | 3.62 |  |  | 2. 72 |
| Japan: s | 1.78 | 3.65 | 1.32 | 1. 49 | 2.01 | 1.34 | 1.11 | 2.16 | 2.91 |  | 1. 68 |
| Hawail: | 1.77 | 4.87 | 1.75 | 1.79 | 2.17 | 1.51 | 1.56 | 2.77 | 3.70 |  | 1.96 |
| M | 2.19 | 5. 04 | 1.95 | 2. 55 | 2.65 | 1.37 | 1. 49 | 2.72 | 3.42 |  | 2.08 |
| L. | 1. 74 | 3.84 | 2. 20 | 2.13 | 2.01 | 1.41 | 1. 26 | 2.04 | 3.36 |  | 1. 69 |
| Hawnii: ${ }^{\text {s }}$ |  |  |  |  |  |  |  |  |  |  |  |
| S | 1.52 |  |  |  | 1. 70 | 1.01 | 1.05 | 1.98 |  |  | 1. 45 |
| L | 1.32 |  |  |  | 2.03 | 1. 20 | 1.05 | 1.51 |  |  | 1. 42 |
| Society Islands: S. | 1. 49 | 4. 12 | 1. 60 | 1.97 | 2. 42 | 1.43 |  |  |  |  | 1.78 |
| Northeast A frica: $\$$ | 2.19 | 3.90 | 1.53 | 2.08 | 2.92 | 1. 93 | 1.87 | 2.98 | 2. 52 |  | 2.38 |
| Angola, A frica: ${ }^{6}$ | 1.88 | 3.98 | 1.33 | 1.47 | 2.29 | 1.39 | 1.46 | 1.62 |  |  | 1. 73 |
|  | 1.90 | 3. 58 | 1. 86 | 2.36 | 2. 24 | 1. 19 | 1.46 | 1. 72 |  |  | 1.70 |
| Means: |  |  |  |  |  |  |  |  |  |  |  |
| S | 1.72 | 3. 86 | 1. 42 | 1. 69 | 2.06 | 1.39 | 1. 32 | 2. 22 | 2.94 | 2. 56 | 1. 74 |
| $\mathrm{M}_{\mathbf{L}}$ | 1.84 1.88 | 3. 97 3.68 | 1. 82 | 2. 09 2.28 | $\begin{array}{r}\text { '2. } \\ \mathbf{2} 21 \\ \hline\end{array}$ | 1.48 1.34 | 1.43 1.32 | 2.19 | 3. 39 3.28 | 2. 26 | 1. 81 |
|  |  |  |  |  |  |  |  |  | 3.20 |  | 1.81 |

${ }^{1} \mathrm{~S}$, fish less than 80 cm ., and compared at a length of 65 cm .; M , fish from 80 to 120 cm ., and compared at a length of 100 cm .; L , fish more than 120 cm. , and compared at a length of 140 cm
${ }^{2}$ Mean of columns (1), (5), (8), (7), and (8). $\quad 3$ Godsil (1948) and in correspondence. $\quad 4$ Schaefer (1952). $\quad$ Godsil and Greenhood (1951). 6 Schaefer and Walford (1950).

Of most interest, however, is the rather small amount of variation in the mean $C$ values for the different samples. These values range from a low of 1.30 , equal in the eastern Marshalls group L and the eastern Carolines group M, to a high of 2.72 in the Philippines group L. The Philippines group $S$ and the northeast Africa group $S$ are next highest. (I have no information on how these samples were collected and the factors that may have caused the higher values.) Among the POFI samples the highest (2.21) value is found in the Phoenix Islands group M.

When I tried to relate the mean $C$ to the number of measurers and to the coverage of the sample in
figure 8, I found little relation. The grand mean for one to three examiners is 1.62 ; for four to six examiners, 1.88 ; and seven or more, 1.92. The relation to length of sampling period is similar: for 1 to 9 days the mean is 1.64 ; for 10 to 19 days, 1.91; and for 20 or more days, 1.80 .

None of this evidence is conclusive, but there appears to be a slight increase in the value of $C$, which is associated with increased time, greater number of measurers, or greater area sampled. I cannot segregate these factors, but because curvilinearity appears in some of Godsil's (1948) samples which were collected during only a few days, the samples taken on fewer than 10 different


Figure 8.-Relation of the mean coefficient of variation of five selected characters to number of examiners and number of days on which parts of the sample were taken.
days may be less representative. Therefore, I conclude that important bias was not introduced by different techniques among measurers, at least not in the centrad and eastern Pacific area, where all of the measurers worked closely with one another.

## CHARAGTER-BY-CHARACTER COMPARISON OF SAMPLES

One of the most direct and useful ways of comparing morphological data is simply to compare the mean values estimated for certain fixed lengths. These values are particularly useful because they may be associated readily with geographic features and show directly the presence of character gradients or clines. Unlike tests of significance or amounts of overlap, an examination of the means shows directly the differences in number of parts or in body form. Of course, with all characters associated with body size it is necessary to control body size by the use of appropriate regressions.

A first comparison of samples is logically among the considerable series available from the equatorial Pacific. Areas from which these samples came extend from the American coast westward about 8,400 miles to the central Carolines area, which is bounded on the west by longitude $140^{\circ}$ E. (fig. 2). This area of comparison is limited to the region between latitude $10^{\circ} \mathrm{N}$. and latitude $10^{\circ} \mathrm{S}$., although some of the samples are more
restricted than this in latitudinal coverage. In the southern and extreme northern parts of this zone are the westerly flowing South Equatorial and North Equatorial Currents. Between these two currents ( $5^{\circ} \mathrm{N}$. to $10^{\circ} \mathrm{N}$.) is the easterly flowing Countercurrent. Throughout this area ${ }^{6}$ yellowfin tuna have been taken near the Equator and have been found to be especially abundant between the Equator and the Countercurrent. They also have been found to be rather consistently scarce north of the Countercurrent and south of the Equator. They do, however, occur well to the north and south of this equatorial region, and no known barriers to their horizontal migration exist in any direction until water too cold for their liking is reached in the vicinity of latitude $40^{\circ}$ N. or S .

So we know that the distribution of yellowfin is continuous from east to west in this equatorial band and that the tuna prefer a band about 300 miles wide in a north-south direction. Here is a situation where character gradients may be expected if the tuna are not freely intermingling across the whole equatorial Pacific.

In order to seek gradients I have adopted a slightly modified form of the method proposed by Hubbs and Hubbs (1953). Theirs is a graphical method in which the mean is plotted, a measure of dispersion is indicated by one standard deviation plotted on either side of the mean as a hollow bar, and a measure of reliability is indicated by two standard errors of the mean plotted as a solid bar on either side of the mean. The range is indicated by a base line. I have used comparable regression statistics, except for the range. First, the mean part size $\hat{Y}$ was calculated directly from the regression equation

$$
\hat{\Gamma}=a+b X
$$

Second, the dispersion around the regression line is indicated by one standard deviation from regression

$$
S_{y \cdot x}=\sqrt{\frac{\Sigma y^{2}-(\Sigma x y)^{2} / \Sigma x^{2}}{n-2}}
$$

plotted as a hollow bar on either side of the mean. The reliability of the mean is indicated by two

[^4]standard errors of the mean estimated from regression
$$
2 S_{\hat{y} \cdot x}=2 S_{y, x} \sqrt{1 / n+x^{2} / \Sigma x^{2}}
$$
plotted as a solid bar on either side of the mean.
These statistics were computed separately for each size group in each sample. For the small (S) group they were computed at a fork length of 65 cm ., for the medium (M) group at 100 cm ., and for the large ( $L$ ) group at 140 cm . The three size groups are shown separately for all samples in figures 9 to 18. In each graph the equatorial Pacific samples are arranged in order from east to west and the other samples are added at the bottom.


Figure 9.-Head length of small ( 65 cm .), medium ( 100 cm. ), and large ( 140 cm .) yellowfin tuna, as estimated from regression statisties. (The center line indicates the mean, solid bar $\pm$ two standard errors of the mean, hollow bar $\pm$ one standard deviation from regression.)

Almost all of the characters show gradientssometimes stepped, sometimes continuous, and sometimes confused, perhaps because differences are small and sampling variation has its effect. The gradients, however, in most cases are unmistakable.

There is a distinct tendency toward shorter heads (fig. 9) in all three size groups from the western Pacific. The gradient is not smooth,
because fish of the large group from longitude $109^{\circ} \mathrm{W}$. to the western Line Islands area have much the same size head, and head size in the samples from the medium and small groups is much the same near the ends of the range.

The length of the pectoral fin (fig. 10) is distinctly greater in fish from the Caroline Islands area than in those from the eastern Pacific. Again similar tendencies occur in all size groups except


Figure 10.-Length of pectoral fin of small ( 65 cm .), medium ( 100 cm .), and large ( 140 cm .) yellowfin tuna, as estimated from regression statistics. (The center line indicates the mean, solid bar $\pm$ two standard errors of the mean, hollow bar $\pm$ one standard deviation from regression.)


Figure 11.-Height of second dorsal fin of small ( 65 cm .). medium ( 100 cm ), and large ( 140 cm. ) yellowfin tuna: as estimated from regression statistics. (The centel line indicates the mean, the solid bar $\pm$ one standard deviation from regression.)

## YELLOWFIN TUNA



Figure 12.-Height of anal fin of small ( 65 cm .), medium ( 100 cm .), and large ( 140 cm .) yellowfin tuna, as estimated from regression statistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)


Figure 13.-Distance from snout to insertion of first dorsal fin of small ( 65 cm .), medium ( 100 cm .), and large ( 140 cm .) yellowfin tuna, as estimated from regression statistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)
that both the small and medium groups suggest a rather smooth cline, whereas the large group shows a rather similar fin length from longitude $139^{\circ} \mathrm{W}$. to the Caroline Islands.

The differences in the height of the anal fin (fig. 12) and the height of the second dorsal fin (fig. 11) are even more marked, with clear and almost uniform gradients from the vicinity of Costa Rica to the eastern Marshalls and then about the same length fins on through the Caroline Islands area. Here the difference among samples of the large size group is about 16 cm . for height of second dorsal fin and 20 cm . for height of anal fin from longitude $109^{\circ} \mathrm{W}$. to the Caroline Islands.

The distance between the snout and the insertion of the first dorsal fin (fig. 13) shows a distinct but somewhat irregular trend in the opposite direction, with the fish in the eastern Pacific having the greater measurement between these two points. In all size groups, insofar as samples are available, clearer trends in the same direction are to be noted in the measurements between the snout and the insertion of the second


Figure 14.-Distance from snout to insertion of second dorsal fin of small ( 65 cm .), medium ( 100 cm .), and large ( 140 cm .) yellowfin tuma, as estimated from regression statistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)


Figure 15.-Distance from snout to insertion of anal fin of small ( 65 cm .), medium ( 100 cm .), and large ( 140 cm.) yellowfin tuna, as estimated from regression stittistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)
dorsal fin (fig. 14) and between the snout and the insertion of the anal fin. In the large fish the trend is especially clearcut for the snout to insertion of anal fin (fig. 15). The snout to insertion of ventral fins (fig. 16) shows a somewhat similar tendency, but again the differences are smaller and sampling variation causes some confusion. The remaining characters, distance from the insertion of the ventral fins to the anterior edge of the vent (fig. 17) and greatest body depth (fig. 18), present a more confused picture. In the medium-sized fish there is a tendency for the fish from the eastern Pacific to have a greater body depth, but this tendency is not so noticeable among the larger specimens. The distance from the ventral insertion to the anterior edge of the vent divides the samples into two groups. The distance is about 40 cm . in the large size group among all samples from between longitudes $109^{\circ}$ W. and $149^{\circ} \mathrm{W}$. and about 39 cm . in the samples from the eastern Line Islands to the central Caroline Islands area.

Clearly, then, a more or less steady cline from the eastern to the west-central Pacific exists,
with the average yellowfin in the eastern Pacific having the larger head, shorter pectoral, second dorsal, and anal fins, and greater distances from the snout to the insertions of first dorsal and ventral fins. It also has considerably the greater distances from the snout to the insertion of the second dorsal and anal fins, a greater body depth, and greater length from the ventral fins to the vent. Evidently, these greater distances to the insertions of the second dorsal and anal fins mean a correspondingly shorter caudal peduncle.

When this series of samples from the equatorial Pacific is compared with other samples from the more temperate waters some surprising differences are found. In the Bikini Island sample, which came from just outside the equatorial area at latitude $12^{\circ} \mathrm{N}$., the fish would be expected to resemble those from the nearby Caroline Islands to the southwest, but they had especially short. second dorsal and anal fins and a greater distance from the snout to the insertion of the first dorsal fin. The Bikini fish were small and were taken by trolling close to the island. In many regions of the Pacific these small yellowfin appear to be


Figure 16.-Distance from snout to insertion of ventral fins of small ( 65 cm .), medium ( 100 cm .), and large ( 140 um.) yellowfin tuna, as estimated from regression statistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)


Figlire 17.-Distance from insertion of ventral fin to anterior edge of vent of small ( 65 cm .), medium ( 100 cm. ), and large ( 140 cm .) yellowfin tuna, as estimated from regression statistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)


Figure 18.-Greatest body depth of small ( 65 cm .), medium ( 100 cm. ), and large ( 140 cm .) yellowfin tuna, as estimated from regression statistics. (The center line indicates the mean, the solid bar $\pm$ two standard errors of the mean, the hollow bar $\pm$ one standard deviation from regression.)
common in the vicinity of islands and are very rarely taken on longlines. So this group of small fish near Bikini may be a relatively isolated one.

Characteristics of the sample from the Philippines are particularly surprising, because in all of the characters examined the fish are much more like those of the eastern Pacific than those of the nearby Caroline Islands area. This is consistently true for all size groups in all characters. Further, in the distance from the snout to the insertion of the first dorsal fin and also to the second dorsal, the means for the Philippine sample are distinctly larger than for any other samples.

The sample from Japan consisted only of small fish and in all respects is remarkably like the groups sampled from Hawaii. In not a single character is the difference of the means great enough to separate the dark bars that represent twice the standard error of the mean and, hence, indicate a statistically significant difference between the means.

The samples from Hawaii show somewhat mixed relationships with those from the equatorial area. In head length they are similar to those from the Caroline Islands, whereas in length of fins and in the distances from snout to insertion of the second dorsal and anal fins they are much more like the yellowfin of the equatorial area southeast of Hawaii between longitudes $129^{\circ}$ and $159^{\circ} \mathrm{W}$.
'The sample of small yellowfin from the Society lslands was measured after being landed and thawed in Honolulu. Such handling may have changed the dimensions and this sample may not be directly comparable to the others. For this reason this is not a satisfactory sample. It is, however, near the Phoenix Islands sample in head length, height of the anal fin and distances from snout to first and second dorsal fins, but it has a very short second dorsal fin and much longer pectoral and anal fins than any other sample.

The sample from off Somaliland in northeast Africa is the most diverse of the group. It is similar to one or more central Pacific equatorial samples in head length and distances from snout to insertion of first and second dorsal fins, but it has very short pectoral, second dorsal, and anal fins. Somaliland fish also have a very long distance from the snout to the insertion of the anal fin, an especially deep body, and a long distance from the snout to the insertion of the ventral fins. This sample is very different from the sample from the west coast of Africa taken near Angola, where the fish are remarkably similar to those of the eastern Pacific in most dimensions. The yellowfin from Angola differ from those from Costa Rica principally in having slightly longer fins (as was pointed out by Schaefer and Walford, 1950).

In summary, yellowfin from the Pacific show a continuous cline morphologically along the Equator, whereas the samples taken in areas distant from the Equator differ erratically from the equatorial cline. The dimensions, however, are within the range of characters in the equatorial cline or
are so close to one of the ends of the cline that there appears to be no evidence of genetically isolated stocks in the Pacific. This evidence will be considered further after data on overlap have been discussed.

## COMPARISON OF SAMPLES FROM THE SAME AREA

Samples by Godsil (1948) and Godsil and Greenhood (1951) were obtained from areas also sampled by Schaefer and Walford (1950) or by POFT, and it is useful to look for evidence that different methods of measurement may have been used. Godsil's sample from Panama and Costa Rica came from an area close to that of Schnefer and Walford's from Costa Rica, and agreement among the four characters available for comparison is generally good even though Godsil's fish have slightly longer heads and a slightly longer distance from the snout to first dorsal 'fin. In addition, Godsil's sample from Hawaii may be compared with that of POFI, for it was obtained from rather limited areas: the small fish came from near Johnston Island and off islands between Kauai and French Frigate Shoals and the large fish from the Honolulu fish market. The POFI sample was obtained from a much wider area, although again most of the large fish were measured in the Honolulu market. Five measurements in two size groups are arailable to compare, and in not a single instance is the difference between means great enough to separate the black bars (and indicate a statistically significant difference).

Not as close statistically are Godsil and Greenhood's samples from Palmyra Island and the POFI samples from the eastern and western Line Islands, but the differences are complicated. Samples are available for comparison of small and medium size yellowfin taken by Godsil and Greenhood with similar sizes taken by POFI from the western Line Islands and a sample of medium size yellowfin from the eastern Line Islands. Godsil and Greenhood's data from Palmyra Island were obtained from frozen fish in a catch made during about 12 days of fishing in the vicinity of Fianning and Palmyra Islands. These days were nearly consecutive during February 1949. The POFI samples of small and medium fish were obtained from these islands as well as in the vicinity of the neighboring Washington and Christmas Islands, Kingman Reef, and a few from farther offishore.
(All of these islands are near the borderline between our eastern and western Line Islands areas.) They were, however, taken over a much longer period (table 2) so they should be much more representative of the areas than Godsil and Greenhood's samples.

When a comparison of the mean character sizes of group $M$ fish is made between our eastern and western Line Islands samples, not a single character differs by more than the length of the black bars, except height of the anal fin, and here the difference is in line with the general trend along the Equator. But when these two samples and the sample of small yellowfin from the western Line Islands are compared with Godsil and Greenhood's sample, I find that in head length their group $M$ runs smaller and their group $S$ somewhat larger; in distance from snout to insertion of first dorsal fin, their group $M$ is about the same, and their group $S$ considerably larger. Their distances from snout to insertions of second dorsal and anal fins show fairly good agreement with POFI samples. In the last character-distance from snout to insertion of the ventral fins-there is fairly good agreement between Godsil and Greenhood's sample and the POFI sample from the western Line Islands for group S ; but then for group $M$ the distance is markedly shorter than in either of the other two samples. Such erratic results suggest either that Godsil and Greenhood may have been sampling too few schools of fish to obtain a thoroughly representative sample or that freezing and thawing may have changed the proportions of the fish.

Despite these differences, I conclude that the techniques of measurement used by POFI were sufficiently close to those used by Godsil and Greenhood to arrive at about the same conclusions with regard to morphological differences among yellowfin from different areas of the Pacific.

## MULTIPLE CHARACTER COMPARISON

After having examined the data for the mean differences in body shape, I. shall consider next the overlap of the frequency distributions not merely of one character but of all characters considered simultaneously.

The measure of overlup that I shall use is similar to the measures of overlap used by taxonomists in many fields (Mayr et al., 1.953: 1.46). The measures have all arisen from the concept of
two overlapping frequency distributions and are expressed either as the percent of the actual frequency classes in the area of overlap or as a proportion of the observations estimated to be in the area of overlap of two normal distributions. The amount of overlap an be indicated as the distance between the means in units of the standard deviation or as an area under the curves. I prefer a measure of the overlapping area under two normal curves, which I have described fully (Royce, 1957) and which I have called $\Omega$. The overlap ( $\Omega$ ) is expressed as a percent and varies from 0 to 100 as the means of the distributions approach one another.

This concept of overlap is especially useful because it answers the question, "What parts of population $A$ possess characters that are within the range of population $B$ ?" I shall construe the answer to this question as a maximum for the proportion of population $A$ which might have migrated from the area of population $B$.

In the computational procedure I shall follow closely the method outlined by Rao (1952, chapters 8 and 9$)$. His method starts with pooled estimates of the correlations and standard deviations which are applied to the normalized mean values in order to transform them to values that are uncorrelated and that have unit standard deviations. In this method of analysis the amount of work increases approximately as the square of the number of characters used. To reduce the number, we have dropped from further consideration the greatest body depth, the distance from insertion of ventral fin to anterior edge of vent, and the distance from snout to insertion of ventral fins. 'This procedure seemed justifiable because (1) in some of our samples one or more of these characters were not measured, (2) none of them revealed as large differences between areas as other characters, (3) the distance from snout to insertion of ventral fins is highly correlated with head length and distance from snout to insertion of anal fin, and (4) it will be shown subsequently that seven characters are probably more than are necessary.

Because the statistics have arisen from regression analysis, it will be necessary to substitute for Rao's statistics comparable statistics determined from regression. Instead of the intragroup standard deviations from the mean, I use the intragroup standard deviations from regres-
sion. Instead of the intragroup correlations of the several characters, I use the intragroup partial correlations independent of total length. Instead of the actual mean values of the characters, I use the mean values estimated for certain given fork lengths. Therefore, in ull of the statistics the effect of any changes with fork length is removed.

It has been impossible to assume that the regression lines were satisfactory beyond limited length groups, so we have broken down all of our statistics (except for partial correlations) into the length groups which were used in the previous section for character-by-character comparisons. They are group $S$, composed of fish less than $80-\mathrm{cm}$. fork length, which are compared at a length of 65 cm . (about 12 lb .); group M, from 80 to 120 cm ., compared at a length of 100 cm . ( 43 lb .) ; and group L, more than 120 cm. , compared at a length of 140 cm . ( 11 Slb .). The basic regression constants, means, et cetera are in the appendir.

Because adequacy of the sampling varied widely, I have sought to obtain estimates of standard deviations from samples that I consider to be more representative. I have chosen the three areas most widely represented in time and among all three length groups; namely, Hawaii, western Line Islands, and eastern Caroline Islands. From these samples for each character in each size group I have obtained the standard deviation from regressions squared, $S_{y . x^{2}, \text { averaged }}$ it for the three areas, and ended with an estimate of a pooled standard deviation from regression (within groups) which gives equal weight to the three areas (table 5).

Table 5.-Pooled mean standard deviations from regression. for each body character for the three size groups

| Size group (cm.) | Head length | Length of pectoral fin | Height of- |  | Snout to insertion of- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Second dorsal fin | Anal fin | First dorsal fin | Second dorsal fin | $\begin{aligned} & \text { Anal } \\ & \text { fin } \end{aligned}$ |
| Small, <80 | 0.3981 | 0.7822 | 0.03163 | 0.03283 | 0.4470 | 0.5990 | 0. 5897 |
| Medium, 80-120 | . 5903 | 1.2891 | . 04626 | . 06141 | . 6776 | . 9426 | . $\mathbf{S 9 4 3}$ |
| Large, >120...-- | . 6596 | 1. 2280 | . 06011 | . 05680 | . 7576 | . 9581 | . 9614 |

These standard deviations are the basic units of morphological distance, and it is desirable to examine them to determine how representative they are of all samples. Two matters are pertinent: first, I have used the actual standard
deviation from regression without adjusting for the difference of the mean $\bar{x}$ from the $X$ used for comparisons, so I need to know how close the means are to the comparison values; and second I need to consider whether the average dispersion about the lines is close to the grand average of all samples. The mean lengths of the three areas (giving equal weight to each) are $62.10,99.32$, and 142.04 cm . The means chosen for comparison are 65,100 , and 140 cm . If we consider that the standard deviation is directly proportional to the length of fish, then I have tended to underestimate slightly the standard deviation for the small and the medium groups and have slightly overestimated it for the large group.

In addition, the standard deviation of $\hat{Y}$ increases with distance from $\bar{y}$. For this reason I have tended to slightly underestimate the $S_{y . x}$ for the small and large groups.

Finally, the average coefficients of variation (table 4) of the three selected areas (for five characters) for the three size groups are $1.85,1.80$, and 1.63. These coefficients are close to the grand means of all samples, which are $1.74,1.81$, and 1.81 for small, medium, and large groups, respectively. With these partly compensating and in all cases small differences, I have chosen to make no adjustments but used the standard deviations from regression directly with confidence that they are very close to the grand average.

For the partial correlations of the soveral characters independent of fork length I have used a selected sample of 30 fish each from Hawaii, Costa Rica, eastern Line Islands, western Line Islands, and central Carolines. The 30 fish were selected from each area in the size range from 80 to 130 cm . and were chosen at random within the size group. From these, the intragroup correlations (table 6) and partial correlations were calculated (table 7). ${ }^{7}$

From the means and the pooled standard deviations the normalized mean values of each character have been obtained. The mouns were simply averaged to obtain a grimd average, and then the deviations of each mean from the grand

[^5]average in units of the ayerage standard deviation were found (iable 8).

Using the notation of Rao (1952), the normalized mean values $x_{1} \ldots x_{p}$ were then transformed to values $Y_{1} \ldots Y_{p}$, which are uncorrelated, and subsequently to other values $y_{1} \ldots y_{p}$, which have unit standard deviation. The general formulas as given by Rao are-

$$
\begin{aligned}
Y_{p} & =x_{p}-a_{p p-1}-\ldots-a_{p 1} Y_{1} \\
a_{i j} & =\frac{b_{i j}}{V\left(\Gamma_{j}\right)} \text { when } j<i-1 \\
b_{i j} & =\lambda_{i j}-\sum_{t=j-1}^{1} a_{j i} b_{i t} \\
V\left(Y_{i}\right) & =\lambda_{i i}-\sum_{j=1}^{i-1} a_{i j} b_{i j} \\
y_{i} & =\frac{Y_{i}}{\sqrt{\bar{V}\left(\overline{Y_{i}}\right)}}
\end{aligned}
$$

The $a$ and $b$ values (tables 9 and 10) are convenient intermediate values in the computations. $V\left(Y_{i}\right)$ (table 11) is the variance of $Y_{i}$ and $y_{i}$ and is the final transformed value of the normalized mean (table 12). From these transformed means which have unit standard deviation and which are uncorrelated with one another, I obtained the distance in units of the standard deviation squared ( $D^{2}$ ) for each possible area comparison in each size group (table 13). The total $D^{2}$, obtained by adding the $D^{2}$ values for each of the seven characters, is subject to a small bias due to the number of characters and the size of the samples. This bias (which is largest in the smallest samples and most troublesome in the samples most closely related) is removed by subtracting the value

$$
p \frac{n_{1}+n_{2}}{n_{1} n_{2}}
$$

in which $p$ is the number of characters and $n_{1}$ and $n_{2}$ the number of observations in each sample (Rao, 1952: 364). ${ }^{8}$

From the adjusted sum of $D^{2}$ the value of the overlap ( $\Omega$ ) is determined by finding $D$, then $\frac{D}{2}$, which is used as an argument to enter the tables of the areit.under a normal curve to find the area of one tail and then multiplying by 200 to express the area of two tails as a percentage $\Omega$.

[^6][See text for explanations]

| Character | $\begin{aligned} & \text { Head } \\ & \text { length } \end{aligned}$ | Length of pectoral fin | Height of- |  | Snout to insertion of- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Second dorsal fin | Anal fin | First dorsal in | Second dorsal fin | Anal fin |
| Fork length. | 0. 08422 | 0.92124 | 0.93830 | 0.92534 | 0. 97846 | 0.99448 | 0.99210 |
| Fread length.-...-.-. |  | . 90009 | .92767 | . 91515 | . 98329 | . 986687 | . 98818 |
| Length of peetoral fin. |  |  | . 92373 | . 89801 | . 88439 | . 90894 | . 90865 |
| Height of Second dorsal fin. |  |  |  | . 96177 | . 91393 | . 92877 | 92584 |
| Anal fin.---.-.-- |  |  |  |  | . 90770 | . 91479 | . 90931 |
| Snout to insertion of- |  |  |  |  |  |  |  |
| First dorsal fin.--- |  |  |  |  |  | . 98647 | . 97739 |
| Sceond dorsal fin.. |  |  |  |  |  |  | . 99074 |

Table 7.—Partial correlations of body characters, independent of fork length

| Charater | 1 Iead length | Length of pectoral fin | Ireight of- |  | Snout to insertion of- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Second dorsal fin | Anal fin | First dorsal fin | Second dorsal fin | Anal fin |
| Iread length.- | 1.0000 | -0.0960 | 0.0883 | 0.0657 | 0.5549 | 0. 4243 | 0.4387 |
| Length of pectoral fin |  | 1.0000 | . 4409 | . 3088 | -. 0873 | -. 1766 | -. 1088 |
| -Leight of- Second dorsal fin |  |  | 1.0000 | . 7133 | -. 0583 | -. 1199 | -. 1164 |
| Anal fin.-------- |  |  |  | 1.0000 | . 0292 | $-.1367$ | -. 1833 |
| Snout to insertion of- |  |  |  |  |  |  |  |
| First dorsal fin_-- |  |  |  |  | 1.0000 | .6191 1.0000 | .2571 .3131 |
| Anal fin..-.-.-.-. |  |  |  |  |  |  | 1. 0000 |

Table 8.-Normalized mean values $\mathbf{x}_{\mathrm{i}}$ of body characters

| Size group and area | Head length | Length pectoral fin | Height of- |  | Snout to insertion of- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Second dorsal fin | $\begin{aligned} & \text { Anal } \\ & \text { fin } \end{aligned}$ | First dorsal fin | Second dorsal fin | $\begin{aligned} & \text { Anal } \\ & \text { fn } \end{aligned}$ |
| SMALL-SIZE GROUP |  |  |  |  |  |  |  |
| West Line Islands | 0.9797 | -0.3068 | -0. 2308 | -0.1889 | -0.2461 | 0. 0334 | -0. 1187 |
| Phoenix Islands | a -6782 $-\quad 5024$ | $-.0511$ | - 5185 | -. 2315 | -. 2284 | -. 03844 | -. 5257 |
| Bikini Island. | -. 5024 | .2813 1.3424 | -. 2940 | -. 1.2489 | .9843 -.7383 | -. 4841 | -.5935 -.8818 |
| Central Caroline Islands. | -. 7284 | 1.5597 | 1.3468 | 1.0448 | -. 7383 | -. 4874 | -. 2035 |
| Japan. | -. 3266 | . 3963 | . 3351 | . 1340 | $-.2013$ | . 1669 | -. 2713 |
| Hawail | $-.5536$ | -. 1790 | $-.1676$ | $-.0061$ | . 3808 | . 5342 | . 2544 |
| Northeast Africa | 1. 1304 | -3. 0043 | -2. 7347 | -2.3089 | . 8725 | . 7846 | 2. 3402 |
| Costa Rica Medium-size group |  |  |  |  |  |  |  |
| East Line Isiands. | . 6776 | -1. 5740 | -1. 2810 | -1.3843 | $-.0443$ | -. 2228 | -. 1565 |
| West Line Islands. | . 5540 | -. 1164 | . 0843 | . 2215 |  | -. 2228 | $-.4137$ |
| Phoenix Islands. | . 1016 | . 7214 | . 5275 | . 6009 | -. 1433 | -. 5092 | -. 7045 |
| East Caroline Islands | -1.2197 | . 9619 | 1.1911 | 1.0780 | -. 5313 | -. 7532 | -1.3083 |
| Central Caroline Islands | -1.2367 | 1.2411 | 1.1170 | . 9168 | -. 5756 | -. 8805 | -. 8722 |
| Hawaii | -. 5252 | -. 1551 | -.4172 | -. 3713 |  |  |  |
| Angola, Africa | . 7623 | -.6283 | -. 5275 | . 7572 | .4280 | 1. 2306 | 1. 0846 |
|  | . 2122 | -1.3029 | -1. 5339 | -1.9894 | . 1320 | 1.2420 | 1.2690 |
| $119^{\circ}-129^{\circ} \mathrm{W}$ | . 3335 | $-.5130$ | -1.1429 | -1.2993 | . 5280 | . 4175 | . 364 |
| $129^{\circ}-139^{\circ} \mathrm{W}$ | . 2426 | -. 5782 | -. 8285 | -. 8838 | . 4884 | . 5219 | . 4473 |
| $139^{\circ}-149^{\circ} \mathrm{W}$ | . 0910 | . 2524 | -. 5107 | -. 4806 | -. 0598 | . 1774 | . 2288 |
| East Line Islands | -. 2122 | . 1629 | . 2196 | . 2289 | -. 2640 | -. 1566 | . 5409 |
| West Line Islands. | . 3487 | . 3502 | . 5523 | . 6454 | -. 5412 | -. 3862 | -. 1144 |
| Phoenix Islands. | -. 2122 | . 3339 | . 7969 | 1.0000 | -. 4488 | -. 3549 | -. 6969 |
| East Marshall Isiands | -. 5761 | . 2769 | 1. 2610 | 1. 4754 | -. 1584 | -. 0417 | -. 6553 |
| East Caroline Islands | -. 6216 | . 5375 | 1. 3026 | 1. 5933 | -. 2336 | -1. 0437 | -1. 3106 |
| Central Caroline Islands | -. 2274 | . 4805 | 1.3159 | 1. 5827 | -. 3300 | -. 9498 | -. 8217 |
| Hawail------- | -.6822 | .3013 -.2606 | -1.3876 | -.4947 -1.4261 | . 1188 | -. 2818 | .1768 .5721 |

The results of these computations expressed as the percentage of overlap between areas appear in table 14. Here the equatorial series has been arranged in order from Costa Rica on the east to
the central Carolines on the west. The other samples from Bikini Island, Japan, Hawaii, Angola, and northeast Africa are added in no special order.

Table 9.-Table of a
[See text for explanation]

| Character | Head length | Length of pectoral fin | Height of- |  | Snout to insertion of- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Second dorsal fin | Anal fin | First dorsal fin | Second dorsal fin | Anal fin |
| Head length.-.------- | 1.0000 | -0.0960 | 0.0633 | 0.6507 | 0.5549 | 0.4243 | 0.4387 |
| Length of pectoral fin. |  | 1.0000 | . 45162 | . 31804 | -. 03435 | -. 13713 | -. 06731 |
| $\begin{aligned} & \text { Height of } \\ & \text { Second dorsal fin.- } \end{aligned}$ |  |  | 1. 0000 | . 71415 | -. 10190 | -. 11033 |  |
| Anal fin--------- |  |  |  | 1.0000 | . 12436 | -. 11991 | -. 21979 |
| Snout to insertion of- |  |  |  |  |  |  |  |
| First dorsal fin |  |  |  |  | 1.0000 | . 55912 |  |
| Second dorsal fin---- |  |  |  |  |  | 1.0000 | $\begin{array}{r} .14781 \\ 1.0000 \end{array}$ |

Table 10.—Table of $b$
[See text for explanation]

| Character | Head length | Length of pectoral fin | Height of- |  | Snout to insertion of- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Second dorsal fin | Anal fin | First dorsal fin | Second dorsal fin | Anal fin |
| Head length ------.-- | 1.0000 | $\begin{array}{r} -0.0060 \\ 1.0000 \end{array}$ | 0.084.4476 | 0.0657 .31511 | 0.5549-.03403 | 0.4243-.13587 | $\begin{gathered} 0.4387 \\ -.06688 \end{gathered}$ |
| Length of pectoral inn- |  |  |  |  |  |  |  |
| second dorsal fin. |  |  | 1.0000 | .56650 -.08083 <br> 1.0000 -.06129 |  | -.08759-.05880 | $\begin{array}{r} -.11625 \\ -.10790 \end{array}$ |
| Anal fin-.------- |  |  |  |  |  |  |  |  |
| Snout to insertion of-- |  |  |  |  |  |  |  |
| Second dorsal fin- |  |  |  |  | 1.0000 | $\begin{aligned} & .37742 \\ & 1.0000 \end{aligned}$ | $\begin{array}{r} .01300 \\ .08478 \\ 1.0000 \end{array}$ |
| Anal fin--------- |  |  |  |  |  |  |  |

Note.-These values are recorded in 5 significant figures; however, 8 significant figures were carried in the computations leading to a-values. The first row was obtained by preceding computations to 4 significant figures.

Table 11.-Variances and square roots of variances for various body measurements
[See text for explanation]

| Variate | $\begin{gathered} \text { Variance I } \\ V\left(Y_{i}\right) \end{gathered}$ | $\mathrm{D} \sqrt{V\left(Y_{i}\right)}$ | Variate | $\begin{gathered} \text { Variance }{ }^{1} \\ V\left(\boldsymbol{Y}_{i}\right) \end{gathered}$ | $D \sqrt{F\left(Y_{i}\right)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $V\left(Y_{1}\right) \ldots$ | 1.00000 | 1.00000 | $V\left(Y_{*}\right)^{\prime}$ | 57360 | . 75730 |
| $V\left(Y_{2}\right) \ldots$ | . 99078 | . 99538 | $V\left(\mathrm{I}_{7}\right)$ | . 74952 | 86575 |
| $V\left(Y_{3}\right) \ldots$ | 79325 | . 840065 | V ( $\mathrm{Y}^{\mathbf{8}}$ ) | . 76599 | . 87521 |
| $V(\underline{Y}$ ) | . 49090 | . 70066 | $1 \cdot(\mathrm{P})^{\prime}$ | 40215 | . 63415 |
| $V\left(\mathrm{I}_{6}\right) \ldots$ | . 67503 | . 82160 | $F\left(Y_{10}\right)$ | 33024 | . 57466 |

1 Values are recorded in 5 significant figures; however, 8 significant figures were carried in the computations leading to $a$-values (in table 9 ).

In the equatorial series there is a clear tendency for more closely located samples to have greater overlap. The overlap varies from a maximum of 82 percent and 81 percent in medium and large size groups for the comparison between eastern Carolines and central Carolines to a low of 3 percent for the comparison of Costa Rica with eastern Carolines and central Carolines. The relation of the average overlap to the separation of the samples in miles (fig. 19) is clear cut and much the same in all size groups. This graph has been made with the assumption that each population was located in the center of each $10^{\circ}$ block of longitude and that the centers of these blocks were separated by units of 600 miles.


Figure 19.-Average percent of overlap of samples of yellowfin from the equatorial Pacific.
(This assumption disregards the small variations in location within the sample areas and the fact that one sample area was $11^{\circ}$ of longitude in width instead of $10^{\circ}$.)

From this graph it appears that, on the average, sumples of yellowfin tuna from along the Equator separated by 1,500 miles overlap less than 50
[See text for explanation]

percent in the seven characters considered; those separated by 3,000 miles overlap less than 25 percent; and those separated by 6,000 miles overlap less than 6 percent.

The graph also shows that the average overlap varies little with the size group of fish, although the data in table 14 indicate a slight tendency for the small and medium size groups to have less overlap than the large. This tendency appears to be most marked in the comparisons of samples' from the western Line and Phoenix Islands areas with those from the eastern and central Caroline Islands areas: In all of these comparisons the large size group shows the most overlap and the small size group the least. In the comparisons of the Hawaiian samples with those from the equatorial area, the small size group shows the least overlap, but the medium size group generally shows slightly greater overlap than the large. The data are too scant to establish the significance of this tendency, but it may be associated with more wandering by the larger fish.

The overlap of the other samples with those from the equatorial Pacific area follows, in general, the relations that were deduced from consideration of single characters. The Bikini Island
sample shows rather little overlap with any of the equatorial samples-even the sample from the nearby Caroline Islands areu-but a considerable overlap with samples from Japan and Hawaii. The Japanese sample, on the other hand, is apparently intermediate in structure between the Bikini Island and equatorial samples, for it shows a considerable overlap with all other samples where a comparison is possible. The samples from Hawaii, likewise, show a fairly large amount of overlap with most of the equatorial samples, but the largest size group is most similar to the equatorial yellowfin from between longitudes $129^{\circ}$ and $159^{\circ} \mathrm{W}$. This area is generally southeast of Hawaii rather than directly south. The Angola, Africa, fish show a large amount of overlap with the large fish from longitudes $119^{\circ}$ to $149^{\circ} \mathrm{W}$. They are as similar to these fish as are many of the samples from adjoining areas along the Pacific Equator. Moreover, in all comparisons of Angola samples with samples from $119^{\circ}$ to $149^{\circ} \mathrm{W}$. there is a marked tendency for the overlap to be less among the larger size group than the medium size group. This finding conforms with the observation made by Schaefer and Walford (1950) that the principal characters differentiating

Table 13.-Value of $D^{2}$ computed from transformed means and adjusted for sample size to determine percentage of overlap ( $\Omega$

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline \multirow[b]{2}{*}{Size group and arca} \& \multirow{2}{*}{Head} \& \multirow[t]{2}{*}{\[
\begin{gathered}
\text { Length } \\
\text { of } \\
\text { pectoral } \\
\text { fin }
\end{gathered}
\]} \& \multicolumn{2}{|l|}{Height of-} \& \multicolumn{3}{|l|}{Snout to insertion of-} \& \multirow[b]{2}{*}{\(D^{1}\)} \& \multirow[b]{2}{*}{Bias} \& \multirow[b]{2}{*}{Adjusted} \& \multirow[b]{2}{*}{\(\boldsymbol{\Omega}\)} \\
\hline \& \& \& Second dorsal fin \& Anal fin \& \(\underset{\text { dorsal fin }}{\text { First }}\) \& Second dorsal fin \& Anal fin \& \& \& \& \\
\hline \multicolumn{12}{|l|}{small-size group} \\
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} \\
\hline \& \& \& \& \& \& \& \& \& \& \& 11 \\
\hline - East Caroline Islands--- \& \(\stackrel{\text { - }}{\text { ¢ }}\) \&  \& - \({ }^{\text {1.0665 }}\) \& . 30457 \& . 313137 \& . 0758 \& - 1.05668 \&  \& . 37858 \& 6.2199 \& 21
15 \\
\hline -Japan.- \& 1. 7004 \& - 3367 \& \(\begin{array}{r}1.81895 \\ \\ \hline\end{array}\) \& . 0055 \& 1.0343 \& . 2375 \& \({ }^{1.0772}\) \& 8. \({ }^{\text {8. } 6460}\) \& . 34882 \& 8.2978
3.3765 \& \(\stackrel{15}{36}\) \\
\hline - Hawaii. \& 2.3479 \& . 0004 \& . 7691 \& . 0977 \& 3. 1528 \& . 2384 \& 1. 39858 \& 8.0051 \& . 3535 \& 7.6516 \& 17 \\
\hline Phoenix-Bikinit Islands \& . 1.02938 \& 7. \({ }^{\text {26547 }}\) \& 2.1360
.8827 \& \begin{tabular}{l}
2452 \\
0920 \\
\hline 0
\end{tabular} \& 2.2479
4.5826 \& 1.2052 \& 5. 32736 \& 17.3503 \& 3049
.4150 \& 17.0454 \& 4 \\
\hline -East Caroline Isiands. \& 1. 1.773 \& 1. 63353 \& . 0554 \& 6059 \& . 0476 \& \({ }^{.0781}\) \& . 2096 \& 4. 2092 \& . 3059 \& 3. 8033 \& 32 \\
\hline -Central Caroline Island \& 1.9785 \& 2. 1981 \& . 0793 \& 1348 \& 1424 \& . 1093 \& 1. 5821 \& 6. 2345 \& . 3784 \& 5. 8461 \& \({ }^{23}\) \\
\hline \({ }^{\text {Japan }}\) \& 1.0096 \& 1243 \& . 0977 \& . 0063 \& . 4591 \& . 2415 \& . 5.204 \& 2. 4589 \& 4150 \& 3.0439 \& 47 \\
\hline - Corthawail ------ \& 1. 5149 \&  \& 2.6400 \& . 2171 \& 2. 2.0627 \& . 2748 \& 1.9673 \& 8.7379 \& \({ }^{.} 38360\) \& \% 8.3543 \& \(\stackrel{15}{2}\) \\
\hline Bikinl-East Caroline Islands. \& . 0057 \& 1. 1208 \& 1.3802 \& :2257 \& 3. 6986 \& 2. 4339 \& . 0139 \& 8.8762 \& . 3425 \& -1.2337 \& 14 \\
\hline -Central Carolinc Island \& . 0511 \& 1. 5939 \& 1.4911 \& . 0041 \& 3. 1096 \& 2. 5963 \& . 4653 \& 9.3114 \& 4150 \& 8. 8964 \& 14 \\
\hline - Tapan \& . 0309 \& . 0175 \& . 3931 \& . 0501 \& 2. 1407 \& 3. 1403 \& . 612 \& 5. 7938 \& 4516 \& 5. 3422 \& 25 \\
\hline -Northeast Africa \& -. 2.6005 \& -.184 \& - 1.6096 \& . 4104 \& . 94638 \& 3.1439 \& - \({ }^{\text {. } 6838}\) \& 5.0409 \& +403 \& 4. \({ }^{\text {4.eOf }}\) \& \(\stackrel{28}{3}\) \\
\hline East Caroline-Central C \& . 0229 \& . 04115 \& \({ }^{.} .0021\) \& 1692 \& . 0253 \& . 0026 \& . 646400 \& 19.95034 \& \({ }_{3759}\) \& \(\begin{array}{r}19.5851 \\ \hline 5975\end{array}\) \& 70 \\
\hline Japan. \& 0631 \& . 86880 \& 3001 \& 48516 \& 2110 \& . 0449 \& . 0695 \& 2.0352 \& 3425 \& 1.6927 \& 51 \\
\hline -Hawaii. \& . 00006 \&  \& 3. 4600 \& 0977 \& 1.4835 \& 0454 \& 8926 \& 8. 3035 \& 3111 \& 7. 9974 \& 16 \\
\hline Central Carcline \({ }^{\text {- }}\) Northeast Africa- \& 2. 9176 \& 17.6576 \& 5. 35731 \& 1. 2548 \& .8868 \& . 5304 \& 4. 19897 \& \(\stackrel{33.4197}{2781}\) \& . 26625 \& 33.1572 \& \\
\hline Central Carcline islands-Japan \& 1634

0309 \& - 1.27812 \& 3. 33344 \& . 00088 \& 1. 1213 \& . 02029 \& . 28877 \& 3.2731
7.8358 \& . 41880 \& 1. 7.8681 \& <br>
\hline -Northeast \& 3.4551 \& 19.4120 \& 6. 2046 \& . 5025 \& 1.6125 \& . 6076 \& -1.5588 \& 32.3531 \& . 3850 \& 32. 0181 \& <br>
\hline Japan-Hawaii \& . 0511 \& . 35949 \& 1.7021 \& . 1494 \& 5755 \& . $0000+$ \& . 4640 \& ${ }^{3} .3217$ \& . 4203 \& 2. 0014 \& <br>
\hline -Northeast A \& - 3.1808 \& 10.7309 \& 3. 5979 \& . 1774 \& . 2326 \& .8842 \& 3. 1859 \& 20.0317 \& . 3716 \& 20.5601 \& <br>
\hline Hawaii-Northeast Africa \& 2.8325 \& 7.1615 \& . 3416 \& .6534 \& .0763 \& . 8860 \& 1.2182 \& 13.1685 \& . 3403 \& 12.8282 \& 7 <br>
\hline $\pm D^{2}$ \& 33.8002 \& 101.3132 \& 45.2911 \& 6.3107 \& 37.8848 \& 20.1191 \& 36.5245 \& \& \& \& <br>
\hline Mean \& 1.2072 \& 3. 6183 \& 1.6175 \& . 2254 \& 1.3530 \& . 7185 \& 1.3044 \& \& \& \& <br>
\hline ${ }_{\mathbf{R}}$ means \& ${ }_{58}^{1.2072}$ \& 4. 8.55 \& ${ }_{20}^{6.4430}$ \& ${ }_{20}^{6.6684}$ \& ${ }_{16} 8.0214$ \& 8. 7399 \& 10.0443 \& \& \& \& <br>
\hline \multicolumn{12}{|l|}{medium-size group} <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& ${ }^{1036}$ \& 1. 6541 \& 1. 9069 \& . 1464 \& . 0441 \& . 8205 \& 4. 7594 \& 9.4350 \& ${ }^{3} \mathbf{3} 218$ \& 9. 1132 \& 13 <br>
\hline -East Caroline Isian \& - 4.41273 \& 4. 4.3185
4.8303 \& 1.2756

5.2436 \& . 2409 \& . 20001 \& . 97685 \& | 4.7476 |
| :--- |
| 4.471 | \& 13.1898

19.9841 \& - 3600 \& 12.8298 \& 3 <br>
\hline -Central Caroline Islan \& 4.4842 \& 6. 1340 \& 4.2758 \& . 1458 \& 1829 \& 7249 \& 2.6387 \& 18. 5863 \& . 3100 \& ${ }_{18} 18.2763$ \& ${ }_{3}$ <br>
\hline -Hawaii \& 1.9771 \& 1.3055 \& 9357 \& 0061 \& 8725 \& . 1318 \& . 9461 \& 6.1748 \& 4473 \& 5. 7275 \& ${ }_{3}$ <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \multicolumn{12}{|l|}{\multirow[b]{2}{*}{}} <br>
\hline \& \& \& \& \& \& \& \& \& \& \& <br>
\hline -Central Caroline Islands \& 3. 6645 \& 2.6860 \& . 7330 \& . 2479 \& 5753 \& . 0435 \& .2030 \& 8. 1932 \& . 2807 \& $7.8125^{\circ}$ \& <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& \& \& \& \& \& \& \& \& \& \& <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& 3. 1638 \& 8312 \& . 883 \& . 0331 \& 4581 \& . 0342 \& \& 5.3411 \& . 2077 \& 5.1334 \& <br>
\hline -Central Caroline Island \& 3. 2245 \& 1.4175 \& . 4718 \& .0000+ \& . 4063 \& . 0030 \& 3105 \& 5. 8340 \& 1491 \& 5. 6849 \& 23 <br>
\hline -Hawaii. \& 1. 1755 \& . 0206 \& . 1711 \& . 0925 \& 1.3090 \& 2945 \& 1.4614 \& 4.5246 \& 2863 \& 4. 2383 \& 30 <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& \& \& \& \& \& \& \& \& \& \& <br>
\hline -Hawaii \& . 3929 \& 8857 \& 2929 \& 1701 \& 8560 \& . 3908 \& 1.4549 \& 4. 4433 \& . 3245 \& 4. 1188 \& 31 <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& . 0003 \& . 0778 \& . 0493 \& .0234 \& . 0015 \& . 0170 \& . 2409 \& . 4102 \& 1959 \& 2143 \& 82 <br>
\hline -Hawali-------------- \& \& 1.1134 \& 1.7493 \& . 2082 \& . 2184 \& .1281 \& 1.3053 \& 5. 2050 \& 3382 \& 4.8718 \& <br>
\hline \multicolumn{8}{|l|}{\multirow[t]{2}{*}{}} \& \& 4606 \& 10.8529 \& <br>
\hline \& 5062 \& 1.7798 \& 1.2111 \& . 0921 \& . 2564 \& 2384 \& . 4447 \& 4. 5087 \& 2745 \& 4.2342 \& <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& \& \& \& \& \& \& \& \& \& \& <br>
\hline \& 43.4554 \& 39.7637 \& 28.5558 \& 6. 1582 \& 9.4942 \& \& 35.5809 \& \& \& \& <br>
\hline Mean \& 1.5550 \& 1.4201 \& 1. 10109 \& 2199 \& 3391 \& 5671 \& 1.2707 \& \& \& \& <br>
\hline ans \& 1.5520 \& 3.9721 \& 3. 9920 \& 4. 2119 \& 4. 5510 \& 5.1181 \& 6. 3888 \& \& \& \& <br>
\hline \& \& \& \& \& 29 \& 26 \& \& \& \& \& <br>
\hline \multicolumn{12}{|l|}{large-size mronp} <br>
\hline \multicolumn{12}{|l|}{\multirow[t]{2}{*}{}} <br>
\hline \& . 0009 \& - 5354 \& . 1777 \& . 7443 \& 1587 \& . 8559 \& . 3214 \& $\underline{2.7988}$ \& . 4823 \& 2.3145 \& 45 <br>
\hline - ${ }^{-139^{\circ}-149^{\circ} \mathrm{W}}$ \& 1469

.1801 \& - 3.3510 \& - 1.1471 \& 1.2629 \& \begin{tabular}{l}
0245 <br>
0207 <br>
\hline 0

 \& $\begin{array}{r}.6273 \\ .8885 \\ \hline\end{array}$ \& . 41885 \& 4.73732 \& 

3853 <br>
\hline 3779
\end{tabular} \& 4. ${ }^{\text {4 } 5859}$ \& ${ }_{21}^{28}$ <br>

\hline -West Line Islands \& . 0186 \& 2. 8023 \& $\underline{2} .2135$ \& -1. 9313 \& . 7383 \& 1.0406 \& . 7218 \& 10.4674 \& 4540 \& 10. 0134 \& 11 <br>
\hline -Phnenix Islands \& . 1801 \& $\stackrel{2}{2712}$ \& 3. 3775 \& 3. 6615 \& 1255 \& . 8393 \& 1,3870 \& 12. 1420 \& 4855 \& 11.6565 \& 9 <br>
\hline - East Marshall Isla \& ${ }^{6214}$ \& ${ }^{2.2834}$ \& 5. 9117 \& 4. 53.36 \& 045 \& - 3617 \& . 78981 \& 14.5604 \& . 5083 \& 14.0521 \& ${ }^{6}$ <br>
\hline - East Caroline istands \& . 19852 \& 3.17601
3.0601 \& +5.5131 \& 5. ${ }^{\text {5. }} \mathbf{0 1 7 7}$ \& -0428 \& 3.2455
2.8190 \& - 1.0251 \& 17.6809 \& 4583
.4306 \& 19.3062
17.2603 \& <br>
\hline -Hawall: \& \& 2.3268 \& . 3372 \& 1.0016 \& 3710 \& 2.0136 \& . 0.58 \& 6. 9082 \& 3880 \& 6.5222 \& 20 <br>
\hline -Angola, A \& 1.2250 \& 1.3315 \& . 0138 \& . 0815 \& 0118 \& . 7898 \& 1.2592 \& 4.7056 \& 5926 \& 4.1130 \& 31 <br>
\hline
\end{tabular}

Table 13.-Value of D2 computed from transformed means and adjusled for sample size to determine percentage of overlap ( $\Omega$ )Continued

the Angola and Costa Rica samples-length of the pectoral fin and heights of the second dorsal fin and the anal fins-all have significantly higher regression coefficients in the Angola samples and diverge more from the Costa Rica sample in the larger size groups.

Lastly, the sample from northeast Africa shows little overlap with any other sample. Such is to
be expected because of the marked differences in fin lengths and distance from the snout to the insertion of the anal fin, which have already been pointed out. However, it has also been mentioned that this sample from northeast Africa was not composed of yellowfin of a size strictly comparable to any of our size groups. Thus, much of these differences may have arisen because of the effects

Table 14.-Percent of overlap ( $\Omega$ ) between areas, using seven characters

| Area and size group | $109^{\circ}-$ | $129^{\circ} \mathrm{W}$ | $139^{\circ} \mathrm{W}$ | $\begin{gathered} 13 y^{\circ}- \\ 149^{\circ} w . \end{gathered}$ | $\begin{gathered} \text { East } \\ \text { Line } \\ \text { Islands } \end{gathered}$ | $\begin{gathered} \text { West } \\ \text { Line } \\ \text { Islands } \end{gathered}$ | Phoenix <br> Is lands |  |  | Central CaroIslands | Bikini Island | Japan | Hawaii | Angola, Africa | Northuast Africa |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Costa Rica: M. |  |  |  |  | 18 | 13 | 7 |  | 3 | 3 |  |  | 23 | 45 |  |
| $109^{\circ}-119^{\circ} \mathrm{W} .:$ L |  | 33 | 45 | 28 | 21 | 11. | 9 | ¢- | 3 | 4 |  |  | 20 | 31 |  |
| $119^{\circ}-129^{\circ} \mathrm{W} .:$ L |  |  | 71 | 52 | 27 | 24 | 31 | 12 | 11 | 12 |  |  | 3 S | 62 |  |
| $129^{\circ}-139^{\circ} \mathrm{W} .:$ L |  |  |  | 64 | 46 | 31 | $\stackrel{88}{8}$ | 19 | 14 | 10 |  |  | 51 | 49 |  |
| $139^{\circ}-149^{\circ} \mathrm{W} .:$ L |  |  |  |  | 55 | 47 | 39 | 23 | 18 | 23 |  |  | 52 | 42 | - |
| East Line Islands: |  |  |  |  |  |  |  |  | 17 | 16 |  |  | 19 | 30 |  |
| L |  |  |  |  |  | 51 | 48 | 30 | 29 | 34 |  |  | 528 | 19 |  |
| West Line Islands: |  |  |  |  |  |  |  |  | 21 | 15 | 11 | 36 |  |  |  |
| M-------- |  |  |  |  |  |  | 67 |  | 21 | 23 |  |  | 30 | $31-$ |  |
| L. |  |  |  |  |  |  | 70 | 37 | 33 | 47 |  |  | 27 | 20 |  |
| Phoenix Islands: S |  |  |  |  |  |  |  |  | 32 | 23 | 14 | 47 |  |  | 2 |
| M |  |  |  |  |  |  |  |  | 44 | 42 |  |  | 31 | 21 |  |
| 1. |  |  |  |  |  |  |  | 65 | 55 | 55 |  |  | 29 | 14 | ------ |
| East Marshall Islands: L |  |  |  |  |  |  |  |  | 53 | 56 |  |  | 23 | 7 | ------- |
| East Caroline Islands: |  |  |  |  |  |  |  |  |  |  | 14 | 51 |  |  | . 4 |
| $\mathrm{M}^{\prime}$ |  |  |  |  |  |  |  |  |  | 82 | 14 | 51 | $\stackrel{18}{97}$ | 10 | . 4 |
| L |  |  |  |  |  |  |  |  |  | 81 |  |  | 21 | 4 | ------ |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| S $\mathrm{M}^{\text {---------- }}$ |  |  |  |  |  |  |  |  |  |  | 14 | 49 | 17 |  | 4 |
| L.----- |  |  |  |  |  |  |  |  |  |  |  |  | 30 | 11 |  |
| Bikini Island: S . |  |  |  |  |  |  |  |  |  |  |  | 25 | 2 S |  | 3 |
| Japan: S....... |  |  |  |  |  |  |  |  |  |  |  |  | 39 |  | 2 |
| Hawaii: |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathbf{S}_{\mathbf{M}_{-}^{-}}^{-}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 7 |
| L. |  |  |  |  |  |  |  |  |  |  |  |  |  | 22 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

of curvilinear regressions, and I cannot say with confidence that this size group is as different as the data indicate.

## EVALUATION OF MULTIVARIATE ANALYSIS

A full evaluation of the merits of the multivariate analysis which I have used here is beyond the scope of this article. ${ }^{9}$ But the procedure is so laborious that some discussion of the value of considering extra characters is warranted. The labor increases approximately in relation to the square of the number of characters, but Mabalanobis, Majundar, and Rao (1949) refer to Mahalanobis, Bose, and Roy (1937), ${ }^{10}$ in which it is shown that $D^{2}$ approaches a limit as additional characters are considered. On an intuitive basis this would be expected to happen rather quickly, because as additional characters are considered they would have an increased chance of being correlated with previously considered characters. The extra amount of work involved in making the $D^{2}$ analysis is approximately related to the square of the number of characters considered, so the problem is how many characters must be con-

[^7]sidered to arrive at a reasonably stable estimate of overlap.

It can be shown readily that more than one character must be considered. To demonstrate this, I have taken 10 comparisons at random out of the total of 122 and calculated the overlap of the single characters showing the greatest difference between samples. These, I compared with the overlap computed from seven characters (table 15). In all but one ${ }^{11}$ there is a substantial reduction in the overlap due to the extra characters. In fact, the single character comparison with the least overlap, that between eastern Marshalls and Angola with respect to height of the anal fin, still shows an overlap of 40 percent. This is reduced to 7 percent when six more characters are added.

The average effect of adding characters one by one may be obtained from the grand average, $D^{2}$, for each size group. These averages have been obtained from table 13 for each character and the overlap computed, first for one character, then two characters, and so on until the seven are considered. It may be seen (fig. 20) that most

[^8]

Figure 20.-Effeet of adding characters on average overlap of all sample comparisons.
of the reduction (if any) in $D^{2}$ occurs in the first three or four characters, but that there is a continuing gradual reduction to the seventh character.
Tarle 15.-Comparison of overlap of one character with
overlap of seven characters considered simultaneously

Another approach has been made in an examination of the character-by-character overlap of our most different, most similar, and moderately different equatorial samples (fig. 21). Here again it may be seen that in each case most of the reduction in overlap (if any) occurs in the first three or four characters.

It would also have been possible to improve the order in which I have considered the characters. The most useful characters are those that show the greatest difference among samples and the least


Figure 21.-Effect of adding characters on overlap of selected comparisons.
correlation with other characters. Thus, a consideration of our character-by-character comparisons and the partial correlations of table 7 indicates that it would be desirable to consider height of the anal fin, which is one of the characters showing the greatest difference among samples, but not height, of second dorsal fin, which is closely correlated with the height of the anal fin. For a similar reason I could have omitted the distance from the snout to insertion of the second dorsal fin after considering that of the snout to insertion of the first dorsal fin, with which it is highly correlated. Another rather high correlation exists between head length and distance from snout to insertion of first dorsal fin.

Thus, it would appear that had I considered only the best four characters, I would have found substantially the same overlap that I did in considering seven. This would have reduced the work of computation to about one-third of that for the seven characters. Rao (1952: 256) notes also that it is profitable to use samples of equal size.

## EXTENT OF INTERMINGLING

As I have previously argued, the percentage of overlap of two samples may be considered to represent the maximum proportion of one sample that might belong to the other. When this concept is extended to two populations separated geographically, the overlap may be assumed to be the proportion of one which might have come from the other. There is, of course, no evidence that any part of the population did come from another, but the overlap may be used, together with other data, to estimate how much intermingling might be occurring.

Such use requires an assumption thait the characters selected to estimate the overlap are fixed. If the characters are genotypic and fixed at time of fertilization, then the overlap would indicate a maximum amount of genetic mixing (gene flow). Many characters, however, are fixed during early development and vary according to environment, especially temperature. Even so, the amount of overlap would still indicate a maximum possible amount of intermingling.

Clearly, between the two ends of the Pacific Equator the overlap is so small (3 percent) that there can be practically no intermingling. Along this long belt where the yellowfin distribution is continuous, I have previously noted that the average overlap is less than 50 percent in samples separated by 1,500 miles and less than 25 percent in samples separated by 3,000 miles. Consequently, it seems probable that east-west migration must be relatively limited and that most yellowfin tuna probably remain within a few hundred miles of where they occur as postlarvae. The eggs and larvae drift passively with the currents, but development is rapid and it seems unlikely that they could drift more than 300 or 400 miles before becoming active swimmers.

I have noted previously that the average overlap among samples was about the same for the different size groups. This clearly indicates that after they reach a weight of about 5 pounds ( 50 cm .) there is no tendency for samples of the larger fish to become more diverse. Such evidence indicates that the morphological differences arise very early in life and considering the similar enviromment in the surface layers along the Equator it seems probable that the differences are genotypic.

The samples from farther away from the Equa-tor-Bikini Island, Japan, and Hawaii-are separated from the Equator by a zone where yellowfin are relatively scarce. The Bikini sample shows little overlap with samples from the adjoining equatorial areas, much less in fact than with the Japanese sample. The Hawaiian sample shows little overlap with the smaller sizes from the equatorial areas, but the larger sizes are quite like those from the Equator southeast of Hawaii. There is also considerable similarity between the Japanese sample and the Hawaiian sample.

The sample from Angola, Africa, has so much overlap with some of the equatorial Pacific samples that the maximum amount of intermingling
might be large, but of course the geographic separation makes absurd the suggestion of any intermingling. In the case of the northeast Africa sample, both the markedly low overlap with all other samples and the geographic separation make the possibility of intermingling very small.

## GEOGRAPHIC DISTRIBUTION OF YELLOWFIN

One kind or another of yellowfin tuna, genus Neothunnus, has been described from each of the warm seas of the world except, the Mediterranean. Rosa (1950) has reviewed the extensive literature and noted that the distribution extends from Point Conception, California, to San Antonio, Chile, in the eastern Pacific; from Hokkaido, Japan, south through the Indonesian Archipelago to Cape Naturaliste, southwest Australia; around the shores of the Indian Ocean to the tip of South Africa; from French Equatorial Africa north to the coast of Portugal in the eastern Atlantic, and from Maryland in the United States south to the coast of Brazil in the western Atlantic. He also reported that yellowfin occur in the Red Sea, which is the warmest sea in the world, so the distribution extends from the warmest waters to those in the vicinity of latitudes $40^{\circ} \mathrm{N}$. and $40^{\circ} \mathrm{S}$.

To these coastwise records must be added the records of capture in the open Pacific far from land, as reported by Yōichi Yabuta in the Japanese atlas "Average Year's Fishing Condition of Tuna Longline Fisheries," from the exploratory fishing of POFI along the central and eastern Pacific Equator, in offshore records from the eastern Atlantic by Mather and Day (1954), and in the more recent unpublished records of the capture of yellowfin tuna in the open parts of the Gulf of Mexico and Caribbean Sea by exploratory fishing vessels. The Japanese atlas records the capture of yellowfin tuna along the Equator from longitude $170^{\circ} \mathrm{W}$. to the Philippines, thence northward at various places to as far as latitude $43^{\circ} \mathrm{N}$. along the coast of Japan, in all of the major seas of the southwest Pacific, and in the Indian Ocean in the vicinity of Sumatra and the Nicobar Islands.

This distribution corresponds quite closely to that of waters warmer than the $65^{\circ} \mathrm{F}$. isothere (line of equal warming) shown by Hutchins and Scharff (1947). Along the coast of Chile the limit is between the $65^{\circ} \mathrm{F}$. and the $60^{\circ} \mathrm{F}$. isotheres,
and in other areas the most poleward record is not quite to the $65^{\circ} \mathrm{F}$. isothere. Further, no temperature barrier exists between any of the populations of yellowfin, for there is a broad band of summer temperatures between $65^{\circ} \mathrm{F}$. and $70^{\circ} \mathrm{F}$. around the Cape of Good Hope between the Atlantic and Indian Oceans.

Within the broad range of this species, however, there are widely varying concentrations. Already mentioned is the concentration along the Pacific Equator, where the yellowfin occur in an east-west band, and the scarcity in the open ocean north and south of this band. They do, however, occur in concentrations in the vicinity of many islands, in the Coral Sea off Australia, and possibly in other places separated from this equatorial belt by a region of yellowfin scarcity. The small yellowfin, in particular, seem to be concentrated fairly close to the islands, because they are rarely seen or caught on the high seas. The persistence of groups of these yellowfin along the reefs of certain islands has led to commercial fishing for them by trolling, and many fishermen feel that such yellowfin populations are relatively static. Thus, concentrations of yellowfin may vary enormously in extent from the clearly continuous distribution along many thousands of miles of the Pacific Equator to perhaps a relatively isolated group around a coral atoll.

Despite the variations in abundance, their widespread occurrence in all tropical oceans, near land and far from land, indicates that yellowfin tuna belong to the pelagic fauna of the warm seas and not merely to local faunal areas.

## NOMENCLATURE

A great variety of scientific names has been assigned to yellowfin tuna in various parts of the world, and there has been no general agreement on the correct names to be assigned to the various species or subspecies. Rosa (1950) recognized three species: Neothunnus albacora (Lowe) 1839 of the eastern Atlantic Ocean, $N$. argentivittatus (Cuvier and Valenciennes) 1831 from the western Atlantic Ocean, and $N$. macropterus (Temminck and Schlegel) 1842 from the Pacific and Indian Oceans. Schaefer and Walford (1950) considered the Atlantic form to be $N$. albacora and the Pacific form to be $N$. macropterus. They designated a specimen from the Malabar coast of India as the lectotype of $N$. argentivittatus, and thus this
name clearly applies to the Indian Ocean form unless it is decided that the Indian Ocean form should be the same species as one with a prior name from another ocean. Later Ginsburg (1953) considered that the name Thannus albacares (Bonnaterre) 1788 was appropriate for the eastern Atlantic yellowfin, T. subulatus (Poey) 1875 for the western Atlantic yellowfin, T. catalinae (Jordan and Evermann) 1926 for the eastern Pacific yellowfin, and T. macropterus (Temminck and Schlegel) 1842 for the western Pacific yellowfin.

Rivas (1954: 316) referred in a footnote to Ginsburg's usage of T. albacares and accepted it as a valid name for all Atlantic yellowfin. Rivas (1961) reviewed the status of T. albacares again and opined that the various yellowfin populations from the Atlantic and the Pacific were not worthy of separate nomenclaturial recognition. He noted the widespread distribution in tropical waters and stated, ". . . it would seem therefore, that the yellowfin tuna represents a single pantropical species
. . . ."
The characters that almost all authors have used to distinguish the species have been length of the pectoral fin and height of the second dorsal and anal fins. Ginsburg (1953) admits that the differences between the tuna of the eastern Atlantic and Hawaii (which he calls western Pacific) are only of racial magnitude and do not warrant separate names. He retained the separate names because he considered that (1) specimens of the two populations had not been directly compared, (2) not all promising phases of the morphology had been studied, (3) the tuna inhabit totally different faunal areas, and (4) most authors have treated the populations as distinct species. He , therefore, considered it desirable to avoid the confusion of shifting names in and out of synonymy.

Schaefer and Walford (1950) considered the differences between the eastern Pacific and eastern Atlantic forms sufficient to warrant separate species pending more information on the variability within oceans as compared with the variability between oceans. This information is now at hand from our studies and it shows clearly that the entire range of variation which has heretofore been used to describe the species of yellowfin occurs within one continuous distribution of yellowfin along the Pacific Equator. In fact,
the differences between yellowfin from Costa Rica and from Angola (which Schaefer and Walford consider to be sufficient for a separate species) are much less than the differences between yellowfin from Costa Rica and the eastern Carolines. This difference between the Costa Rican and Caroline Islands yellowfin is far beyond the conventional level of a subspecific difference, but because of the clear evidence of continuous distribution and morphological gradients between these two areas the yellowfin from the two areas must be considered conspecific.

There also may be a similar cline across the tropical Atlantic. Ginsburg (1953) reviewed the scanty evidence which indicates that the western Atlantic form has longer second dorsal and anal fins than the eastern Atlantic form. If the cline is present, then the Atlantic forms, also, are conspecific.

If we add to this evidence the fact that the yellowfin is clearly a fish of the high seas and not restricted to any coastal faunal areas and the strong probability that the distribution is continuous in the oceans from the Pacific through the Indian to the Atlantic, all of the forms should be
considered conspecific. The confusion can best be settled by reducing them to one species.

There will remain, of course, the possibility that certain yellowfin populations may be distinct enough to warrant a separate specific or subspecific nome. This must be considered for the sample from northeast Africa oft Somaliland, in which the fins are shorter than any we have found in the Pacific. However, our sample is not good, and with the evidence of continuous distribution through the Indian Ocean it seems most probable that this group is not completely separated from other yellowfin populations. Futhermore, it occurs in one of the warmest parts of the ocean, where the yellowfin would be expected to be the most different in structure.

Settling the matter of the proper specific name is only part of the problem. The generic name is also in dispute. Fraser-Brunner (1950) and Ginsburg (1953) used Thunnus. rather than the long established generic name of Neothunnus. Godsil (1954) did not follow Fraser-Brunner but separated Thunnus, Neothumnus, and Parathunnus, principally on the basis of markings on the liver; however, he gives this problem of generic separation


Figure 22.-Figure of tuna from Sloane (1707) on which Bonnaterre's description (1788) was based.
little consideration. Fraser-Brunner . reduced Parathunnus and Neothumbus to subgeneric status on the principle that a generic name is intended to express relationship. It is not desirable to have a group of monotypic genera. There is now no evidence to indicate that these genera should be separate, and so I follow Fraser-Brunner and Ginsburg, who use Thumnus for the bluefin, yellowfin, bigeye, and albacore group.

The final question is which specific name is correct. Schaefer and Walford (1950) considered that T. argentivittatus (Cuvier and Valenciennes) $18: 31$ would have priority if only one species of yellowfin was recognized, but they did not discuss the merits of $T$. albacares (Bonnaterre) 1788. Ginsburg (1953) reviewed the question and concluded that the original figure of albacares, which shows the distinctive long second dorsal and anal fins of the yellowfin, must be considered a yellowfin even though the pectoral fin is too short. Bonnaterre's description of the yellowfin was based on a description and figure by Slome (1707) which I reproduce here in full (fig. 22).
The Sea hereabout is very well provided with Albacores, or Thynni, whose Description follows:

## ALBACORES DESCRIBED

This Fish was Five Foot long from the end of the Chaps to that of the Tail, the Body was of the make and shape of a Mackerel, being roundish or torose, covered all over with small Scales, White in some places, and Darker colour'd in others, there was a Line run along each side. The coverings of the Gills ot each side were made of two large and broad Bones covered with a shining Skin, the Jaws were about Six Inches long, having a single row of short strong sharp Teeth in them, and were pointed. The Eyes were large, and the Gills very numerous, behind which were a small pair of Fins. Post anum was a Foot long Fin, about Three Inches broad at bottom, and Tapering to the end. It had another on its Back answering that on the Belly, and from these were small Pinnula at every Two Inches distance to the forked Tail, which was like a New Moon falcated, before which on the Line of the two sides was a membranous thick horny Substance, made up of the Fishes Skin, stood out about three quarters of an Inch where it was highest, something like a Fin. It was about Three Foot Circumference a little beyond the Head, where it was thickest. The Eye was about an Inch and a half Diameter. The Figure of this Fish is here added, Tab. I. Fig. I. taken from a dried Fish, where every thing was perfect save the first Fin on the Back, which I suppose was accidentally rub'd off.

It is frequently taken by Sailers with Fisgigs or White Cloath, made like Flying-Fish, and put to a Hook and Line for a Bait; The Flesh is coloured, and Tasts as the Tunny of the Mediterranean, from whence I am apt to
believe it the same Fish. It is to be found not only about Spain, and in the way to the West-Indies; but in the SouthSeas about Guayaquil, and between Japan and New-Spain every where.

This is called Tunnyes of Oviedo fum. p. 214. Albicores of Terry, p. 9. Albocores of Mandelfo, p. 196. Dolphin or Tunin of Marten, Orcynus Rondelel, p. 249. Thunnus Gesner. 1158. Aldrovand. p. 307. Mus. srammerd. Raii. Hist. p. 176. Tab. M. I. Corett. Thynni S'pecies ejusd. $a p p . p .5 . \& 24$. Tab. 9. No. I. where the Figure seems not good. Thynnus Bellon. p. 106. Salvian. p. 124. An palamite of Oviedo Sum. p. 211? Guarapucu Brasiliensibus, an Cavala Lusitanis, nostratibus Coninghvisch. Marcgr. p. 178? Pif. Ed. 1658. p. 59? vel an. Curvata pinima ejusd. p. 150? Ed. 1650. p. 51? Tons of Escarbot Nova Francia, p. 35. du Raveneau de Lussan, p. 171. An Albacoretta Pis. Ed. 165s. p. 73? Toni di Fernan Colon vita di Christof. f. 29. An Ox-Eye of Anonymus Portugal. ap. Purchas, p. 1313? vel Toninas Ejusd. ib. p. 1314? Tunnies of Francis Gualle. Purchas, 806. Albacoras Ejusd. p. 446. Hakl. of Smith New-England, p. 227. of Galvanos Purchas, in $42^{\circ}$. North Lat. South-Seas, p. 1685. Ton ou tasard de Cauche, p. 138. An tonine Ejusd. p. 142? Ulasso a Tuny Fish of Duddeley. p. 576. Albacore of Ligon. p. 6. Abbeville. p. 30. An a Spanish Maequerel of Ligon? Albachores Pyrard. de Laval. p. 6. 137.

A tuna of the size of Sloane's specimen almost certainly must have been one of either the yellowfin or the bluefin group. A comparison of measurements of Atlantic bluefin, Angola yellowfin, and Sloane's figure (table 16) indicates that Sloane's figure is closer to the yellowfin than to the bluefin in all characters except length of the pectoral fin. Further, Sloane's figure was taken from a dried fish from which the first fin on the back was missing and his figure is a dorsolateral view instead of a lateral one. These facts explain most of the differences from an accurate sketch of a yellowfin, which include the shorter pectoral fin, shorter anal

Table 16.-Comparison of body proportions calculated from Sloane's figure of Albacore, yellowfin from Angola, Africa, and bluefin tuna from Cape Cod, Mass.
[Expressed as thousands of fork length]

| Character | Sloane's figure 1 | Yellowfin? | Atlantic bluefin ${ }^{3}$ |
| :---: | :---: | :---: | :---: |
|  | cm. | cm. | cm. |
| Fork length | 151 | 140 | 125. 7-131.4 |
| Head length | 212 | 258 | 284-294 |
| Length of pectoral fin | 135 | 256 | 197-216 |
| Height of second dorsal fi | 27 C | 249 | 132-145 |
| Height of anal fin. .-. . | 197 | 238 | 129-144 |
| Snout to insertion of- |  |  |  |
| First dorsal fin. | 190 | 280 | 306-318 |
| Second dorsal fin | 489 | 509 | 541-559 |
| Anal fin. | 580 | 559 | 606-621 |
| Ventral fins | 276 | 286 | 315-339 |

[^9]fin, more slender body, and first dorsal fin too far forward.

Therefore, I concur with Ginsburg and conclude that $T$. albacares (Bonnaterre) 1788 is a valid name for yellowfin tuna. It has priority and hence the appropriate name for a single worldwide species of yellowfin tuna is Thunnus albacares (Bonnaterre) 1785 .

## SUMMARY AND CONCLUSIONS

The study was undertaken in order to understand better the intermingling of the populations of yellowfin tuna and to distinguish the species.

Twenty-four samples of yellowfin tuna from the Pacific Ocean, one from the Atlantic off Angola, Africa, and one from the Indian off Somaliland are compared.

Regression statistics are used to control effect of size of fish in order to compare samples by each of ten characters. Seven of the characters are further used in a multiple character measure of overlap.

The regression equations used by Schaefer (1948) are used. These require log of fork length with log height of second dorsal fin and log height of anal fin, and log fork length with length of pectoral fin. All other characters approximate a linear relationship.

Neither linear, transformed linear, nor simple curvilinear regression equations are completely satisfactory for the full range of the data. Therefore, samples are divided into small fish, less than $80 \mathrm{~cm} . ;$ nedium, 80 to 120 cm .; and large, more than 120 cm . in fork length. Comparisous are made at $65 \mathrm{~cm} ., 100 \mathrm{~cm}$., and 140 cm ., respectively.

A cline, or character gradient, exists along the Pacific Equator from the eastern Pacific to the Caroline Islands. The yellowfin in the eastern Pacific have larger heads, slightly shorter pectoral fins, much shorter second dorsal and anal fins, and greater distances from snout to the insertion of first dorsal, second dorsal, ventral, and anal fins. They also have a greater body depth and a greater distance from the insertion of the ventral fins to the vent.

Most other samples were like some part of the cline. The sample from Angola, Africa, closely resembled the samples taken between Costa Rica and the Line Islands. The samples from Hawaii were quite like those taken between longitude $129^{\circ} \mathrm{W}$. and the Line Islands. The sample from

Japan was like the one from the Caroline Islands. The Bikini Island sample, however, was rather unlike the others but most similar to those from Japan and Hawaii. The Philippine sample was most like samples from the eastern Pacific and very different from the nearby Caroline Islands samples. Most diverse was the sample from Somaliland, which had especially short fins, deep body, and a long distance from the snout to the insertion of the ventrals.

The overlap of samples from along the Pacific Equator is inversely related to distance between samples. The average between samples taken 1,500 miles apart is less than 50 percent; 3,000 miles apart, less than 25 percent; and 6,000 miles apart, less than 6 percent. It is concluded that east-west migration is limited and that most yellowfin remain within a few hundred miles of where they occur as juveniles.

The multivariate analysis is evaluated. It is shown that overlap is greatly reduced by considering more than one character but that it is not worthwhile to use more than four characters.

The distribution of the yellowfin indicates that it belongs to the pelagic faunal group and not to coastal faunal groups. It occurs in all oceans, except the Mediterranean, in waters warmer than $65^{\circ} \mathrm{F}$. at the surface. No temperature barrier to movement of the yellowfin exists between the Atlantic and Indian or Indian and Pacific Oceans. The distribution is probably continuous although not uniform.

It is considered desirable to place all yellowfin tunas of the world in a single species because of the continuous distribution and because the full range of characters which have been used to distinguish species occurs in the series of samples from the Pacific Equator. The name should then be Thunnus albacares (Bonnaterre) 1788.

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My debt to the many people who have carefully measured thousands of tuna is detailed in a previous paper (Dung and Royce, 1953). The formidable task of analyzing the data has been accomplished almost entirely by Mrs. Dorothy D. Stewart, nee Dung. Joseph J. Graham, Garth I. Murphy, O. E. Sette, and A. L. Tester critically reviewed the manuscript.

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## APPENDIX

Table A-1.-Morphometric measurements of yellowfin tuna (mm.), from longline catches near the Equalor and longitude $110^{\circ}$ W., March 195.4

| Fork length | $\begin{gathered} \text { woight. } \\ (\mathrm{ib} .) \end{gathered}$ | Hend | Snout to insertion of- |  |  |  | Insertion of ventral fin to anterior edge of vent | Great-bodybodydepth | Length of pectoral fin | Height of- |  | Diamiris | Sex | Examiner |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | First dorsal fin | $\begin{aligned} & \text { Second } \\ & \text { dorssal } \end{aligned}$ fin | $\begin{gathered} \text { Anal } \\ \text { fin } \end{gathered}$ | $\begin{aligned} & \text { Ventral } \\ & \text { fin } \end{aligned}$ |  |  |  | $\begin{aligned} & \text { Second } \\ & \text { dorsal } \\ & \text { fin } \end{aligned}$ | $\begin{gathered} \text { Anal } \\ \text { fin } \end{gathered}$ |  |  |  |
| 764 |  | 217 | 243 | 416 | 454 | 238 |  | 188 | 207 | 98 | 99 | 33 | F | William F. Royce. |
| 800 | 2314i | 323 | 242 | 4330 | 479 | ${ }_{25}^{243}$ | ${ }_{235}^{249}$ | $\stackrel{214}{208}$ | 225 | 113 119 | 113 | 30 31 | $\frac{\mathrm{M}}{\mathrm{F}}$ | Do. |
| ${ }_{1051}$ |  | $\stackrel{38}{ }$ | -247 | 435 | 489 | ${ }_{319}$ | 235 | -378 | - | 190 | 119 | 35 |  | Do. |
| 1175 |  | 310 | 342 | 616 | 678 | 350 | 343 | 306 | 309 | 229 | 30.5 | 36 | F | Do. |
| 1180 |  | 309 | 334 | 605 | ${ }^{678}$ | 333 |  | 300 | 310 | 229 | 246 | 40 | F | Do. |
| 1206 |  | 308 | 341 | 627 | 689 | 344 | 353 | 293 | 322 | 218 | 213 | 34 |  | Do. |
| 1332 |  | 314 | 339 | 623 | 692 | 353 | -346 | 303 | 330 | 216 | 234 | 35 | F | Do. |
| 1283 |  | 325 | 359 | 661 | 733 | ${ }_{391}^{365}$ | . 377 | 311 <br> 348 | 330 | 376 <br> 363 | 239 | 36 40 | $\stackrel{\mathrm{F}}{\mathrm{F}}$ | H. So. Yuen. |
| 1412. 1446 |  | 350 | 387 <br> 417 | 735 | ${ }_{819}$ | 411 |  | ${ }_{375}^{348}$ | 341 | $3{ }^{368}$ | 465 | 41 | M | H. S. D. Huen. |
| 1449 - |  | 360 | 400 | 732 | 816 | 398 | 428 | 380 | 356 | 378 | 416 | 41 | M | William F. Royee. |
| 1465 |  | 367 | 394 | 779 | 819 | 404 | 421 | 362 | 3 sa | 396 | 381 | 44 |  | Do. |
| 1466 |  | 366 | 383 | 737 | 817 | 400 | 448 | 388 | 343 | 366 | 319 | 35 | M |  |
| 1476 |  | 379 369 | ${ }_{316}^{416}$ | 785 | 844 | 420 | 441 | 391 | 369 | 379 | 404 | 40 |  | H. S. H. Yuen. |
| 1480 |  | 369 388 3 | ${ }_{417}^{391}$ | 756 | 840 851 881 | 419 |  | 379 | 358 <br> 347 | 363 36 3 | ${ }^{393}$ | ${ }_{48}^{38}$ | $\underset{\mathrm{F}}{\mathrm{F}}$ | Do. |
| ${ }_{1525}^{1517}$ |  | 388 <br> 385 | 417 <br> 425 | 767 <br> 764 <br> 8 | 851 853 | ${ }_{430}^{431}$ | 445 | 382 <br> 398 | $\begin{array}{r}347 \\ 378 \\ \hline\end{array}$ | $\stackrel{362}{391}$ | 443 <br> 465 | 4 |  | Do. |
| 1531 |  | 404 | 445 | 781 | 858 | 454 |  | 417 | 371 | 446 | 512 | 42 | M | Do. |
| 1537 |  | 379 | 420 | 777 | 846 | 417 |  | 410 | 379 | 417 | 434 | 45 | $\stackrel{\text { M }}{ }$ | William F. Royce. |
| ${ }^{1567}$ | 165 | 387 | 439 | ${ }_{7}^{791}$ | 880 | 428 | 461 | 411 |  |  | 592 | 4 |  | H. S. H. Yuen. |
| 1603 1608 |  | 408 <br> 408 <br> 08 | 437 <br> 430 | 813 803 | 893 413 | 459 466 46 | 452 457 | ${ }_{417}^{420}$ | 367 <br> 358 | 506 <br> 458 | 10 <br> 543 <br> 10 | 4 |  | Do. |
| 1649 |  | 415 | 450 | 888 | 906 | 454 | 470 | 429 | 391 | 420 | 502 | 41 | M | Do. |
| 1850 |  | 435 | 457 | 838 | 908 | 472 | 453 | 427 | 375 | 477 | 362 | 40 | M |  |
| 1690 | 220 | 427 | 483 | 871 | 957 | ${ }_{41}$ |  | 454 | 406 | 640 | 716 | 40 | M |  |

${ }^{1}$ Frayed.
[Measured by A. Fraser-Brunner]

| Fork length | Weight (kg.) | Head length | Snout to insertion of- |  |  |  | Insertionof ventralfin toanterioredgeof vent | Greatest body depth | $\begin{gathered} \text { Length } \\ \text { of } \\ \text { pectoral } \\ \text { fin } \end{gathered}$ | Height of- |  | $\begin{aligned} & \text { Diam- } \\ & \text { cter of } \\ & \text { iris } \end{aligned}$ | Number of gill rakers | Sex | Montis of 19.53 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | First <br> dorsal fin | Second dorsal fin | Anal fin | $\begin{gathered} \text { Ventral } \\ \text { fin } \end{gathered}$ |  |  |  | Second dorsal fin | $\begin{aligned} & \text { Anal } \\ & \text { fin } \end{aligned}$ |  |  |  |  |
| 62.5 | 5. 25 | 18. 5 | 20.5 | 34 | 39 | 33 |  | 16.5 | 16.5 | 7 | 6.5 | 2.5 | $9+18$ | M | March. |
| 65. | 6.3 | 18.75 | 20 | 35.5 | 40 | 21.5 |  | 17 | 18 | 7. 25 | 7.5 | 3 | $8+20$ | $\mathbf{M}$ | February. |
| 65 | 6.4 | 19 | 21 | 36 | 40 | 21.5 |  | 17 | 18 | 8.5 | 8 | 3.5 | $9+18$ | F | January. |
| 65 | 6.4 | 19 | 21.5 | 36.5 | 39.5 | 31 |  | 17 | 17.5 | 9 | 9 | 3.5 | $9+18$ | F | February. |
| 67.5 | 6 | 19.5 | 20.5 | 37.5 | 42 | 23) |  | 17 | 18. 5 | 8.5 | 9 | 3 | $10+19$ | F | Do. |
| 68. | 6 | 19.5 | 23 | 38 | 43 | 20 |  | 17.5 | 18.5 | 8.5 | 9 | 3 | $10+19$ | F | January. |
| 69.5 | 6.4 | 20 | 21.5 | 38 | 42 | 20 |  | 18.5 | 19 | 9.5 | 10 | 3.25 | $10+21$ | M | February. |
| 70 | 5.6 | 20 | $\underline{9}$ | 41 | 44 | 23 |  | 20 | 19.5 | 8.5 | 8 | 3 | 8+20 | M | January. |
| 70. | 5.8 | 20 | 22 | 29 | 43 | 20 |  | 17.5 | 18 | 8.5 | 8 | 3. 5 | $10+18$ | F | March. |
| 70. | 7 | 20 | $\underline{9}$ | 29 | 43 | 23 |  | 17.5 | 18 | 8 | 8.8 | 3. 5 | $9+19$ | F | Do. |
| 70.5 | 5 | 20 | $\underline{8}$ | 39 | 42.5 | 23 |  | 18. 5 | 19 | 8.5 | 8 | 3 | $9+20$ | F | January. |
| 70.5 | 5.4 | 20. 5 | 22 | 38 | 42.5 | 23.5 |  | 18.5 | 18.5 | 8.5 | 8 | 3 | $9+20$ | M | Feliruary. |
| 70.5 | 5.8 | 20 | 23.5 | 39 | 43 | 23 |  | 19 | 20 | 9 | 8 | 3.5 | $9+20$ | F | January. |
| 71.5 | 7.8 | 20.5 | 22.5 | 39 | 43 | 23.5 |  | 19 | 18.5 | 8.25 | 9 | 3. 5 | $9+20$ | F | March. |
| 72 | 7 | 20.5 | 22.5 | 30.5 | 43 | 28 |  | 19 | 30 | 8 | 8.5 | 3.5 | $10+20$ | M | 10. |
| 73. | 8 | 20.5 | 22.5 | 38 | 45 | 24 |  | 19 | 19.5 | 10 | 10 | 3.25 | $9+20$ | M | 10. |
| 73 | 8 | 20.5 | 23 | 37.5 | 45 | 24 |  | 19 | 19. 5 | 9. 5 | 10 | 3.5 | $9+20$ | M | 10. |
| 73.5 | 7.3 | 20.5 | 93 | 39 | 44 | 23.5 |  | 19 | 19. 5 | 8.5 | 8.5 | 3 | $9+20$ | $\mathbf{F}$ | To. |
| 74 | 8 | 21 | 95 | 42 | 45 | 24 |  | 90 | 30 | 9 | 11 | 3.5 | $9+20$ | F? | February. |
| 74 | 8 | 21 | 24 | 41 | 45. 5 | 25 |  | 30 | 20 | 9 | 10 | 3.5 | $9+20$ | M | March. |
| 75. | 7.7 | 21.5 | 23 | 41.5 | 46 | 94 |  | 19.5 | 20 | 9.5 | 10 | 3. 5 | $9+19$ | F | Do. |
| 76. | 5.5 | 18.5 | 21 | 36 | 40 | $\underline{1}$ |  | 16.5 | 19 | 8 | 8. 25 | 3. 5 | $9+21$ | $\mathbf{M}$ | 170. |
| 76. | 6 | 18.5 | 91 | 35 | 40 | 21.5 |  | 16.5 | 13 | 8.5 | 8. 25 | 3.5 | $9+21$ | $\mathbf{M}$ | 1). |
| 76. | 9 | 22 | 94.5 | 42 | 46 | 25 |  | 20.5 | 21.5 | 10 | 11.5 | 3. 5 | $9+20$ | F | Do. |
| 77. | 5.5 | 19 | 21.5 | 36. 5 | 40.5 | 22 |  | 17 | 19 | 8 | 8.5 | 3.5 | $9+20$ | $\mathbf{M}$ | Do. |
| 80 | 10 | 23 | 24 | 42.5 | 49.5 | 26 |  | 29 | 20 | 11.25 | 12 | 3.5 | $9+20$ | F | Do. |
| 80 | 10 | 23 | 34 | 42.5 | 49 | 25 |  | 22 | 20 | 11 | 11.5 | 3. 75 | $10+20$ | F | Do. |
| 80 | 11 | 23 | 26 | 44 | 48.5 | 26 |  | 22 | 21.5 | 11 | 12 | 4 | 9+20 | F | Do. |
| 80 | 11 | 23 | 26 | 44 | 48 | 26 |  | 22 | 21.5 | 11 | 12 | 4 | $9+21$ | F | 10. |
| 80.5 | 10 | 22.5 | 25 | 44 | 48 | 26 |  | 21 | $\underline{20.5}$ | 9.5 | 10 | 4 | $9+21$ | F | Do. |
| 80.5 | 10 | 22.5 | 25 | 44 | 48 | 26 |  | 21 | 20 | 9.5 | 10 | 4 | $9+22$ | F | 170. |
| S1. | 10 | 23 | 25.5 | 44 | 47 | 25.5 |  | 21 | 21 | 9 | 11 | 3.5 | $8+20$ | $\mathbf{M}$ | 10. |
| 81. | 10 | 33 | 24 | 43 | 50 | $\underline{9}$ |  | 29. 25 | 20 | 11.5 | 12 | 3. 75 | $9+20$ | F | 10. |
| 81 | 10. 7 | 23 | 25, 5 | 44 | 47 | 25.5 |  | 21 | 21 | 0 | 11 | 3.5 | $9+30$ | $\mathbf{M}$ | Do. |
| 81.5 | 10 | $\underline{23}$ | 95 | 43. 25 | 44 | 37 |  | 20.5 | 22. 5 | 9.5 | 10 | 4 | 10-23 | F | Jo. |
| 81.5 | 10 | 24 | 26.5 | 44. | 49 | 25 |  | 22 | 20.5 | 9.5 | 12 | 3.5 | $10+21$ | F | 110. |
| $8{ }^{80}$ | 11.6 | 24 | 97 | 45.5 | 49 | 26 |  | 21.5 | 33.5 | 10.5 | 12.5 | 4 | $10+20$ | $\mathbf{M}$ | 130. |
| 89.5 | 10.5 | 22.5 | 24 | 43.5 | 46.5 | 24 |  | 23 | 22.5 | 12 | 14 | 3.5 | 9+20 | M | Do. |
| 83. | 11.5 | 23 | 25.5 | 44.5 | 50 | 26.5 |  | 22 | 21.5 | 11 | 12 | 3. 5 | $9+20$ | F | Do. |
| 83 | 11.7 | 23. 5 | 25. 5 | 44.5 | 50.5 | 26.5 |  | 21.5 | 21.5 | 11 | 11.5 | 3.5 | $9+20$ | F | Do. |
| 84 | 11. | 22.5 | 26. | 45 | 50 | 26.5 |  | 22.5 | $\underline{21}$ | 11 | 13 | 3.5 | $9+20$ | F | Do. |
| 84 | 11.8 | 38.5 | 35.5 | 44.5 | 50.5 | 23.5 |  | 21.5 | 21.5 | 11 | 11 | 3. 5 | $10+20$ | F | Do. |
| 84 | 12 | $\stackrel{24}{24.5}$ | 26.5 | 45 46 | 50 50 | 97 | ---------- | 23 | 21 | 11. | 12 | 4 | $10+20$ | $\mathbf{M}$ | Do. |
| 84 | 12.6 | 34.5 | 26 | 46 | 50 50.5 | 27 |  | 29.5 | 21 | 10.5 | 11.5 | 4 | $9+20$ | M | To. |
| 84.5 | 12 | 24.5 | 26 | 47 | 50.5 | 28.5 |  | 23.5 | 21 | 12.5 | 12.5 16.5 | 4. 25 3.5 | $9+21$ $8+20$ | ${ }_{\mathbf{M}}^{\mathbf{M}}$ | 130. |
| 84.5 | 12 | 23 | 28 | 45.5 | 50.5 | 23.5 |  | 22 | 21.5 | 11.5 | 11.5 | 4 | $9+21$ | M | Do. |
| 84.5 | 12.7 | 23 | 96 | 45. 5 | 50.5 | 20.5 |  | 22 | 23 | 11.5 | 11.5 | 4 | $8+21$ | M | $1) 0$. |
| 85.5 | 19 | 23.5 | 26.5 | 45 | 51 | 26 |  | 2n. 5 | 29 | 11 | 14 | 4 | $10+20$ | F | Do. |
| 86 | 12 | 23.5 | 27 | 45 | 49 | 26 |  | 23 | 22 | 11.5 | 10.5 | 4 | 8+21 | F | 10. |
| 86 | 13 | 24 | 27.5 | 46. 5 | 52.5 | 27.5 |  | 23 | 24 | 125 | 14 | 3.5 | $9+20$ | $\mathbf{M}$ | 10. |
| $86$ | 13 | 34 | 27 | 46.5 | 51 | 27.5 |  | 23 | 22 | 12 | 13 | 4 | $10+20$ | F | Do. |
| 87 | 13 | 24.5 | 26.5 | 45.5 | 50.5 | 26.5 |  | $\underline{23.5}$ | 22 | 12 | 12 | 4. | 9+50 | $\underset{\sim}{5}$ | Do. |
| 87 | 13.3 | 24.5 | 27 | 46 | 52 | 27.5 |  | 23 | 24.5 | 13 | 14.5 | 3.75 | $9+20$ | M | Do. |
| 89 | 14 | 26 | 28 | 48 | 52 | $\stackrel{\mathrm{ng}}{ }$ |  | 24 | 33 | 13.5 | 15 | 4 | $8+20$ | F | Do. |
| 105.5. | 22 | 28 | 31.5 | 56 | 61 | 31.5 |  | 27 | 20 | 16 | 18 | 4 | $9+20$ | $\mathbf{M}$ | Do. |

Note.-Data furnished through the courtesy of G. L. Kesteven, Fisheries Division, U.N. Food and Agriculture Organization. Measurements were recorded in half or quarter centimeter units identifed by the upper limit of each unit; thus are $1 / 8$ to 14 em. too great.

Table A-3.-Regression statistics of yellowfin tuna samples
 mean $\overline{y ;} b=$ regression coefficient; $a=$ constant in regression equation; $s=$ standard deviation from regression (cm.); $\hat{\mathbf{r}}=$ estimated character size (cm.) at standard comparison length of size group (cm. except for logarithums which have characteristies for mn.)]

| Character and size group 1 | $N$ | SX | $s Y$ | Sx: | SY ${ }^{2}$ | SXY | Sr ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $X=$ fork length: $Y=$ head length: |  |  |  |  |  |  |  |
| Costa Rica: ${ }^{2}$ M $M$------------- | 29 | 2.504 .5 | 789.9 | 292, 493. 79 | 21,688.87 | 79, 225.88 | 3, 198.3676 |
| $109^{\circ}-119^{\circ} \mathrm{W} .: ~ L$ | 21 | 3, 146. 2 | 797.0 | 475,009. 34 | 30, 504. 64 | 120,353. 63 | 3. 648.6524 |
| $119^{\circ}-129^{\circ} \mathrm{W} .: L$ | 47 | 6, 895.8 | 1.739. 1 | 1, 016, 781.01 | 64, 638.71 | 256, 300.39 | 5,005.7588 |
| $129^{\circ}-139^{\circ} \mathrm{W} .: L$ | 46 | 6,6677.6 | 1.680. 6 | , $988,059.18$ | 62,520.78 | 248, 469.53 | 21, 605.0548 |
| $139^{\circ}-149^{\circ} \mathrm{W}: L$ | 111 | 16, 507.1 | 4,150.5 | 2, 468, 765.29 | 156,032. 57 | 620, 546. 47 | 13,951. 3223 |
| East Line Islands: |  |  |  |  |  |  |  |
| $\underline{L}$ | 155 | 22,524. 5 | 5,631.8 | 3, 288, 056.75 | 205,433. 66 | 821, 786. 68 | 14. 810.9420 |
| West Line Islands: |  |  |  |  |  |  |  |
| S | 43 | 2.954. 4 | 849.3 | 205, 448.86 | 16, 039. 55 | 58,973.52 | 2, 460.9680 |
| $\boldsymbol{M}$ | 86 | 8, 407.2 | 2.288 .3 | 832, 615. 32 | 61.334. 71 | 225, 881.31 | 10.743. 0894 |
| $L_{\text {L }}$ | 57 | 7.876.2 | 1.998. S | 1,094, 133. 62 | 70.433.44 | 277.547.24 | 5. 808.5948 |
| Palmyra Island: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |
| M | 57 | 5, 379.7 | 1, 446.6 | 511, 367.03 | 36, 886. 28 | 137, 303. 18 | 3, 627.1688 |
| Phoenix Islands: |  |  |  |  |  |  |  |
| S.----------- | 37 | 2, 503.6 | 715.2 | 171, 117. 96 | 13, 927. 34 | 48.793. 54 | 1,712.2044 |
| $M$ | 59 | 5,795. 3 | 1,559.6 | 576, 982.99 | 41. 586.04 | 154, 811. 32 | 7.737. 1918 |
| L | 46 | 6, 142. 5 | 1, 139.6 | 836, $866 \mathrm{B}$. | 52,633.16 | 209, 836.18 | 16.942. 3411 |
| East Marshall Islands: $L$ | 40 | 5,453.4 | 1,359.8 | 746, 253. 02 | 40,398. 12 | 186, 058.56 | 2. 763.7310 |
| Blaini Islapd: S--- | 31 | 1,829.9 | 520. 9 | 109, 843.77 | 8.859.57 | 31, 185.95 | 1, 526.5439 |
| East Caroline Islands: |  |  |  |  |  |  |  |
| M | 50 | 5. 5104.4 | 1.411.5 | 539.53320 | 36. 60289 | 140, 475.74 | 3,559,8619 |
| $L$ | 54 | 7.516.0 | 1,372.4 | 1,052.115.44 | 65, 213. 40 | 261,801. 54 | 5, 5989.5882 |
|  |  |  |  |  |  |  |  |
| S- | 37 | 2,513.9 | 698.9 | 173.346. 55 | 13. 385.38 | 48.132. 23 | 2. 544.0309 |
| $\boldsymbol{M}$ | 102 | 10,289. 2 | 2, 773.5 | 1, 049, 698. 10 | 70.639. 51 | 272, 240.75 | 11,780. 0938 |
| $L$ | 69 | 9,125.8 | 2,287. 5 | 1, 211, 068. 54 | 76. 126.13 | 303, 577.84 | 4. 109. 7482 |
| Philippines (SW. Panay): |  |  |  |  |  |  |  |
| $\cdots$ | 81 | 7, 349.8 | 1,993. 6 | 674, 62]. 22 | 49, 439.00 | 183, 526. 67 | 7,713.0714 |
| $L_{\text {L }}$ | 32 | 4.334. 2 | 1,085. 1 | 562. 353. 60 | 36,983. 97 | 144,065.00 | 2,089.548s |
| Japan: S | 31 | 1.789 .5 | 505.7 | 108, 296. 33 | 8, 686. 13 | 30, 660. 85 | 4.905.9994 |
| Hawaii: ${ }_{\text {c }}$ |  |  |  |  |  |  |  |
| $S_{\text {S }}$ | 36 | 1,884. 6 | 534.2 | 100.518.50 | 8,061. 62 | 28,461.45 | 1,859.6900 |
| $\stackrel{M}{L}$ | 34 | 3.466. 4 | 913. 2 | 356. 040.12 | 24,6fi 30 | 93.673. 95 | 2; 630.4448 |
| L----- | 133 | 19.955. 4 | 4.929. 5 | 3,028.042. 30 | 184.479. 19 | 747. 259.96 | 33;922. 0808 |
| Hawaii: ${ }^{\text {a }}$ | 47 | 2,679.3 | 762.9 | 153.111. 13 | 12,412. 53 | 43, 589.67 | 373.9281 |
| L | 20 | 2,859. 2 | 714.2 | 400, 803.42 | 25, 588.64 | 102,393.11 | 1,062. 1880 |
| Society Islands: S. | 17 | 988.5 | 234.4 | E8, 503.31 | 4, 827.06 | 16, 801.56 | 1. 024.0424 |
| Northeast Africa: | 48 | 3,805.0 | 1,077.3 | 304, 447.00 | 24, 35i. 69 | 86, 085.00 | 2,821.4792 |
|  |  |  |  |  |  |  |  |
| $L_{\text {L }}$ | 27 | 3.717.0 | 961.3 | 515, 125. 62 | 34, 411.43 | 133, 110.49 | 3, 418.6200 |
| $\mathbf{F = \text { pectoral fin lengtlu: }}$ |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| $109^{\circ}-119^{\circ} \mathrm{W} .: ~ L$. | 21 | 66. 650 | 758. 0 | 211. 5663268 | 27, 490.42 | 2, 407.5185 | . 031863 |
| $119^{\circ}-123^{\circ} \mathrm{W} .: ~ L$ | 46 | 154.626 | 1.680. 7 | 461.064214 | 61, 652. 59 | 5, 329.2928 | . 043956 |
| $129^{\circ}-139^{\circ} \mathrm{W} .: L$ | 46 | 145. 115 | 1.650. 4 | 458. 098769 | 60. 123. 18 | 5, 222. 2368 | . 308285 |
| $139^{\circ}-149^{\circ} \mathrm{W} .:$ L | 113 | 358.339 | 4,216. 1 | 1, 1315. 467083 | 157.63b. 55 | 13.374.0386 | . 123376 |
| East Line Islands: |  |  |  |  |  |  |  |
| $\boldsymbol{M}$ | 32 | 96.263 | 917.8 | 289.652424 | 213. 501.70 | 2. 764.9444 | . 054713 |
| West Line Islands: |  |  |  |  |  |  |  |
| $\stackrel{S}{\text { S }}$ | 43 | 121.882 | 874.9 | 345. 577724 | 18.022. 45 | 2, 484.4753 | . 107447 |
| ${ }_{\mathbf{M}}^{\mathbf{L}}$ | 86 | 256.925 | 2,418. 1 | 767.775975 | 88, 804.05 | 7,236. 1381 | . 212538 |
| Phoenix İlands: | 56 | 175.831 | 2,030.0 | 552.137153 | 73, 803. 70 | 6, 376.5446 | . 0 Eibl 72 |
| Phoenix Islands: |  |  |  |  |  |  |  |
| $\boldsymbol{\lambda}$ | 58 | 173. 201 | 1,646. 1 | 517.898774 | 50. 125. 13 | 5.075.4469 | . 144109 |
| $L$. | 40 | 143.943 | 1,643.0 | 450.460353 | 58.862. 76 | 5, 142. 9820 | . 034544 |
| East Marshall Islands: $L$ | 40 | 185. 349 | 1,441.5 | 392. 839943 | 52.058. 77 | 4. 518.3836 | . 029948 |
| Bikini Island: | 31 | 85.798 | 558.8 | 237.546178 | 10,226, 10 | 1.550.0649 | . 084981 |
| East Caroline Islands: |  |  |  |  |  |  |  |
| N | 53 | 158.390 | 1,568. 3 | 473. 5000596 | 25, 984.71 | 3, 491. 4148 | . 153576 |
| $L$ | 53 | 173.007 | 2,023.5 | 544. 271157 | 74, 624. 13 | B, $367.61 \mathrm{b4}$ | . 0633484 |
| Central Caroline Islands: |  |  |  |  |  |  |  |
| S | 36 | 101. 854. | 778.3 | 288.288240 | 17, 128. 15 | 2,207. 7750 | 114982 |
| $\stackrel{M}{L}$ | 102 | 308.117 | 3.125. 4 | 918.930709 | 90. 471.08 | 9,391. 1201 | . 223635 |
| L_--1 Japarn | 72 | 224.688 | 2, 576. 1 | 701. 22.2332 | 92.354 .33 | $8,040.8810$ | . 054880 |
| Japan: S- | 30 | 82.441 | 515.3 | 226. 832298 | 9.385. 21 | 1,425.2000 | . 281682 |
|  |  |  |  |  |  |  |  |
| M | 34 | 102. 230 | 990.4 | 307.429448 | 29.046 .30 | 2,980.3773 | . 047893 |
| $L$ L | 133 | 42.105 | 5.032. 9 | 1.339. 929970 | 191.379.69 | 15,986. 6720 | . 286128 |
| Society Islands: S $^{\text {d }}$ | 21 | 57.897 | 374.4 | 159.676581 | 6,854.34 | 1,035. 2576 | . 054552 |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| $L$ | 27 | 84.710 | 953.7 | 265. 790772 | 33, \$30. 51 | 2.983. 9101 | . 029991 |

See footnotes at end of table.

Table A-3.-Regression statistics of yellowfin tuna samples-Continued


[^10]Table A-3.-Regression statistics of yellowfin tuna samples-Continued

| Cbaracter and size group ${ }^{1}$ | $N$ | $s \mathrm{~S}$ | SI | SX ${ }^{2}$ | $S \mathrm{Y}^{-9}$ | SxY | Sis ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| East Marshall Islands: $L_{\text {- }}$ | 30 | 5.310.9 | 1,461.4 | 725,946. 77 | 54, 957. 40 | 199,720.51 | 2,724.7493 |
| Bikini Island: $S$ Sast Caroline Islands: | 31 | 1,829.9 | 560.6 | 109,843.77 | 10,254, 82 | 33, 547.13 | 1,826. 5439 |
| S | 59 | 3, 841. 4 | 1,189.4 | 356, 189.28 | 24, 2033.44 | 78,707.02 | 3,450.4672 |
| M | 55 | 5,404.4 | 1, 660.8 | 539, 532. 20 | 44.782 .08 | 155, 380. 36 | 8.486. 0298 |
| $L_{\text {L }}$ | 56 | 7,837.2 | 2,150.0 | 1,103,798. 16 | 83,008. 82 | 303, 614.71 | 6,88. 02200 |
| Central Caroline islands: | 35 | 2,378.7 | 729.8 | 163, 886. 53 | 15, 390.80 | E0, 295.33 | 2, 393.2818 |
| M | 102 | 10,289.2 | 2.955.1 | 1,049,698. 10 | 86, 320.21 | 300. 905.71 | 11.780.0938 |
| L | 71 | 9,404.3 | 2,587. 7 | 1,249.939. 11 | 95, 321.55 | 345.077.67 | 4, 293.2158 |
| Phillpphes (SW. Panay): | 242 | 15,776.4 | 5,121.5 | 1.040, 719.56 | 109, 406.73 | 337, 258,66 | 12.228. 6635 |
| AI | 81 | 7.349 .8 | 2, 3 23. 5 | 6774.621.22 | 61.959.87 | 204, 321.76 | 7.713.0714 |
| $L$ | 33 | 4,388.7 | 1,243.0 | ${ }^{586,233.85}$ | 47,014. 72 | 165. 933.26 | 2. 566.6473 |
| Japanis | 31 | 1,759.5 | 564.0 | 108, 296. 33 | 10, 885.40 | 33,999. 64 | 4, 995.9994 |
| Hawaii: |  | 1,884.6 | 601.8 | 100, 518.50 | 10. 334.96 | 32,067. 13 | 1,859.6900 |
| $\cdots$ | 34 | 3,466. 4 | 1,015. 2 | 356\%, 040.12 | 30. 484.58 | 104, 134.53 | 2,630.4448 |
| $L$ | 131 | 19.610. 4 | 5,379.7 | 2, 968, 469.30 | 222, 997. 89 | 813, 401. 91 | 32, 837. 3299 |
| Hawailis |  |  |  | 153,111.13 | 14.856. 44 | 47, 686. 86 | 373.9281 |
| L | 20 | 2,859.2 | 794.0 | 409.803. 42 | 31, 624.14 | 113,819.11 | 1,052. 1880 |
| Society Islands: $S$ | 22 | 1, 260. 6 | 400.2 | 73. 377.44 | 7. 3715.30 | ${ }^{23.254 .99}$ | 1. 145.0660 |
| Northeast Africa: $\mathbf{S}$ | 48 | 3. 8105.0 | 1,189.5 | 304, 447.00 | 29,713.75 | 95,067.25 | 2.821. 4782 |
| Angola, Atrioa: ${ }_{\text {M }}$ |  |  |  | 206, 277, 69 | 17,860. 48 |  | 6,061.0115 |
| L-.....------- | 27 | 3,717.0 | 1,042.7 | 515, 125. 62 | 40, 514. 29 | 144, 427.97 | 3.418.6200 |
| =snout to insertion second dorsal in: |  |  |  |  |  |  |  |
| Costa Rica: ${ }^{2}$ M | $\stackrel{29}{29}$ | $\frac{2,8196.5}{3,146.2}$ | 1,527.6 | 292, 493. 79 $\mathbf{4 7 5 , 0 0 9 . 3 4}$ | $\$ 1.184 .30$ | 154,073. 13 | 3, 193.3676 |
| $119^{\circ}-129^{\circ} \mathrm{W} .: L$ | $4{ }^{4}$ | 6,470.7 | 3,255.0 | 956. 166.11 | 941, 933.41 | 480, 926.32 | 4,576. 1444 |
| ${ }^{1299^{\circ}-139^{\circ} \mathrm{W}} \mathrm{W}^{\text {a }}$ L | 46 | 6, 6678. ${ }^{6}$ | 3.364. 6 | 938, 059.18 | ${ }^{2} 250,539.34$ | 497.756.66 | 21,605.0548 |
| 139 ${ }^{13}{ }^{\circ}-149^{\circ} \mathrm{W}$ W.: $L$ L-: | 112 | 16, 666.4 | 8.371.8 | 2, 494, 141.78 | 629, 133.06 | 1,252, 559.93 | 14, 062.4142 |
| East Line islands: |  | 3,382.8 | 1,739.9 | 348,710.50 | 92,411.97 | 179,750.04 | 2,942. 7473 |
| L | 155 | 20, 517.15 | 11, 245.8 | 3, 265, 363.6. | 819, 6167.82 | 1,641, 017.17 | 15, 142.9719 |
| West Line islands: |  | 2947.4 |  | 204.508. 51 | 59,288.09 | 110,045.93 | 2, 430. 8261 |
| M | 88 | 8,394.8 | 4,337.7 | 836,038. 12 | 2ni,074.05 | 428, 290.45 | 10, 586.5033 |
| L----------- | $5{ }^{5}$ | 7,732.7 | 3.868.1 | 1.073, 541.37 | 268, 490.83 | 538, 807. 26 | 5,779.7756 |
| Palmyra island: ${ }^{\text {a }}$ | 34 |  |  | 180, 100.01 | 52, 130.85 | 96, 888, 92 |  |
| M | 57 | 5,379.7 | 2,796. 1 | 511,367.03 | 137.936. 41 | -265, 548.40 | 3. 627.1688 |
| Phoenix islands: |  |  |  |  |  |  |  |
| M | 39 59 | 2, $5,793.6$ | -1,947.6 | 576,988.99 | 151, 964.35 | 295, 9888.88 | 7,737.1919 |
| $L$ | 46 | 6,907. 1 | 3,110.9 | 841,039.55 | 211, 181.35 | 421, 398.64 | 3. 473.3672 |
| East Marshall Islands: | 39 | 5.321.7 | 2.675.8 | 738, 908. 13 | 154, 225. 62 | 366, 486.68 | 3, 741.6970 |
| Bikini Lsland: S-... | 31 | 1,829.9 | 983.7 | 109, 843.77 | 32,271.29 | 59, 529.17 | 1,826.5439 |
| East Caroline Islands: |  |  |  |  |  | 136,067. 48 | 3. 513.4455 |
| M | 55 | 5,404.4 | $2,764.7$ | 539, 533.20 | 140,667. 69 | 275. 442.73 | 8. 486.0298 |
|  | 56 | 7,837.2 | 3,881.4 | 1,103,798.15 | 270, 556. 54 | 546, 441.15 | 6,989.0200 |
| Central Caroline Islands: |  | 2. 513.9 | 1,344.8 | 173.346.55 | 49, 485. 68 | 92, 604.46 | 2,544.0309 |
| M | 101 | 10, 183.7 | 5,180.5 | 1,038, 567.85 | 268, 193.53 | 587, 681.15 | 11,76S. 4870 |
|  | 68 | 8,907.1 | 4,472.9 | 1, 194, 303.33 | 295, 159.21 | 598, 660.64 | 3. 894.3828 |
| Philippines (SW. Panay): |  |  |  | 1,036, 546. 40 | 332, 391.36 |  | 12.238. 3119 |
| M |  | 7,349.8 | 3,996. 1 | 1,674, 621. 22 | 1988.764. 79 | 366, 0177.21 | 7.713. 0714 |
| L | 2 | 3,713.5 | 1,925.6 | 494,392. 59 | 132, 923.10 | 256, 315. 20 | 1.859.6535 |
| Japan: | 31 | 1,789.5 | 979.4 | 148, 246.33 | 32. 243.84 | 59,082. 02 | 4,995.994 |
| Hawaii: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |
| ${ }_{\text {S }}$ | 36 36 | 1.884.6 | 1,041.4 | 100,518. 50 | 30,637.02 | 55.486.52 | 1,859.6900 |
| M | ${ }^{34}$ | 19.466.4 | $1,8180.3$ 9.852 .0 | 2, 2966 , 3588.30 | 742, 617.40 | 184.731 .82 $1.491,51.29$ | 33.134.4306 |
| Hawail: ${ }^{\text {a }}$ | 132 | 19,777.4 | 9,85..0 | 2, 996, 358.30 | 74.67 .30 | 1.491,51..33 |  |
|  | 47 | 2.679 .3 | 1.463.S | 153, 111. 13 | 45, 690.50 | 83, 635.85 | 373. 9281 |
| L | ${ }_{20}^{20}$ | 3,359. ${ }^{2}$ | 1.437.6 | 409, 803.42 | ${ }_{\text {10, }}^{103,834.86}$ | 206, 068.57 | 1, 165.1880 |
| Society islands: $S$ | ${ }_{46}^{21}$ | 1.209.3 | 1665.7 | 70.745.75 | - 81.36750 .69 | $38,87.54$ 158.920 .80 | 2,642. 1087 |
| Northeast Africa: ${ }^{\text {Angola, Arrica: }}$ | 46 | 3.6i5.0 | 1.878.2 | 294, 847.00 | 85.750 .74 | 158,920.80 | 2,642. 108 |
| M | 21 | 2,050.5 | 1,089.0 | 206, 277.69 | 57.699.46 | 109, 041.36 | 6, 061.0115 |
|  | 27 | 3,717.0 | 1.892.8 | 515, 125. 62 | 133.489.44 | 202, 908.21 | 3, 418.6200 |
|  | 29 | 2, 896, 5 |  |  | 101,685. 80 | 172.442. 86 | 3. 193.3676 |
| $109^{\circ}-119^{\circ}$ W.: $L$ | 21 | 3.146. 2 | 1,766. 2 | 475, 009. 34 | 149, 575.84 | 266, 533.77 | 3. 648.6524 |
| ${ }^{119^{\circ}-129^{\circ} \mathrm{W}}{ }^{\text {W }}$ - ${ }^{\circ} \mathrm{L}$ | 47 |  |  | 1,018. 7881.01 | 312.644 .10 <br> 305 <br> 168.85 | 563, 751.14 540. 03723 |  |
| $139^{\circ}-149^{\circ}$ W:: $L$ | 113 | 16.807.0 | 3, $4,330.2$ | 2,513.910.14 | 774, 456.14 | 1,395, 190.05 | 14, 129.1754 |
| East Line Istands: |  |  |  |  |  |  |  |
| ${ }_{L}$ | 153 | 23, 2398 | 1.869 .7 $12,270.3$ | 3, $347,595.60$ | 110,060.09 988, 18. 19 | 1.791, 256.16 | 14, 858.9724 |
| West Line Islands: |  |  |  |  |  |  |  |
| M |  | 3, 956.6 | $1,750.1$ 4 486.3 | $205,741.90$ $832,220.21$ | 71,942, 63 | ${ }^{121.639 .515}$ | ${ }_{10}^{2,451.5847}$ |
|  | 56 | 7,724.0 | 4,236.3 | 1,070,968. 78 | 329, 570.95 | 594, 558.0 | 5,608. 4943 |
| Palnyra Island: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |
| M | 57 | 5.379 .7 | 3,069.5 | 511, 367.03 | 166, 188.61 | 291.470. 97 | 3.627. 1688 |
| Phoenix Islands: |  |  |  |  |  |  |  |
| M | 5 | $\stackrel{\text { 2, }}{5697.8}$ | 1.4.289.9 | 567, 476.74 | 181,786. 19 | 321. 112.35 | 7.736.6566 |
| L. | 45 | 6.078. 7 | 3. 350.5 | 824, 552.99 | 250.433.17 | 464, 396. 25 | 3. 428.6858 |

YELLOWFIN TUNA

Table A-3.-Regression statistics of yellowfin tuna samples-Continued

| Character and size group ${ }^{1}$ | $N$ | SX | SY | SX ${ }^{\text {a }}$ | $S Y^{2}$ | SXY | $S r^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| East Marshall Islands: $L_{\text {- }}$ | 40 | 5.453.4 | 3.002. 7 | 746, 253.02 | 226, 261.25 | $410,890.35$ | 2,763.7310 |
| Bikini Island: S-..-.-.-. | 31 | 1, 529.9 | 1,024.9 | 109,843. 77 | 39, 177.77 | 65, 588.67 | 1,826.5439 |
| East Caruline Islands: | 30 | 3.916. 3 | 2,302. 4 | 259, 183. 29 | 89.401. 86 | 152. 204.64 | 3. 559.8619 |
| M | 54 | 5,312.8 | 2. 282.3 | 531, 141. 64 | 166.751. 45 | 297. 575.13 | 8. 440.8282 |
| $L$. | 55 | 7,682. 1 | 4,195. 5 | 1,079, 742.15 | 321.854. 99 | 589,467. 25 | 6.748. 3344 |
| Central Caroline Islands: |  |  |  |  |  |  |  |
| S | 37 | 2, 513.9 | 1. 489.0 | 173.346. 55 | 60. 687.04 | 102, 546. 64 | 2,544.0309 |
| M | 102 | 10.289.2 | 5.796. 7 | 1.049. 688. 10 | 332, 230. 77 | 590. 407.37 | 11.780. 0938 |
| L | 68 | 8,977. 3 | 4,940.0 | 1.189,017. 29 | 360, 056. 26 | 654, 229. 69 | 3. 842.0652 |
| Philippines (SW. Panay): | 242 | 15, 776. 4 | 9, 798.3 | 1,040, 719.56 | 4(0), 472. 31 | 645, 393.74 | 12.228. 6635 |
| M | 81 | 7, 349.8 | 4. 391.4 | 1. $674,621.22$ | 240, 101.84 | 402, 363. 09 | 7,713.0714 |
| $L$ | 31 | 4, 109.1 | 2,351. 4 | 546, 703. 59 | 178, 857. 86 | 312. 602.05 | 2, 035.7575 |
| Japan: S- | 31 | 1.789. 5 | 1,071. 4 | 108, 296.33 | 38, 581.78 | 64, 628.88 | 4.995.9894 |
| Hawaii: ${ }^{2}$ |  |  |  |  |  |  |  |
| $\stackrel{S}{M}$ | 36 34 | 1,884.6 | $1,144.4$ $1,988.6$ | 100, 515.50 | 36,977.80 | $60,956.99$ 904.081 .16 | 1, 8539.6900 |
| $L_{\text {L }}$ | 132 | 19,809.0 | 10,946.0 | 3, 006, 609. 34 | 916.354. 34 | 1,659,647.04 | 33,903. 7264 |
| Hawaii: 3 |  |  |  |  |  |  |  |
| S | 47 | 2, 679.3 | 1,613. 8 | 153. 111. 13 | 55.536. 18 | 92, 207.49 | 373.9281 |
| L---- | 20 | 2, 859.2 | 1, 599.7 | 409.803. 42 | 128, 289.01 | 229.277. 36 | 1. 052. 1880 |
| Northeast Africa: $S$ | 47 | 3,723.5 | 2,236. 5 | 297. 804. 75 | 107. 216.25 | 178.643. 00 | 2.816.4043 |
| Angoln, Africa: ${ }_{\text {M }}$ | 21 | 2,050. 5 | 1, 196.7 | 206, 277. 69 | 69, 700.95 | 119, 863.37 | 6,061. 0115 |
| $L$ | 26 | 3, 559.3 | 1,994. 1 | 490, 25ib. 33 | 153, 727. 89 | 274, 493.04 | 3. 001.8497 |
| $119^{\circ}-129^{\circ} \mathrm{W} .:$ L | 47 | 8, 895.9 | 1,929.5 | 1,016,7S1. 01 | 79,629. 77 | 284, 429.37 | 5,005. 7588 |
| $129^{\circ}-139^{\circ} \mathrm{W}$.: $L$ | 46 | 6. 6667.6 | 1, 867.5 | 988,059. 18 | 77, 173. 33 | 276.043. 66 | 21, 605. 0548 |
| $139^{\circ}-149^{\circ} \mathrm{W}:$ L $L$ | 113 | 18.807. 0 | 4.698.3 | 2, 513, 910. 14 | 195, 546.89 | 700, 965.38 | 14, 129.1754 |
| East Line Islands: | 31 | 3,183. 1 | 955.3 | 329. 762.05 | 29,610. 51 | 9S, 779, 60 | 2, 919. 2884 |
| $L$ | 153 | 22, 222.4 | 6, 212.5 | 3.242. 746.86 | 253, 634. 17 | 900, 612. 53 | 15.066. 7178 |
| West Line Islands: |  |  |  |  |  |  |  |
| $S^{\text {S }}$ | 42 | 2.889.5 | 923.4 | $201,158.85$ | 20, 499.36 | 64. 190. 27 | 2. 368.1298 |
| M | 84 | 8.216.6 | 2.495 .6 | 814, 259. 78 | 74.868. 24 | 246, 773. 28 | 10.539.3567 |
| $L$ | 56 | 7,735. 2 | 2,217. 1 | 1.074. 252. 62 | 88, 196. 69 | 307, 744.22 | 5. 800. 4943 |
| Palmyra Island: ${ }^{3}$ |  |  |  |  |  |  |  |
| $\stackrel{S}{\mathbf{M}}$ | 35 67 | 2,537.2 5,379.7 | 799.1 $1,598.4$ | 184.770 .90 $511,367.03$ | 18.312 .33 $45,029.14$ | 588, 159.51 | $\begin{array}{r} 845.6475 \\ 3,627.1688 \end{array}$ |
| Phoenix Islands: |  |  |  |  |  |  |  |
| S | 35 | 2. 383.6 | 757.8 | 163, 903. 38 | 16, 512.23 | 51, 994. 83 | 1,573.4098 |
| M | 56 | 5. 535.9 | 1,663.0 | 554. 436.73 | 49,892. 82 | 166, 246.01 | 7, 183. 3584 |
| $L$ | 46 | 6, 207.1 | 1.738. 5 | 841, 039.55 | 65.959: 63 | 235, 434. 15 | 3, 472. 3672 |
| East Marshall Islands: | 38 | 5,180. 2 | 1,434.9 | 708, 885. 88 | 54.390. 23 | 196. 334.36 | 2, 715.5633 |
| Bikinl Island: $\mathrm{S}^{\text {. }}$ | 31 | 1,829.9 | 587.3 | 109, 843.77 | 11.263. 09 | 35, 156. 10 | 1, 826. 5439 |
| East Caroline Islands: |  |  |  |  |  |  |  |
| S | 60 | 3.916. 3 | 1,216.9 | 259, 183. 29 | 24,959. 13 | 80.411. 50 | 3. 559.8619 |
| $M$ | 54 | 5,311.8 | 1,546. 5 | 530, 657.44 | 44.777. 35 | 154, 125. 35 | 8,453.3800 |
| L------------- | 55 | 7, 685.0 | 2, 136. 2 | 1, 080, 633. 32 | 83, 369. 00 | 300, 077. 18 | 6;829. 2291 |
| Central Caroline Islands: | 36 | 2.459.9 | 771.5 | 170.430. 55 | 16.747. 37 | 53, 398.72 | 2,344. 9164 |
| M | 101 | 10, 204.4 | 2.979.7 | 1,042, 507. 06 | 88. 623.57 | 303, 814. 74 | 11,519.1456 |
| $L^{2}$ | 68 | 8.958. 5 | 2,533. 2 | 1,184, 125. 53 | 94, 729.64 | 334, 759. 16 | 3, 909.0264 |
| Plilitppines (SW. Panay): | 241 |  | 5,088.9 | 1.035.302. 60 | 108. 524. 29 | 335, 066.42 | 12.157.6712 |
| M | 81 | 7,342.8 | 2, 255.4 | 1.074, 621. 22 | 63. 326. 76 | 206, 603. 06 | T. 713.0714 |
| $L$. | 32 | 4,257.3 | 1,233.6 | 568, 957. 89 | 47,760. 94 | 164.733. 11 | 2, 564.0372 |
| Japan: s | 31 | 1,789.5 | - 568.9 | 108. 206.33 | 10. 856.57 | 34, 274.53 | 4.905.9994 |
| Hawaji: ${ }^{2}$ |  |  |  |  |  |  |  |
| S | 36 | 1,884.6 | 606.9 | 100. 518. 50 | 10,399. 99 | 32, 318, 81 | 1, 859.6900 |
| M | 34 | 3.466. 4 | 1,025. 2 | 356.040. 12 | 31, 093. 84 | 105, 169.90 | 2, 6330.4448 |
| $L$. | 133 | 19.955. 4 | 5, 551.6 | 3, 023, 042. 30 | 233, 905. 70 | 841, 363. 67 | 33, 922.08018 |
| Hawail: ${ }^{3}$ | 47 | 2, 679.3 | 870.5 | 153, 111.13 | 16. 161.23 | 49, 734. 11 | .373.9281 |
| $L$ | 20 | 2,859.2 | 800.9 | 409, 803.42 | 32. 168.53 | 114. 804.21 | 1052.1880 |
| Northeast Africa: S | 48 | 3,805.0 | 1.217.0 | 304, 447.00 | 31.064. 50 | 97. 190.35 | 2, 521.4792 |
| Angola, Africa: ${ }^{1}$ |  |  |  |  |  |  |  |
| ${ }_{L}$ | 27 | 2.050.5 | 622.5 1.065 .6 | 206. 275.69 | $18,896.95$ $42,276.26$ | 147. 542.98 | 6.061.0115 3.418 .6200 |
| $Y=$ greatest body depth: |  |  |  |  |  |  |  |
| Costa Rics: ${ }^{\text {a }}$ M $\mathrm{M}^{\text {a }}$ - | 29 | 2,896. 5 | 737.1 | 292, 493. 79 | 18.981. 65 | 74, 476. 86 | 3, 193.3676 |
| $109^{\circ}-119^{\circ} \mathrm{W} .: ~ L$ | 21 | 3. 146. 2 | 813.0 | 475.009.34 | 31. 814.56 | 122.976. 02 | 3.648.6524 |
| $119^{\circ}-129^{\circ} \mathrm{W} .: ~ L$ | 47 | 6.895 .9 | 1,729.6 | 1,016,781. 01 | 64,090. 80 | 255.053. 53 | 5,005. 7588 |
| $129^{\circ}-139^{\circ} \mathrm{W} .: L$ | 46 | 6.867.6 | 1.673.6 | 988.059. 18 | 62, 388.60 | 248.086. 74 | 21.605.0548 |
| $139^{\circ}-149^{\circ} \mathrm{W}$.: $L$ | 109 | 16.168. 8 | 4,111.2 | 2, 412, 075.52 | 156. 425.62 | 613.937. 28 | 13.684. 2995 |
| East Line Islands: | 32 | 3.278.6 | 797.7 | 338, 852.86 | 20,035.94 | 82. 350.48 | 2. 839.7988 |
| $\underline{L}$ | 154 | 22, 339.4 | 5,580. 4 | 3, 255, 028.66 | 203.481.16 | 813. 560.86 | 14.452.0863 |
| West Line Islands: |  |  |  |  |  |  |  |
| $\stackrel{S}{M}$ | 43 | 2,947.9 | 736.8 | 204. 526. 51 | 12.786.92 | 51.111.30 |  |
| $\frac{M}{L}$ | 83 | 8,106. 1 | 1,973.0 | 801, 700. 31 | 47,469.79 | 194.905. 57 | $10,027.3318$ 5.808 .5448 |
| Phoenix Islands: | 57 | 7,876.2 | 1,949.6 | 1.094, 133.62 | 67.274. 94 | 271, 142.41 | 5.808.5948 |
| S | 36 | 2,428.3 | 602.8 | 165, 447. 87 | 10, 182. 66 | 41,030. 24 | 1.652. 2898 |
| $M$ | 59 | 5,795.3 | 1,422.5 | 576,983.99 | 34. 800.57 | 141. 587.97 | 7, 737.1918 |
| $L$. | 44 | 5. 943.0 | 1.478. 5 | 806, 235, 34 | 49.956. 87 | 200.558 .37 | 3. 525. 1355 |
| East Marshall Islands: $L$ | 39 | 5.314.9 | 1,318.7 | 727,070. 77 | 44.873. 79 | 180, 554. 5b | 2.758.9236 |
| Bikini Island: s.---- | 31 | 1,829.9 | 453.4 | 109, 843. 77 | 6. 729.06 | 27,179. 50 | 1.826. 5439 |
| East Caroline Islands: | 60 | 3,916. 3 | 974.8 | 259, 183. 29 | 15. 994.84 | 64, 346. 21 | 3, 559.8019 |
| M | 55 | 5,404. 4 | 1.295.6 | 539, 532. 20 | 31,008. 23 | 129,209. 56 | 8, 486.0298 |
| $L$ | 56 | 7.837.2 | 1,949. 7 | 1, 103, 798. 16 | $68,456.67$ | 274, 743.15 | 6.982. 0200 |

Table A-3.-Regression statistics of yelloufin huna samples-Continued

| Character and size group 1 | $N$ | $s$ S | SY | SX ${ }^{\text {a }}$ | SY' | SSXY | Sx: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  | 37 | 2.513.9 | 620.5 | 173, 34b. 55 | 10, 554.85 | 42, 751.50 | 2,544.0309 |
| $M$ | 102 | 10,289.8 | 2, 465.5 | 1, 049, 698.10 | 69.904. 61 | 250,653.30 | 11, 780.0938 |
| $L$ | 71 | 9,394. 9 | 2,332. 8 | 1,247,581. 59 | 77, 105.00 | 309,934. 35 | 4, 424.6040 |
| Japan: S | 30 | :1,728. 2 | 450.4 | 104, 538.64 | 7,083. 56 | 27, 201.25 | 4,982. 7837 |
| Hawail: |  |  |  |  |  |  |  |
| S | 36 | 1,884.6 | 490.7 | 100,518.50 | 6.787.50 | $26,098.06$ | 1,859.6900 |
| M | 34 | 3. 466.4 | 874.9 | 356,040. 12 | 22, 676. 15 | 89.801. 52 | 2, 630.4448 |
| $L$ | 132 | 19,792.5 | 5.011.4 | 3.001, 505.89 | 193, 468.49 | 761, 486.24 | 33.755.4839 |
| Northeast Africa: $S$. | 48 | 3. 805.0 | 1,006.2 | 304, 447.00 | 21,317.84 | 80, 536. 85 | 2. 821.4792 |
| $Y=$ insertion ventral fin to anterior edge vent: |  |  |  |  |  |  |  |
|  | 47 | 2. 5553.6 6. 895.9 | 739.8 $1.85+4$ | 387.099 .44 $1,016,781.11$ | 32.482 .38 81.621 .42 | 112.090. 41 | 3.518. 6777 $\mathbf{5}, 005.7588$ |
| $129^{\circ}-139^{\circ} \mathrm{W} .: 1$ | 46 | 6.667.6 | 1,891.8 | 958.050. 18 | 79,521.56 | 280,216. 10 | 21.605. 0548 |
| $139^{\circ}-149^{\circ} \mathrm{W}$ : $L$ | 112 | 16,636.5 | 4,704.8 | 2. $484,839.89$ | 198,883. 76 | 702, 735.61 | 13.651. 2091 |
|  |  |  |  |  |  |  |  |
| M | 33 153 | 3,382.8 | 8934.7 | - $349,710.50$ | 26,706.59 | $96,615.03$ ci4, 976.23 | 2.942 .7473 15.046 .7831 |
| West Line islands: | 153 | 22,251.1 | 6,194.2 | 3,251, 069.35 | 252.070.96 |  |  |
| $s$ | 38 | 2.600 .9 | 734.4 | 179,843. 35 | 14,337. 12 | 50,761.21) | 1, 325.4340 |
| M | 83 | 8,070. 3 | 2, 240.3 | 794, 878.69 | 81, 207. 59 | 220, 517.27 | 10. 183.0022 |
| $L$ | 5 | 7.746.7 | 2.154.5 | 1,077, 363.37 | 83,350, 01 | 299,562.14 | 5.731.9256 |
| Phoenix Islands: |  |  |  |  |  |  |  |
| A | 49 | 4,762.2 | 1, 305.9 | 469.014 .30 | 35, 944.71 | 128. 544.55 | 6. 186.7727 |
| $\underline{L}$ | 36 | 4.834 .4 | 1,353.4 | 651.354 .14 | 51,091. 58 | 182, 369.37 | 2. 147.9356 |
| East Marshall Islands: $L$ | 39 | 5,321.7 | 1,479.3 | 738.908. 13 | 56. 402.21 | 202, 694.27 | 2, 741.6970 |
| East Caroline Islands: |  |  |  |  |  |  |  |
| M | 54 | 5,319.5 | 1,487.0 | 532, 324.19 | 41,555.98 | 148.692.69 | 8, 304. 1854 |
| L | 55 | 7.699. 4 | 2.148.7 | 1,084, 809.32 | 84, 431.95 | 302.578.93 | 6,977.3135 |
| Central Carolize Isiands: |  |  |  |  |  |  |  |
| $\mathrm{S}_{\mathbf{H}}$ | 36 | 2,438.9 | 704.0 | 167.721.55 | 13. P34. 26 | 48, 774.98 | 2. 492.8488 |
| $\stackrel{M}{L}$ | 102 | 10.289. 2 | 2,884. 7 | 1.049.698.10 | 82. 400.69 | 293, 998.80 | 11.780. 0938 |
| $L$. | 71 | 9, 404.3 | 2,598.8 | 1, 249.938 .11 | 95. 578.08 | 345, 473.82 | 4.293 .2158 |

Table A-3.-Regression statistics of yellowfin tuna samples-Continued

| Character and size group ${ }^{1}$ | Sty ${ }^{2}$ | Sxy | $\overrightarrow{\boldsymbol{r}}$ | $y$ | $b$ | $a$ | 8 | $\hat{\boldsymbol{Y}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $X=$ fork legnth; $V^{\prime}=$ head length: |  |  |  |  |  |  |  |  |
|  | 173.62<3 | 731. 312 S | 99.879 | 27.238 | 0. 22901 | 4. 365 | 0. 477 | $\stackrel{27.266}{ }$ |
| $109^{\circ}-119^{\circ} \mathrm{W} .: ~ L$. | 256. 5924 | 947.8990 | 149.819 | 37. 953 | . 25979 | . 969 | . 738 | 35. 402 |
|  | 988. 34198 | 1.137. 4179 | 146.721 | 37. 002 | - 22723 | 3. 664 | 815 | 35.475 |
| $129^{\circ}-139^{\circ} \mathrm{W} .: 1$ | 1, 120.4244 | 4, S70. 2135 | 144.948 | 36. 535 | . 22542 | 3.861 | . 716 | 35. 420 |
| $139^{\circ}-149^{\circ} \mathrm{W}:=L$ | 1.837.5227 | 3,314. 7714 | 148.713 | 37.382 | . 23760 | 2.059 | . 677 | 35. 323 |
| East Line Islands: |  |  |  |  |  |  |  |  |
| $\boldsymbol{L}$ | \$36.7488 | 3,377. 1175 | 145. 319 | 36.334 | . 22802 | 3. 198 | 660 | 35.121 |
|  |  |  |  |  |  |  |  |  |
| M | 553. 6904 | 2, 378. 9556 | 97. 755 | 26. 585 | 20125 | 4.956 | . 575 | 27.081 |
| L | 342.1867 | 1,355. 1600 | 138.179 | 35.067 | . 23330 | 2.830 | . 688 | 35. 482 |
|  |  |  |  |  |  |  |  |  |
| $\cdots$ | 173.0948 | 779.0569 | 94.381 | 25. 378 | . 21285 | 5. 200 | . 399 | 26.575 |
|  |  |  |  |  |  |  |  |  |
| M | 359. 7323 | 1.618. 6492 | 98.225 | 26.434 | . 20924 | 5. 881 | . 607 | 26.805 |
| $L$ | 1,103. 4174 | 4,249.3757 | 133. 533 | 33. 470 | . 25534 | -. 326 | . 646 | 35. 132 |
| East Marshall Islands: $L$ | 171. 7190 | 670. 2270 | 135. 335 | 33.995 | . 24251 | . 932 | . 492 | 34, 883 |
| Bikini Island: S. | 106. 7897 | 437.7271 | 59. 029 | 16. 803 | . 23965 | 2.657 | . 254 | 18.646 |
| East Caroline Islands: |  |  |  |  |  |  |  |  |
| M | 378. 4373 | 1,779.1837 | 98.362 | 25. 664 | . 20986 | 5.082 | . 330 | 26. 028 |
| $L$. | 289.6638 | 1,281.1993 | 139.185 | 34.674 | . 21355 | 4.951 | . 550 | 34.848 |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |
| $\mathbf{M}_{\mathbf{H}}$ | 564.9781 | 2.552. 7481 | 100.875 | 26. 211 | . 21670 | 4. 351 | . 344 | 26.021 |
| L | 290.5322 | 1,037.7314 | 132.258 | 33.15: | . 25250 | -. 243 | . 652 | 35.107 |
|  |  |  |  |  |  |  |  |  |
|  | 850.8985 371.8277 | 3.151. 3350 $1,630.8518$ | 65.199 90.738 | 18.802 | .25770 .21144 | 2. 002 | . 402 | 18.763 26.570 |
| $L$ | 138.9072 | 1,485. 9244 | 132. 319 | 33.909 | . 2325.5 | 3.138 | . 929 | 35. 695 |
| Japan: S- | 338.6271 | 1,295. 7323 | 57.726 | 16. 410 | . 25935 | 1. 438 | . 292 | 18. 297 |
| Hawaii: 2 - |  |  |  |  |  |  |  |  |
| M | 134.8224 | 570. 5241 | 101.953 | 26. 859 | . 21689 | 4.746 | . 688 | 36. 435 |
| L | 1,772.6468 | 7,634.8149 | 150. 041 | 37. 064 | . 223507 | 3. 294 | . 644 | 34. 804 |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
| $L$ | S4. 5580 | 291.0780 | 142. 960 | 35. 710 | . 276164 | -3.838 | . 473 | 34. 892 |
| Society Islands: $\mathbf{S}$. | 69. 2153 | 264. 5365 | 58. 147 | 16. 729 | . 25810 | 1. 721 | . 260 | 18. 488 |
| Northeast Africa: $S^{\text {S }}$ | 178. 0382 | 683.5313 | 79.146 | 22. 319 | 24332 | 3. 061 | . 489 | 18. 877 |
| Angola, Africa: ${ }^{4}$ <br> M | 287.9981 | 1, 310. 2386 | 97.643 | 26. 690 | . 21817 | 5.683 | . 601 | 27.200 |
| $L$ | 185. 5896 | 1, 771.5233 | 137.667 | 35. 604 | . 22588 | 4. 535 | . 677 | 36.130 |

YELLOWFIN TUNA

Table A-3.-Regression statistics of yellowfin tuna samples-Continued

| Character and size group ${ }^{1}$ | $S y^{2}$ | Sry | $\bar{x}$ | y | $b$ | a | \% | $\hat{r}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Sigma=$ pectoral in length: |  |  |  |  |  |  |  |  |
| Costa Ricas ${ }^{2}$ M | 134.4011 | 2. 6880 | -2.9963 | 26. 882 | 432.97201 | -102. 540 | 0. 845 | 27.142 |
| 1190-129 ${ }^{\circ}{ }^{\circ}$ W: ${ }^{L}$ | ${ }_{244 .} \mathbf{9 2 7 2}$ | 2. 27620 | 3.1568 | 38.537 | - 514.5189698 | $\xrightarrow{-140.400}$ | 1. 2989 | - ${ }_{\text {34, }}^{3454}$ |
| $129^{\circ}-139^{\circ} \mathrm{W} .: \frac{L}{L}$ | 909.6983 | 15.8129 | 3. 1547 | 35.878 | 512. $\mathrm{Pe547}$ | -125.947 | 1. 497 | 35.437 |
| ${ }^{139^{\circ}-149^{\circ}}$ W.: $L$ | 331. 2473 | 4.1885 | 3.1711 | 37.311 | 339.49066 | -70.345 | 1.305 | 36.462 |
| East Line Islands: | 418.4364 | 4.1211 | 3. 1605 | 36.850 | 350.85434 | -74.038 | 1.493 | 36. 354 |
| L | 178.0457 | 2. 9152 | 3. 0053 | 28.681 | 532.81670 | -131.606 | . 870 | 28. 339 |
| West Line Islands: | 221.2870 | 4.6015 | 2. 8345 | 20.347 | 423.25557 | -101.051 | . 768 | 19.421 |
| ${ }_{\text {M }}$ | 813.2639 | 1.2.0643 | -2.9875 | 28.117 | 567. 138026 | -141.463 | 1. 234 | 28. $\mathrm{S}^{266}$ |
|  | 216.2060 | 3.9708 | 3. 1398 | 36. 250 |  | -130.103 | 1. 144 | 36. 583 |
| Phoenix istands: | 177.6927 | 3. 3265 | -. 8288 | 20. 329 | 461.18443 | -110.110 | 831 | 19.617 |
| ${ }^{\text {M }}$ | 555.9023 | 7. 8803 | - 9878 | 29. 243 | 546883293 | $-134.140$ | 1. 3023 |  |
| East Marshail | 143.0861 | 1.7135 | 3.1292 3.1337 |  | - 4996.103104 | -119.502 | 1.149 | ${ }_{\text {che }}^{36.555}$ |
| Eikini Island: $\mathbf{S}$ Lands: $L$ | 153. 7794 | 3. 4868 | -. 7677 | 18. 026 | 410.25520 | -95.520 | . 594 | 19.881 |
| East Caroline Islands: |  |  |  |  |  |  |  |  |
| ${ }^{\text {a }}$ | 520.3053 | 8. 3698 | 2.2884 | 39.591 | 544. 98401 | $-133.275$ | 1.122 | 30.223 |
|  | 177. 7235 | 2.5316 | 3. 1456 | 3f. 791 | 398.77764 | -88.648 | 1. 204 | 36. 811 |
| Central Caraline Islands: | 301.7364 | 5.7481 | 2. 8293 | 21.619 | 409.01303 | -119.746 |  |  |
| M | 705. 1471 | 11. 3351 | 3.0011 | 30. 641 | 495.77274 | -118. 145 | 1. 197 | 30.687 |
| ${ }_{\text {L }}$ | 183. 6188 | 1.7332 | $\begin{array}{r}3.1207 \\ \hline\end{array}$ | 35. 779 | 376.72901 430 | - $\mathrm{-lil}^{81.787}$ | 1.300 | -3i.736 |
| Japran: S | 534.0737 | 13.1384 | 2. 7480 | 17.177 | 430. 92565 | -101. 341 | . 627 | 19.974 |
| S. | 215.5789 | 4. 5411 | 2. 7154 | 15. 295 | 433.19946 | -102. 33i | 745 | 19. 519 |
| ${ }_{\text {ar }}$ | 197.1306 | 2.4781 | 3.0069 | 29.129 | 517. 42426 | -138.459 | 1.467 | 28. 777 |
| $L$ | 927.9926 | 13.6475 | -3.1737 | 37.818 | ${ }_{5}^{476} \mathbf{4} \mathbf{4} \mathbf{9 7 1 8 4}$ | ${ }^{-113.536}$ | 1. 454 | 36.524 |
| Society Islands: $S$ - | ${ }_{171.7448}^{179.329}$ | 3. 3800 |  | 20.698 | +07, 39721 | ${ }_{-97.272}$ | . 805 | 17.305 |
| Angola, Africa: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |
|  | ${ }^{4633.7067}$ | 7.7847 | ${ }^{\text {3 }}$ 3. 13874 | - 37.133 | 611.03338 588.40886 | - $\begin{aligned} & -155.145 \\ & -14986\end{aligned}$ | 1.079 | ${ }_{35}^{28.166}$ |
| $\Gamma=$ height seend dorsal |  |  |  |  |  |  |  |  |
| Costa Ricas ${ }^{\text {a }}$ MI | .$^{25565966}$ | . 114971 | ${ }^{2} .9983$ | -2. 1809 | 1. 433116 | -3. 68951 | ${ }^{0366}$ | 1971 |
| $10190^{\circ}-119^{\circ} \mathrm{W} \cdot \mathrm{L}$ | ${ }^{2436991}$ |  | 3.1788 | 2.8851 | $\frac{1}{3} \cdot \underline{26332}$ | -5.86 |  | $\bigcirc$ |
| $129^{\circ}-139^{\circ} \mathrm{W}$ : ${ }^{L}$ | ${ }_{1}$ 1.623733 | . 6861232 | ${ }_{3}^{3.1540}$ | ${ }_{2} .5734$ | ${ }_{3} 1.15071$ | -7.2099 | 0685 | 2.5584 |
| ${ }^{139^{\circ}-149^{\circ}}$ W. $L$ | 1.205756 | .297734 | 3.1712 | 2.6373 | 2.46014 | -5.1643 | . 06651 | 2.5755 |
| East Line islands: | .953147 | .0S7181 | 3.0069 | 2.3747 | 1.71269 | - 3.8752 | 0588 |  |
| L----------1-1 | 1. 281956 | .420403 | 3.1610 | 2.6842 | 3.00440 | -6.8327 | . 0686 | 2. 6194 |
| West Line islands: |  |  |  |  |  |  |  |  |
| M | 1.037693 | . 414389 | 2.6856 | 2.2504 | 2. 04152 | $-3.8448$ | 0484 | 2.2798 |
|  | .7387\%0 | . 171563 | 3. 1392 | 2.6188 | 2. 99334 | -6.7748 | . 0840 | 2. 6394 |
| Phoenix Islands: |  |  |  |  | 1.80376 | -3.1127 | 0925 |  |
| M | . 497785 | . 2223371 | 2.9866 | 3.2771 | 1.73367 | -3. 9007 | 0460 | $\stackrel{1}{2.3003}$ |
|  | .425877 | . 108706 | 3. ${ }^{3} 1275$ | $\stackrel{2}{2.6043}$ | ${ }^{2} .687678$ | -5.7607 | ${ }^{0578}$ | ${ }^{2} .68541$ |
| East Marshall | . 327443 | . 0180457 | 3.1344 <br> 3.7646 | 1.8574 | ${ }^{3} .761759$ | -5. 5677 | .0550 | - 3.635 |
| East Caroline Islands: | 219409 | - | 2.7646 |  |  | -2.6062 | . 23 |  |
| S-------------1 | 退 | ${ }^{-2683826}$ | 2. 2.8116 | 1. ${ }^{\text {1. } 8812}$ | ${ }_{\text {1 }} 1.63446$ | -3.6142 | . 02047 | 1.9834 |
| L-------------- | . 442076 | . 139895 | 3.142 | ${ }_{2} .6505$ | ${ }^{2} .11757$ | $-3.9770$ | . 0530 | 2.6845 |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |
| M | . 1125388 | 184815 | 2.8872 | 3.0107 | ${ }^{1} .833348$ | -2.6075 | . 0185 | 1.9873 |
| ${ }_{L}$ | 1. ${ }_{6224480}$ | . 2125178 | ${ }_{3}^{3.1205}$ | $\underline{3} 5157$ | 2. 72033 | -t. 8731 | - 303 | ${ }^{2}$ |
| Japan: s | .660717 | .430861 | 2.7516 | 1. 8633 | 1.49317 | $-2.2448$ | 045 | 1. 9563 |
| Hawaii: |  |  |  |  |  |  |  |  |
| M | . 188446 | .07539 | ${ }^{3} .0006$ | 2.2678 | 1.66645 | -2. 74.78 | ${ }_{044}$ | - 3.2565 |
| $L$ | 2. ${ }^{23799}$ | . 69805 | 3. 7737 | $\bigcirc-6449$ | ${ }^{2} .42554$ | -5.0484 | 0583 | 2. 5889 |
| Society Islands: $s$ | . 2025096 | . 1038140 | $\stackrel{\mathbf{2}}{\mathbf{2} .7531}$ | 1.8640 | ${ }_{1}^{1.88337}$ | -3.1697 | 0299 0309 | 1.9733 |
| Northeast Africa: Angola, A frica: t | . 180946 | .084192 | 2.9054 | $\underline{2.0141}$ | 1.25539 | -2. 856 | 0309 | 1.8582 |
| M--------- | . 351508 | . 134019 |  | $\bigcirc .2290$ |  | -2.9398 | .0296 | 2.9515 |
| $\boldsymbol{Y}=$ height anal on | . 168917 | .1055379 | 3. 1397 | 2.5297 | 2.09388 | -4.0445 | . 0470 | 2. 5431 |
| Costa Rica: ${ }^{\text {M }}$ | .28615? | 120993 | 2.9864 | 2.2232 |  | -3.7708 | . 0412 |  |
| $1099^{\circ}-119^{\circ} \mathrm{W} .: ~ L$ | . 3288749 | 087570 | 3.1723 | 2. 6178 | 2. 83333 | -6.3935 | .0667 | 3. 5433 |
| $119^{\circ}-129^{\circ} \mathrm{W}$. | 55721 | 123457 | 3. 1650 |  | 2.85608 | -6. 4030 | .0667 | $\cdots$ |
| 12990-139 ${ }^{\circ} \mathrm{W} .:$ L | 1.689788 | . 6760038 | 3. 11330 | ${ }^{\text {2. }}$. 6213 | 3.21464 | -4.3611 | . 0677 | -2.8001 |
|  | 1.103309 | . 264315 | 3. 1705 | 2.6837 | 2.300343 | -4.3935 | . 0667 | 2.6290 |
| M | . 313393 | . 110760 |  | 2.3050 | 2. 11323 | $-3.7524$ | . 0540 | $\stackrel{3}{ } .2873$ |
| West Line islands: | 1.916466 | . 385379 | ${ }^{3} 1803$ | 2.7088 | 2.85648 | -6.3175 | 0735 | 2.6683 |
| S ${ }_{\text {S }}$ | . 343110 | . 1773580 | ${ }_{2}^{2} .8361$ | ${ }^{1.9814}$ | 1.71601 | -2.8854 | . 03081 | 1.9416 |
| 1 | 1.566031 .7029 | . 166075 | ${ }_{3}{ }^{2} .1388$ | $\frac{2.6726}{}$ | $\frac{3.37045}{3.17042}$ | -7.8.2787 | .0643 | 2. 6095 |
| Phoenix Islands: |  |  |  |  |  |  |  |  |
| M | $: 333352$ | . 1452508 | 2.8884 | $\xrightarrow{1.9862}$ | 1.83379 | ${ }_{-}^{-3.7309}$ | .0658 | 1.9554 |
|  |  | . 071908 | 3.12066 | 2. 2598 | 2.73654 | -5. 5963 | . 0524 | 3.7131 |
| Rast Marshall Islan | . 26335383 | 064190 | -3. 1363 | $\stackrel{.}{2.7137}$ | 2. 463318 | 4. 9778 | 0535 | 2. 7401 |
| drin mand. |  | 2400 | . | 1.8031 | 1.803 | -3.40- | Or | 1.925 |

Table A-3.-Regression statistics of yellowfin tuna samples-Continued

| Character and size group ${ }^{1}$ | $S y^{2}$ | Sxy | $x$ | $y$ | $b$ | $a$ | 8 | $\hat{\boldsymbol{Y}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| East Caroline Islands: |  |  |  |  |  |  |  |  |
| S | 0. 647968 | 0. 318363 | 2.8116 | 1. 9883 | 1.94135 | $-3.4720$ | 0.0261 | 1. 9888 |
|  | . 819340 | . 350096 | 2. 9889 | - 2.3532 | 2. 153387 | -4.0845 | . 0351 | $\stackrel{3}{3} 3711$ |
|  | . 419122 | . 141299 | 3. 1427 | 2.7392 | 2.22911 | -4.2662 | . 0456 | 2. 7468 |
| Central Caroline Islands: | . 477109 | .226364 | 2.8208 | 2.0155 | 1.97398 | -3. 5705 | . 0303 | 1.9821 |
| $\boldsymbol{M}$ | 1. 198853 | . 484446 | 3. 0020 | 2.3715 | 2. 19595 | -4. 2207 | . 0368 | 2. 3672 |
| L | .478073 | . 109642 | 3. 1203 | 3.6859 | 2.44464 | -4.9449 | . 0556 | 2. 7462 |
| Japan: S | . 804493 | . 464202 | 2. 7544 | 1.8535 | 1.68668 | -2. 7923 | . 0277 | 1.9522 |
| Hawail: |  |  |  |  |  |  |  |  |
| $\stackrel{N}{M}$ | . 259888 | . 1798168 | 2.7165 3.0070 | 1. 3.3009 | 1.82453 | -3.1565 | . 05817 | 1.9476 |
| $L$ | 2. 16105 | . 70561 | 3. 1737 | 2. 6959 | 2.45174 | -5.0852 | . 0574 | 2.6282 |
| Soclety Islands: $\mathbf{S}$ | .204286 | . 088154 | 2.7558 | 1.8589 | 1.84795 | -3.2337 | . 0367 | 1.9644 |
| Northeast Africa: S | . 255261 | . 094904 | 2. 9054 | 2.0478 | 1.89883 | -3.4720 | . 0427 | 1.8720 |
| Angola, Africa: ${ }^{1}$ $\mathrm{M}$ | . 465751 | . 229392 | 2.9831 | 2.2316 | 1.94056 | -3.5573 | . 0329 | 2.2644 |
| $L$ | . 197757 | . 058162 | 3.1374 | 2. 5594 | 1.80400 | -3.1632 | . 0605 | 2. 5753 |
| $Y=$ snout to insertion first dorsal fin: |  |  |  |  |  |  |  |  |
| Costa Rica: ${ }^{2} \mathrm{M}$ | 247.3317 | 875.6769 | 99.879 | 29.445 | . 27429 | 9.050 | .517 | 39.478 |
| $109^{\circ}-119^{\circ} \mathrm{W} .:$ L | 273.6429 | 943.5086 | 149.819 | 41.229 | . 25859 | 2. 487 | 1.249 | 38.690 |
| $119^{\circ}-129^{\circ} \mathrm{W} .:$ L | 297. 6080 | 1.131.0567 | 146.598 | 40. 557 | . 23818 | 5. 641 | . 817 | 38.886 |
| $129^{\circ}-139^{\circ} \mathrm{W} .:$ L | 1,335. 25.4 | 5, 309.5731 | 144.948 | 40.180 | . 24576 | 4.558 | . 831 | 38.964 |
| $139^{\circ}-149^{\circ} \mathrm{W} .: ~ L$ | 1,065.7168 | 3, 687. 1724 | 148. 617 | 40.830 | . 26423 | 1. 561 | . 912 | 38. 553 |
| East Linc Islands: |  |  |  |  |  |  |  |  |
| M | 190.5364 1.015 .4022 | 726.4491 $3,624.0635$ | 102.509 145.412 | 29.736 39.693 | . 246886 | 4.431 4.707 | . 601 | 29.117 38.391 |
| West Line Islands: |  |  |  |  |  |  |  |  |
| S. | 193.8216 | 666.9093 | 68. 684 | 21.270 | . 17039 | 2. 664 | . 560 | 30.272 |
| $M_{1}$ | 662. 518 : | 2,592.9605 | 97. 701 | 28.595 | 2.41917 | 4. 959 | . 648 | 29.151 |
| $L$ | 368.3411 | 1.357. 9180 | 137.760 | 37. 613 | . 25409 | 2.610 | . 663 | 38.183 |
| Palmyra Island: ${ }^{8}$ |  |  |  |  |  |  |  |  |
| S | 68.7829 | 219.2757 | 72. 491 | 22.786 | . 25930 | 3. 989 | . 601 | 20.844 |
| $\boldsymbol{M}$ | 219.5742 | 861.7644 | 94.381 | 27.840 | . 23758 | 5.417 | . 519 | 29.175 |
| Phoenix Islands: |  |  |  |  |  |  |  |  |
| S | 128.3457 | 438.3757 | 68.137 | 21.157 | . 28120 | 1.997 | . 392 | 20.275 |
| M | 453.8894 | 1,834. 8211 | 98. 225 | $\underline{28.659}$ | . 23714 | 5. 366 | . 574 | 29.080 |
| $L$ | 195.9245 | 767.8912 | 134.878 | 37.111 | . 22161 | 7.221 | . 774 | 38. 246 |
| East. Marshall Islands: $L$ | 196.1190 | 711.5547 | 136.177 | 37.472 | . 26114 | 1. 911 | . 598 | 38.471 |
| Bikini Island: S. | 117.0019 | 455.4545 | 59.029 | 19.331 | . 24935 | 4.612 | . 344 | 20.820 |
| East Caroline Islands: | 205. 9424 | 863.8139 |  | 20.159 | 25035 | 3. 775 | 412 | 20.048 |
| M | 489.4139 | 2.013.2142 | 98.262 | 28.378 | . 23724 | 5. 066 | . 472 | 28.790 |
| $L$ | 464.1772 | 1.722.2100 | 139.950 | 38.393 | . 24668 | 3.873 | . 854 | 38.405 |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |
| S | 173.4274 | 626.0369 | 67.963 | 20.851 | . 26946 | 2. 538 | . 336 | 20.053 |
| $\boldsymbol{M}$ | 706.3275 | 2,811.4461 | 100.875 | 28.972 | . 23886 | 4. 887 | . 595 | 28.763 |
| L | 278.6586 | 999.4995 | 132.455 | 36.587 | . 23281 | 5. 750 | . 816 | 38.343 |
| Philippines (SW. Panay): | 1,019.2827 | 3,379.1865 | 65.192 | 21.163 | 27633 | 3.14S | 597 | 21.109 |
| M | 1,428.3114 | 1,748.5687 | 90.738 | 27.562 | 22670 | 6.902 | . 636 | 29.669 |
| $L$ | 195. 15534 | 625. 5600 | 132.991 | 37.667 | . 24373 | 5. 253 | 1. 172 | 39.375 |
| Japan: S. | 420.2387 | 1.442.2852 | 57.720 | 18. 194 | . 28869 | 1. 529 | . 365 | 20.294 |
| Hawali: 2 |  |  |  |  |  |  |  |  |
| S | 174.8700 | 562.9000 | 52.350 | 16.717 | . 30268 | . 872 | . 363 | 20.546 |
| M | 171.8026 | 831.8042 | 101.953 | 29.859 | . 24098 | 5. 367 | . 782 | 29.380 |
| $L$ | 2,072. 9122 | 8,073. 1400 | 149.688 | 41.066 | . 24585 | 4. 263 | . 827 | 38.685 |
| Hawaii: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |
| S | 36.0749 | 109.3328 | 57.006 | 17.757 | . 29239 | 1.089 | . 302 | 20.094 |
| $L$ | 102.3400 | 308.8700 | 142. 960 | 39.700 | . 29355 | -2. 266 | . 805 | 38.831 |
| Society Islands: $\mathrm{S}^{\text {. }}$ | 95.2982 | 323. 53310 | 57.300 | 18. 191 | . 28254 | 2. 001 | . 441 | $\stackrel{0.366}{ }$ |
| Northeast Africa: S. | 236.4532 | 774. 5938 | 79.146 | 24. 656 | . 27453 | 2.028 | . 719 | 20.778 |
| Angola, Africa: |  |  | 97.643 | 28.895 | 22925 | 6. 510 | . 661 | 29.435 |
| $L$ | 246. 76018 | 1. 882.9367 | 137.687 | 38.619 | . 25887 | 3.064 | . 865 | 30.222 |
| $Y=$ snout to insertion second dorsal in: |  |  |  |  |  |  |  |  |
| Costa Rica: ${ }^{2}$ M | 716.6532 | 1,497.4956 | 99.879 | 52.676 | . 46894 | 5. 839 | 731 | 52. 733 |
| $109^{\circ}-119^{\circ}$ W.: $L$ | 845.0696 | 1,731.8520 | 149.819 | 76. 195 | . 47466 | 5.082 | 1. 101 | 71.534 |
| $119^{\circ}-129^{\circ}$ W.: $L$ | 1,004. 2098 | 2, 109.2962 | 147.061 | 73.998 | . 46092 | 6.215 | .873 | 70.744 |
| $129^{\circ}-139^{\circ} \mathrm{W} .:$ L | 4,730.7931 | 10, 065. 2044 | 144.948 | 73.143 | . 46587 | 5.616 | . 973 | 70.838 |
| $139^{\circ}-149^{\circ}$ W.: $L$ | 3, 362. 0565 | 6. 772.2915 | 148.807 | 74.748 | . 48159 | 3. 084 | . 956 | 70.507 |
| East Line Islands: |  |  |  |  |  |  |  |  |
| ${ }_{\boldsymbol{M}}^{\mathbf{L}}$ | 676.3607 $3,309.7462$ | $1,384.4728$ $6,849.5643$ | 102.509 145.275 | 52.704 72.572 | .47387 .45233 | 4.148 6.860 | .709 1.176 | 51.535 70.186 |
| West Line Islands: |  |  |  |  |  |  |  |  |
| S. | 575.4945 | 1,172. 4419 | 68.556 | 36.933 | . 48232 | 3.867 | 494 | 35.218 |
| M | 2. 287.5834 | 4, 870.4040 | 97.314 | 50.438 | . 46006 | 5. 5330 | . 787 | 51.5336 |
| $L$ | 1,308. 7299 | 2, 704.8159 | 138.084 | 69.073 | . 46798 | 4.452 | . 892 | 69.969 |
| Palmyra Island: ${ }^{3}$ | 180.7674 | 376.7145 | 72.615 | 39.091 | . 45521 | 6. 036 | . 539 | 35. 625 |
| M | 775.4415 | 1,650.5199 | 04.381 | 49.054 | . 45504 | 6. 107 | . 666 | 51.611 |
| Phoenix Islands: |  |  |  |  |  |  |  |  |
| S. | 390.3168 | 793.6846 | 67.665 | 36.419 | . 46352 | 5.054 | . 801 | 35.183 |
| M | 1, 340.9868 | 3,463.7556 | 98.295 | 50.476 | . 44768 | 6. 503 | 1. 259 | 51.271 |
| $L$ | 796.5933 | 1,623.2620 | 134.937 | 67.628 | . 46748 | 4.548 | . 926 | 69.995 |
| East Marshall Islands: $L$ | 638.2959 | 1.303. 4785 | 135.454 | 68.610 | . 47543 | 3.736 | . 709 | 70. 296 |
| Bikini Island: S | 418.3968 | 872.0206 | 59.029 | 32.058 | . 47742 | 3.876 | . 268 | 34.908 |
| East Caroline Islands: | 7810.0523 | 1. 650.8019 | 65.156 | 34.966 | . 46999 | 4.343 | . 423 | 34.892 |
| M | 1.693.7611 | 3,778.2813 | 98.262 | 50.267 | . 44524 | 6.517 | . 466 | 51.041 |
| L. | 1,533.9336 | 3,239.2500 | 139.950 | 69.311 | . 46394 | 4.388 | . 759 | 69.335 |

See footnotes at end of table.

Table A-3.-Regression statistics of yellowfin tuna samples-Continued

| Character and size group ' | Sp ${ }^{\text {a }}$ | Sxy | $\bar{x}$ | $\bar{j}$ | ${ }^{6}$ | $a$ | $s$ | $\hat{\mathbf{r}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |
| S | 607. 6519 | 1, 234.3865 |  |  | 0.48521 | 3. 379 | 0.499 | 34.918 |
| $\stackrel{\sim}{L}$ | ${ }^{2} .941 .0570$ | 1,849.3555 | ${ }_{132} 1100$ | ${ }_{65.788}^{66.292}$ | . 47487 | 2.948 | . 976 | 50.916 69.430 |
| Philippines (SW. Panay): | 1. 108 | 5.080 .687 |  |  |  |  |  |  |
| M | 1,618.9233 | 3,478.0029 | ${ }_{90} 9.738$ | ${ }_{49.355}^{36.963}$ | ${ }_{45092}$ | 5.077 8.419 | . 801 | 36.868 53.511 |
| $L$ | -496.8372 | 932. 50nw | 132.625 | 68.771 | ${ }_{49348}$ | ${ }_{3} 323$ | 1.283 | 73.410 |
| Japan: S | 1,301.1187 | 2,545.3652 | 57.726 | 31. 594 | 50914 | 2.203 | . 422 | 35. 297 |
| Hawaii: ${ }^{\text {a }}$ | 511.6323 | 969.2300 | 52.350 | 28.928 | 52118 | 1.644 |  |  |
| M | ${ }^{551.5250}$ | 1,186.0400 | 101.953 | 52.85ii | 45089 | 6. 980 | . 724 | ${ }_{52} 0.069$ |
|  | 7,209.8055 | 15,390.0719 | 149.829 | 74.636 | 46475 | 5.003 | 1.049 | 70.068 |
| Hawair ${ }^{\text {a }}$ | 100.8362 | 189.9036 | 57.006 | 31.145 | 50787 | 2. 193 | . 316 | 35:205 |
| L | 300.1720 | 549.2740 | 142.960 | 71. 880 | 52203 | $-2.749$ | . 864 | 70.335 |
| Society Islands: S. | -206.0000i | $\begin{array}{r}537.7360 \\ 1 \\ \hline\end{array}$ | -57.586 | 31.700 | . 4885850 | 3. 736 | . 452 | 35.300 |
| Northeast Africa: ${ }^{\text {Angola, Africa: }}$ | 679.5392 | 1,309.8653 | 79.549 | 42.879 | . 49570 | 3. 442 | . 828 | 35.666 |
| M | 1,220.0315 | 2,708.2886 | 97.643 | 51.857 | . 44684 | 8.226 | 720 | 59.910 |
| $L$ | 797.1497 | 1,632. 7434 | 137. 667 | 70. 104 | . 47760 | 4.354 | 833 | 71.218 |
| Costa Rica: ${ }^{\text {a }} \boldsymbol{A}$ | 901.9325 | 1,6S9.1911 | 99.879 | 58.952 | 52897 | 6.119 | 558 | 59:016 |
| $109^{\circ}-119^{\circ} \mathrm{W} .: L$ | 1,030.0096 | 1.923. 3651 | 149.819 | 84.105 | . 52714 | 6. 129 | 921 | 78.929 |
| $119^{\circ}-122^{\circ} \mathrm{W}$ W.: $L$ | 1, 289.0966 | 3.483.5686 | 146.721 | \$1. 391 | . 49814 | 8. 597 | 1.124 | 78. 057 |
| $129^{\circ}-139^{\circ} \mathrm{W} .: L$ | 5, 338.7524 | 11,092. 3631 | 144.948 | 80. 680 | . 51342 | 6. 261 | . 997 | 78.140 |
| $139^{\circ}-149^{\circ} \mathrm{W} . L$ East Line Islands: | 4, 479.4653 | 7,467. 2943 | 148.773 | 82.568 | . 52850 | 3.941 | 1.095 | 77.93i |
| $M_{\text {- }}$ | 817.0247 | 1,518.4694 | 102. 856 | 58.428 | . 52005 | 5.042 | 955 | 57.047 |
| West Line island | 4. 131.1894 | 7,667.8075 | 145. 358 | 80. 998 | . 51604 | 5.987 | 1.074 | $78:{ }^{233}$ |
| S | 713.5660 | 1, 305. 8900 | 68. 758 | 40.700 | . 53267 | 4.075 | .662 | 38.699 |
| M | 2, 875. 5732 | 5.466. 1261 | 97.735 | 55.655 | . 51179 | 5.635 | . 864 | 56.814 |
| $L$ | 1.49̇. 9556 | 2, 855. 7543 | 137.929 | 76.541 | . 50918 | 6.311 | . 348 | 77: 596 |
| ${ }^{1}$ 1.alnyra Island: ${ }^{\text {a }}$ | 233.9869 | 435.8838 |  | 42.946 | . 51544 | 5.581 |  | \%ild |
| M | 903.3425 | 1,769.4060 | 94.381 | 53.851 | . 48782 | 7.810 | . 855 | 58.592 |
| Phoenix Islands: | 444.3098 |  |  |  |  |  |  |  |
| M | 1.929.7416 | 3.813.6566 | 98.238 | 39.997 55.888 | . 51949293 | 7. 7028 | . 5949 | 38.463 56.557 |
| ${ }_{L}$ | 989.7312 | 1. 103.2645 | 135.082 | 74.456 | ${ }_{52593}$ | 3. 412 | 981 | 77.042 |
| East Marshall Islands: | 856.0678 | 1, 517.2455 | ${ }^{136 .} 335$ | ${ }^{75.068}$ | . 548988 | - 233 | 780 | 77:080 |
| Bikini Lsland: S--7-: | 506. 6084 | 957.7826 | 59.029 | 35. 290 | 52437 | 4. 337 | 388 | 38.421 |
| East Caroline Islands: | 1,051.0974 | 1,923. 1547 |  | 38.373 | . 54023 | 3.111 |  | 38.296 |
| ${ }_{4}$ | 3.045.6484 | 4, 142. 9923 | 98. 385 | 55. 2128 | . 49083 | 6. 938 | 483 | 56.021 |
| Central caroline Islands: | 1,814. 6219 | 3.462.6946 | 139.675 | 76.282 | . 51312 | 4. 612 | 845 | 78.4.49 |
| S. | 764.8509 | 1,379.1509 | 67. 943 |  |  | 3. 410 | 701 |  |
|  | 2, 802. 13358 | 5, 668.0991 2.055. 2489 | 100.835 | 56.8.830 | .48116 .43493 | 8.293 |  | 56. 409 76.910 |
| Philippines (Sw. Panay): |  |  |  |  |  |  |  | 76.916 |
|  | 3, 750.4799 | 6. 625.5577 | 65.192 | 40.489 | 54181 | 5. 167 | . 818 | 40.385 |
| M | 2.022. 90023 | 3.895.0441 | 90. 738 | 54.215 | 50499 | 8.393 | . 842 | 58.89: |
| ${ }_{\text {Japan: }}^{\text {L-- }}$ |  | 2,781.4510 | 13.552 57.726 | 75.852 | ${ }_{55674}$ | 15.937 <br> 2.423 | 1.706 .384 | 79.918 38.611 |
| Hawail: ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |
| S | 598.5950 | 1,047.6500 | 53.350 | 31.789 | . 56335 | 2. 298 | . 497 | 38.916 |
| ${ }_{L}$ | 704.4953 | 1.337, 5412 | 101.953 | 58.488 | . 50848 | 6.047 |  | 57. 485 |
| Hawaii: ${ }^{\text {a }}$ | 8 8,665. 5824 | 17,000. 7218 | 150.063 | 82.924 | . 50137 | 7.634 | 1.045 | 77.876 |
|  | 124.4687 | 210.5892 | 57.006 | 34.337 | . 56318 | 2.232 | 361 | 38.839 |
|  | 337.0055 | 584.2480 | 142.960 | 79. 985 | . 555278 | . 604 | 836 | 78. 342 |
| Northeast Africa: | 792.1596 | 1,459.8564 | 79.098 | 47.460 | . 51834 | 6.460 | 888 | 40.152 |
| Angola, Anica: | 1,513. 1488 | 3, 014. 1629 | 7.643 | 56. 986 | 49730 | 8. 428 | 834 |  |
|  | 787.8897 | 1. 508.4197 | 1316.893 | 76.696 | . 50250 | 7.907 | 1.116 | 78.257 |
| =snout to insertion ventral fin: |  |  |  |  |  |  |  |  |
| ${ }_{1199^{\circ}-1299^{\circ} \mathrm{W}: \text { : }}^{\text {L }}$ | 393. 417.6371 | $1,003.0157$ $1,330.6669$ | 149.819 146.721 | 49.186 41.053 | . 274463 | 1.041 <br> 2.051 | +.992 | 39.489 |
| $129^{\circ}-139^{\circ} \mathrm{W}: L$ | 1.356.8898 | 5.353.5948 | 144.948 | 40.598 | . 24779 | 4.681 | . 830 | 39.372 |
| ${ }^{139} 9^{\circ}-149^{\circ} \mathrm{W} .:$ L | 1.032. 2273 | 3.653.3615 | 148. 773 | 41.489 | . 25857 | 3.021 | 888 | 39.291 |
| East Line Islands: |  |  |  |  |  |  |  |  |
| ${ }_{L}^{\text {L }}$ | 171.8619 $1,378.2468$ |  | 102.651 | 30.816 | $\begin{array}{r} .93594 \\ .28416 \end{array}$ | $6.589$ | $\begin{array}{r}.588 \\ \hline 1.035 \\ \hline\end{array}$ | $30.153$ |
| West Line Islands: |  |  |  |  |  |  |  |  |
|  | 197.7514 | 662. 5486 | 68.798 | 21.986 | . 27978 | 2. 738 | 556 | $\stackrel{20.924}{ }$ |
| ${ }_{L}$ | 725. 1524 |  | 97.817 | 29. 710 | . 25258 | 5. 003 | 802 | ${ }^{30 .} 261$ |
| Palmyra İ-and: | 419.3256 | 1.499. 3643 | 135.129 | 39.581 | . 25849 | 3.886 | . 767 | 40.075 |
| S. | 67.7354 | 23, 6094 | 72.491 | 229.831 | 27388 | 2.977 | 361 | 20.779 |
| Phoenix Islands: | 206.6390 | 838.6164 | 94.381 | 28.043 | 23120 | 6. 221 | 481 | 29.341 |
|  |  | 386.4849 | 68.103 | 21.651 | . 24564 |  | 547 | 20.889 |
|  | 507.6593 | 1. 849.5511 | 93. 855 | 29.699 | . 25748 | 4. 243 | 763 | 29. 991 |
|  | 255.6681 | 846. 2511 | ${ }^{134.937}$ | 37.793 | . 24371 | 4. 908 | 1. 060 | 39.0.07 |
| Bikini Island: $\mathcal{S}$. | 207. 6508 | 729.2810 | ${ }^{136.321}$ | ${ }^{37 .} 780$ | . 26782 | 1.250 | . 598 | 38.745 |
| East Caroline Ssiands: | 136.5968 | 485.3494 | 59.029 | 18.945 | .26736 | 3. 163 | 456 | 20.541 |
| S. | 278.3699 | 982.4089 | 65.272 | 20.282 |  |  |  |  |
| ${ }_{L}$ | ${ }_{399.8920}^{487.3084}$ | 2,001.3060 1.591. 7800 | 98. 367 139.727 | 28. 639 38.840 | .23674 .2308 | 8. ${ }^{\text {5. }} 272$ | ${ }_{738} 510$ | 29.026 38.903 |

Table A-3.-Regression stalistics of yellowfin tuna samples-Continued

| Character and size group i' | $S y^{2}$ | Sry | $\bar{x}$ | $\bar{y}$ | $b$ | $a$ | 8 | $\hat{\boldsymbol{Y}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |
| S | 213.6064 | 681. 6864 | 68.331 | 31.431 | 0.29080 | 1. 560 | 0.674 | 20.462 |
| M | 716.5196 | 2, 764.7333 | 101.034 | 29.502 | . 24001 | 5. 253 | . 731 | 29. 254 |
| ${ }^{L}$ | 360.4895 | 1, 028. 6865 | 131. 743 | 37.253 | 28316 | 2. 584 | 1.166 | 39. 426 |
| Philippines (SW. Panay): |  |  |  |  |  | 2.413 |  |  |
| AI | 1.088 .2501 526.4000 | 3, 4891.7440 1.951 .9623 | 65.157 80.738 | 27.116 27.844 | . 285304 | 2. 4881 | . 641 | 21.071 30.188 |
| $L$ | 205.6800 | 614. 1950 | 133.041 | 38. 550 | . 23954 | 6. 681 | 1. 397 | 40.217 |
| Japan: S | 416.3374 | 1,434. 3187 | 57.726 | 18.352 | . 28708 | 1.778 | 396 | 20.440 |
| Hawail: \% | 168.6675 | 547.5950 | 59) 350 | 16.858 | 29445 | 1.444 |  |  |
| ${ }_{\mathbf{M}}$ | 181.0448 | 647. 7448 | 101.953 | 16.858 | . 294825 | 1.444 | 4820 | 20.583 |
| $L_{\text {L }}$ | 2, 174.4026 | 8,398. 2667 | 150.041 | 41..741 | . 24758 | 4. 594 | . 852 | 39.255 |
| Hawail: ${ }^{\text {3 }}$ |  |  |  |  |  |  |  |  |
| $\mathbf{S}$ | 38.4587 | 110.0536 307.5480 | 57.006 14.960 | 18. 501 | . 29432 | 1.743 | . 367 | 20.874 39.180 |
| Northeast Africa: | 206. 4792 | 717.6459 | 79.146 | 25. 229 | . 25435 | -1. 548 5.098 | . 751 | 39.180 21.631 |
| Angola, Alrica: 4 |  |  |  |  |  |  |  |  |
| M I --. | 374.2714 | 1,497.3414 | 97.643 | 29.643 | . 247704 | 5. 521 | . 479 | 30.225 |
|  | 220.5800 | 845.3900 | 137.667 | 39.467 | . 24729 | 5.423 | . 679 | 40.044 |
| $\boldsymbol{Y}=$ greatest body depth: | 246.6014 | 855.8203 | 99879 | 25. 417 | 26800 | -1.351 | 799 | 25. 449 |
| $100^{2}-119^{\circ}$ W.: $L$ | 390.8457 | 1,173.1343 | 149.819 | 38. 714 | .32153 | -9.457 | . 848 | 35. 557 |
| $119^{\circ}-129^{\circ} \mathrm{W} .:$ L | 441.5200 | 1,284.4100 | 146. 721 | 36.800 | . 256569 | -. 847 | 1.577 | 35. 076 |
| $129^{\circ}-139^{\circ}$ W.: $L$ | 1,498. 6661 | 5,502.0583 | 144.948 | 36. 383 | . 25467 | $-.530$ | 1.488 | 35.124 |
| $139^{\circ}-149^{\circ} \mathrm{W} .: ~ L$ | 1,361. 7169 | 4,091.6786 | 148.338 | 37.717 | . 30010 | -6.799 | 1.118 | 35.215 |
| East Line Islands: | 150.7747 | 681.1294 | 102.456 | 24. 928 | . 21128 | 3. 281 | 807 |  |
| L | 1,267.7564 | 4,062.2382 | 145. 061 | 36.236 | . 28108 | -4. 538 | . 910 | 34.813 |
| West Line Islands: |  |  |  |  |  |  |  |  |
| S | 161.9377 | 599.3763 | 68.556 | 17.135 | . 24657 | . 231 | . 587 | 16. 258 |
| M | 569.4407 | 2,214.78:33 | 97.684 | 23.771 | . 22087 | 2.200 | . 295 | 24. 237 |
| $L$ | 591.7708 | 1,748.7343 | 138.179 | 34.204 | . 30106 | -7.396 | 1.090 | 34.752 |
| Phoenix Islands: |  |  |  |  |  |  |  |  |
|  | 89.1089 503.8539 | 369.7056 1.862 .3048 | 67.453 98.255 | 16.744 24.110 | . 22375 | 1. 6567 | .433 .988 | 16. 195 |
| $L$ | 275.9098 | 1.860. 80832 | 135.068 | 33. 602 | . 24398 | . 648 | 1. 254 | 34. 805 |
| East Marshall Islands: L | 284.8236 | 842.8003 | 136.279 | 33. 813 | . 30548 | -7.818 | . 860 | 34.949 |
| Bikini Island: S | 97.7194 | 416.0368 | 59.089 | 14.626 | . 22777 | 1. 181 | . 319 | 15. 886 |
| East Caroline Islands: |  |  |  |  |  |  |  |  |
| ${ }_{\text {S }}$ | 157.5883 488595 | 719.3893 1991.5484 | 65. 272 | 16.247 | . 202088 | 3. 0595 | . 459 | 16. 192 |
| $L$ | 575. 7756 | 1,882. 63.0 | 139.950 | 34.816 | . 26964 | -2.920 | 1. 123 | 34. 830 |
| Central Caroline Islands: |  |  |  |  |  |  |  |  |
| S | 148.8973 | 592. 7176 | 67.943 | 16.770 | . 23248 | . 941 | . 556 | 16.085 |
| M | 647. 5291 | 2, 653.3177 | 100.875 | 24.103 | . 22524 | 1.382 | . 706 | 23.906 |
| $L$ | 457.7347 | 1, 252. 3398 | 132.323 | 32. 856 | . 28304 | -4. 597 | 1.223 | 35.020 |
| Japan: S | 321.5547 | 1,255.2073 | 57.607 | 15.013 | . 25181 | . 501 | . 437 | 16.875 |
| Hawaii: | 08.98 | 409.915 | 52350 | 13.631 | 22042 | 2.092 | 504 | 16.419 |
| A | 162.894 I | 802.8818 | 101:953 | 25.732 | . 229420 | 2. 364 | . 879 | 25. 284 |
| $L$ | 3, 209.8397 | 10.060.9787 | 149.943 | 37. 965 | . 29805 | -6.726 | 1.274 | 35.001 |
| Northeast Africa: $\mathbf{S}$ | 225.3725 | 774.6375 | 79.146 | 20.837 | . 27455 | -. 893 | . 525 | 16.953 |
| $y^{\prime}=$ insertion ventral fin to anterior edge |  |  |  |  |  |  |  |  |
| $109^{\circ}-119^{\circ} \mathrm{W} .: ~ L$ | 288.0247 | 963.7465 | 150.212 | 43, 518 | . 27389 | 2.376 | 1. 207 | 40.721 |
| $119^{\circ}-129^{\circ} \mathrm{W} .:$ L | 351.6464 | 1,206. 2371 | 146. 721 | 41.583 | . 24097 | 6. 228 | 1.164 | 39. 964 |
| $129^{\circ}-139^{\circ} \mathrm{W} .: ~ L$. | 1,719.2287 | 6,003.8027 | 144.948 | 41. 126 | . 27776 | . 865 | 1.075 | 39.751 |
| $139^{\circ}-140^{\circ} \mathrm{W} .: ~ L$ | 1. 248.5543 | 3, 883.7779 | 148. 540 | 42. 007 | . 28450 | -. 253 | 1. 143 | 39.577 |
| East Line Islands: | 231.9206 |  |  |  |  |  |  |  |
| ${ }_{L}$ | 1. 208.9754 | 4.141.1737 | 145.432 | 28.384 40.485 | . 27522 | . 469 | 1.027 | 38. 990 |
| West Line Islands: |  |  |  |  |  |  |  |  |
| S. | 143.8737 | 495.3853 | 68.445 | 19.326 | . 27138 | . 751 | . 512 | 18. 391 |
| M | 738.3841 | 2,687. 2328 | 97.233 | 26. 992 | . 26389 | 1.333 | . 601 | 27.722 |
| L---------- | 459.4699 | -1:521.6909 | 138.334 | 38.473 | . 26548 | 1.748 | 1. 014 | 38.915 |
| Phoenix Islands: |  |  |  |  |  |  |  |  |
| S | 44. 2063 | 145.1658 1.627 .0607 | 68.905 97.188 | 19.149 | .28462 .26298 | $\begin{array}{r}-.470 \\ \mathbf{1} \\ \hline 1.82\end{array}$ | 412 .531 | 18.030 27.391 |
| $\boldsymbol{L}$ | 441.1425 | $1,627.0607$ 622.7878 | 97.188 134.289 | 20. 651 | . 262989 | -1.092 | . .951 | 27.391 39.250 |
| East Marshall Islands: L | 291.2231 | 838.0954 | 136.454 | 37.931 | . 30568 | -3.780 | . 973 | 39.015 |
| East Caroline Islands: |  |  |  |  |  |  |  |  |
| S. | 278.5460 | 972.9090 | 65.272 | 18.670 | . 27330 | . 831 | . 467 | 18.596 |
| M | 608.4060 | 2,209.4215 | 98.509 | 27.537 | . 26806 | 1.328 | . 629 | 27.934 |
| L -------------- | 644.2975 | 2,064.3486 | 139.989 | 39.031 | . 29587 | -2.388 | . 795 | 39.034 |
| Central Caroline Isiands: | 197.1489 | 680.9356 | 67.747 | 19.556 | . 27316 | 1.050 | . 573 | 18.805 |
| $\lambda^{\prime}$ | 817.7146 | 3, 006.1016 | 100.875 | 28. 281 | . 25.518 | 2.540 | . 709 | 28.058 |
| $L$ | 454.6795 | 1,249.9491 | 132.455 | 36. 603 | . 29115 | -1.961 | 1.147 | 38.800 |

$1 \mathrm{~S}, \mathrm{small}$, less than 80 cm ., compared at length of $65 \mathrm{em} . ; \mathrm{M}$, medium, 80 to 120 em ., compared at length of 100 em.: $L$, large, over 120 cm ., compared at length of $140 \mathrm{~cm} .{ }^{2} \mathrm{Sthaefer}(1952)$. $\quad{ }^{3}$ Godsil and Greenhood (1951). ${ }^{4}$ Schaefer and Walford (1950).


[^0]:    Note.-Approved for publication June 3, 1963.
    ${ }^{1}$ The Pacific yellowfn tuna has been named Neothunnus macropterus (Temminck and Schlegel) by recent authors. I consider the yellowfin to be a single world wide species, which I choose to call Thunnus albacares (see page 42S).

[^1]:    ${ }^{2}$ Now the Biological Laboratory of the Bureau of Commerclal Fisheries, Honolulu, Hawaii.

[^2]:    a This sample was compared with the Pacific samples by Royce (1953) and found to be most like the Phoenix Islands sample. It will not be further considered here.

[^3]:    ${ }^{4}$ An evaluation of the regression formulae will be found in the following section.
    ${ }^{3}$ This was usually more than about 15 percent (about four standard deviations) of the size of the character away from the general trend.

[^4]:    ${ }^{6}$ In the gap between longitude $109^{\circ} \mathrm{W}$. and the American coast (fig. 2), yullowfin have been taken by commercial vessels and research ships sponsored by the Inter-American Tropical Tuna Commission.

[^5]:    7 This table of partial correlations is one of the more laborious parts of the entire computation. The particular data were chosen during preliminary computations as a test of the method on rather widely dispersed groups, all with good sample coverage. The size group corresponds nearly but not exactly to size group $M$. I have assumed that the partial correlations of these body parts for what is essentially the medium-size group for five samples with wide coverage are the same for all areas and also for the small and large size groups.

[^6]:    ${ }^{8}$ I have ignored the slight variation in value of $n$ among different charaeters within the samples.

[^7]:    ${ }^{2}$ A detailed evaluation of the application of $D^{2}$ to an anthropometric survey may be found in Mahalanolis, Bose, and Roy (1937).
    10 Not available to me.

[^8]:    ${ }^{11}$ In this instance the seven characters show an overlap of 82 percent and the single character with the greatest difference shows an overlap of only 75 percent. This anomaly occurs because the other six characters when combined show less difference than the correction for small samples.

[^9]:    1 From Sloane (1707) fig. 1, table 1.
    2From Schaefer and Walford (1050), using the regressions for our large size group and assuming a fork length of 140 cm .
    3 From Godsil and Holmberg (1050), page 7 . converted from their ratios of part size to body length.

[^10]:    See footnotes at end of table.

